



Intro to Statistics with R: Analysis of Variance (ANOVA)

# ANOVA

# Analysis of variance (ANOVA)

- Compare groups means across 3+ groups
- Separate, independent groups of subjects
- More than 2 group means from same subjects (i.e. repeated measures)

# Working memory training

- Four independent groups (8, 12, 17, 19 sessions)
- Measured IQ before and after training
- Dependent variable is IQ gain
- Null hypothesis: All groups are equal (i.e. all groups have equal IQ gain)
- Alternative hypothesis: More training leads to larger IQ gain



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# Exploration of the F-test

# Working memory ANOVA

- Null hypothesis: all groups are equal
- ANOVA provides a significance test
- Test statistic is the F-test (or F-ratio)

$$F = \frac{\text{Variance between groups}}{\text{Variance within groups}} = \frac{\text{Systematic variance}}{\text{Unsystematic variance}}$$

- Large F-ratio indicates significant effect

# Getting to a p-value

- Similar to t-test and family of t-distributions
- Family of F-distributions depends on...
  - Number of subjects in sample
  - Number of groups being compared



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# F-Ratio

# F-ratio

$$F = \frac{\text{Variance between groups}}{\text{Variance within groups}}$$

$$F = \frac{\text{Systematic variance}}{\text{Unsystematic variance}}$$

$$F = \frac{\text{"Good" variance}}{\text{"Bad" variance}}$$

$$F = \frac{MS_{\text{Between}}}{MS_{\text{Within}}}$$





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# More ANOVA

# ANOVA (continued)

- Calculate a total sum of squares
- Calculate a total degrees of freedom
- Sum of between groups value and within groups value

# Summary Table

Source	SS	df	MS	F
A	$n \sum (Y_j - Y_T)^2$	$a - 1$	$SS_A / df_A$	$MS_A / MS_{S/A}$
S/A	$\sum (Y_{ij} - Y_j)^2$	$a(n - 1)$	$SS_{S/A} / df_{S/A}$	-
Total	$\sum (Y_{ij} - Y_T)^2$	$N - 1$	-	-

# Effect size

- F-test biased by sample size
- Supplement with effect size
- $R^2 = \eta^2$  (eta-squared)  $\longrightarrow$  **Percentage of variance in the dependent variable explained by the independent variable**
- $\eta^2 = SS_A / SS_{\text{Total}}$

# Assumptions

- Dependent variable is continuous (i.e. interval or ratio variable)
- Dependent variable is normally distributed
- Homogeneity of variance (check with Levene's test)