The prior model BAYESIAN MODELING WITH RJAGS



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Course goals

- Explore foundational, generalizable Bayesian models (eg: Beta-Binomial, Normal-Normal, and Bayesian regression)
- **Define**, **compile**, and **simulate** Bayesian models using RJAGS
- Conduct Bayesian posterior inference using RJAGS output

Bayesian elections: The prior

0.3 0.4 0.7 0.5 0.6 proportion of votes



Bayesian elections: The prior





Bayesian elections: The prior







Bayesian elections: The data







Bayesian elections: The posterior







Bayesian elections: New data







Bayesian elections: New posterior







Bayesian elections: Newer data







Bayesian elections: Newer posterior







Bayesian thinking

A Bayesian posterior model:

- Combines insights from the ulletprior model & observed data
- Evolves as new data come \bullet in





Building a prior model

- p = proportion that supportyou
- p is between 0 and 1
- The prior model for p is a Beta distribution with shape parameters 45 and 55

 $p \sim ext{Beta}(45, 55)$





Tuning the prior







Let's practice!



Data & the likelihood

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Polling data

Parameter

p = proportion that supportyou

Data

X=6 of n=10 polled voters plan to vote for you

Insights

You are more likely to have observed these data if p pprox 0.6 than if p < 0.5.





Modeling the dependence of X on p

Poll assumptions:

voters are independent p = probability that a voter supports you

- X = number of n polled voters that support you (count of successes in *n* independent trials, each having probability of success p)
- Conditional distribution of X given p: $X \sim \operatorname{Bin}(n,p)$



Dependence of X on p







Dependence of X on p







Dependence of X on p



datacamp



Dependence of X on p





What's the likelihood?







Likelihood

The likelihood function

summarizes the likelihood of observing polling data Xunder different values of the underlying support parameter p. It is a function of p.

- High likelihood $\Rightarrow p$ is \bullet compatible with the data
- Low likelihood $\Rightarrow p$ is not compatible with the data





Let's practice!



The posterior model BAYESIAN MODELING WITH RJAGS



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Bayesian election model

prior: $p \sim ext{Beta}(45, 55)$



р





Bayesian election model

Prior: $p \sim ext{Beta}(45, 55)$

Likelihood: $X \sim \mathrm{Beta}(10, p)$



р



Bayesian election model

Prior: $p \sim ext{Beta}(45, 55)$

Likelihood: $X \sim {
m Bin}(10,p)$



р



Posterior model of p

Prior: $p \sim ext{Beta}(45, 55)$

Likelihood: $X \sim {
m Bin}(10,p)$

Bayes' Rule:

posterior \propto prior \times likelihood



р



Getting started with RJAGS

RJAGS combines the power of R with the JAGS (Just Another Gibbs Sampler) engine. To get started:

- Download the JAGS program outside R
- Within R, install the rjags package \bullet



Bayesian models in RJAGS: DEFINE

```
DEFINE the model
#
vote_model <- "model{</pre>
    # Likelihood model for X
    X \sim dbin(p, n)
    # Prior model for p
```

```
p ~ dbeta(a, b)
```

}"

- $X \sim \operatorname{Bin}(n,p)$
- $p \sim \text{Beta}(a, b)$
- Warning: the rjags function dbin() is different than base dbinom()



Bayesian models in RJAGS: COMPILE

```
# DEFINE the model
vote_model <- "model{</pre>
    # Likelihood model for X
    X \sim dbin(p, n)
    # Prior model for p
    p ~ dbeta(a, b)
}"
# COMPTLE the model
vote_jags_A <- jags.model(textConnection(vote_model),</pre>
    data = list(a = 45, b = 55, X = 6, n = 10),
    inits = list(.RNG.name = "base::Wichmann-Hill", .RNG.seed = 100))
```



Bayesian models in RJAGS: SIMULATE

```
# DEFINE the model
vote_model <- "model{</pre>
    # Likelihood model for X
    X \sim dbin(p, n)
    # Prior model for p
    p ~ dbeta(a, b)
}"
# COMPILE the model
vote_jags <- jags.model(textConnection(vote_model),</pre>
    data = list(a = 45, b = 55, X = 6, n = 10),
    inits = list(.RNG.name = "base::Wichmann-Hill", .RNG.seed = 100))
# SIMULATE the posterior
vote_sim <- coda.samples(model = vote_jags,</pre>
    variable.names = c("p"),
    n.iter = 10000)
```

Bayesian models in RJAGS: SIMULATE

PLOT the simulated posterior plot(vote_sim, trace = FALSE)



N = 10000 Bandwidth = 0.007935

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Let's practice!

