

Interpreting GAM outputs

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R



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GAM summaries

```
mod_hwy <- gam(hw.mpg ~ s(weight) + s(rpm) +  
               s(price) + s(comp.ratio) +  
               s(width) + fuel + cylinders,  
               data = mpg, method = "REML")
```

```
summary(mod_hwy)
```

```

Family: gaussian
Link function: identity

Formula:
hw.mpg ~ s(weight) + s(rpm) + s(price) + s(comp.ratio) +
  s(width) + fuel

Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  23.873      3.531   6.760 1.89e-10 ***
fuelgas      7.571       3.922   1.931  0.0551 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Approximate significance of smooth terms:
              edf Ref.df      F  p-value
s(weight)    6.254  7.439 20.909 < 2e-16 ***
s(rpm)        7.499  8.285  8.534 2.07e-09 ***
s(price)      2.681  3.421  1.678  0.155
s(comp.ratio) 1.000  1.001 18.923 2.22e-05 ***
s(width)      1.001  1.001  0.357  0.551
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

R-sq.(adj) =  0.89   Deviance explained = 90.1%
REML = 464.81  Scale est. = 5.171      n = 199

```

GAM summaries (3)

```
summary(mod_hwy)
```

```
Family: gaussian
```

```
Link function: identity
```

```
Formula:
```

```
hw.mpg ~ s(weight) + s(rpm) + s(price) +  
         s(comp.ratio) + s(width) + fuel
```

```
...
```

GAM summaries (4)

```
summary(mod_hwy)
```

```
...  
Parametric coefficients:  
              Estimate Std. Error t value Pr(>|t|)  
(Intercept)  23.873     3.531    6.760 1.89e-10 ***  
fuelgas       7.571     3.922    1.931  0.0551 .  
---  
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '  
...
```

GAM summaries (5)

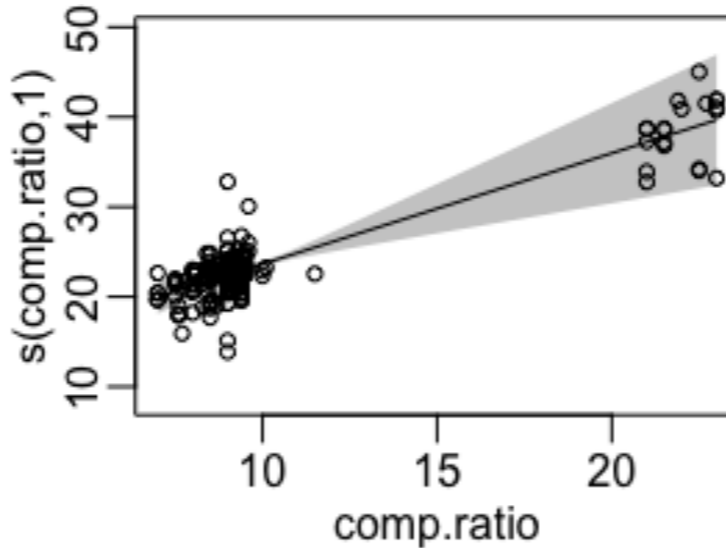
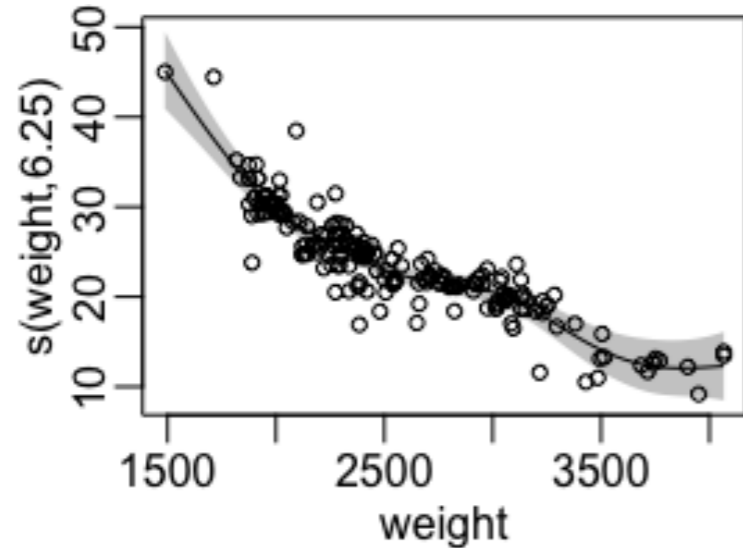
```
summary(mod_hwy)
```

```
...
Approximate significance of smooth terms:
              edf Ref.df      F  p-value
s(weight)      6.254  7.439 20.909 < 2e-16 ***
s(rpm)         7.499  8.285  8.534 2.07e-09 ***
s(price)       2.681  3.421  1.678  0.155
s(comp.ratio)  1.000  1.001 18.923 2.22e-05 ***
s(width)       1.001  1.001  0.357  0.551
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
...
```

Effective degrees of freedom

Approximate significance of smooth terms:

	edf	Ref.df	F	p-value		
s(weight)	6.254	7.439	20.909	< 2e-16	***	<--
s(rpm)	7.499	8.285	8.534	2.07e-09	***	
s(price)	2.681	3.421	1.678	0.155		
s(comp.ratio)	1.000	1.001	18.923	2.22e-05	***	<--
s(width)	1.001	1.001	0.357	0.551		



Significance of smooth terms

Approximate significance of smooth terms:

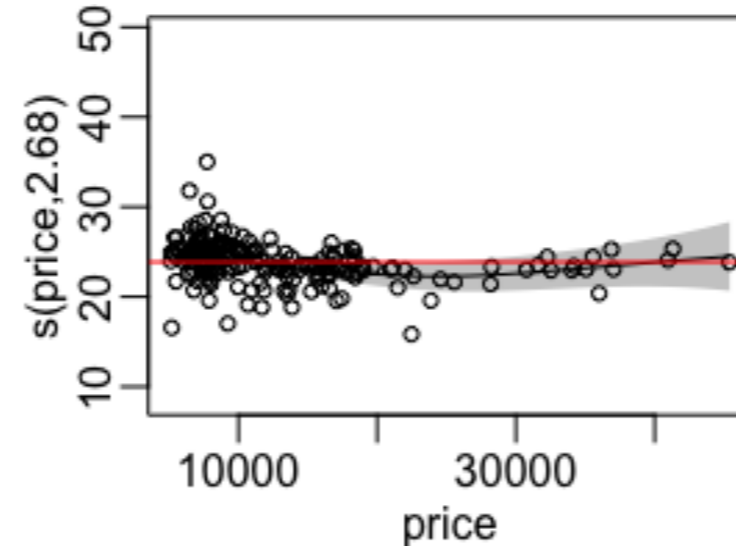
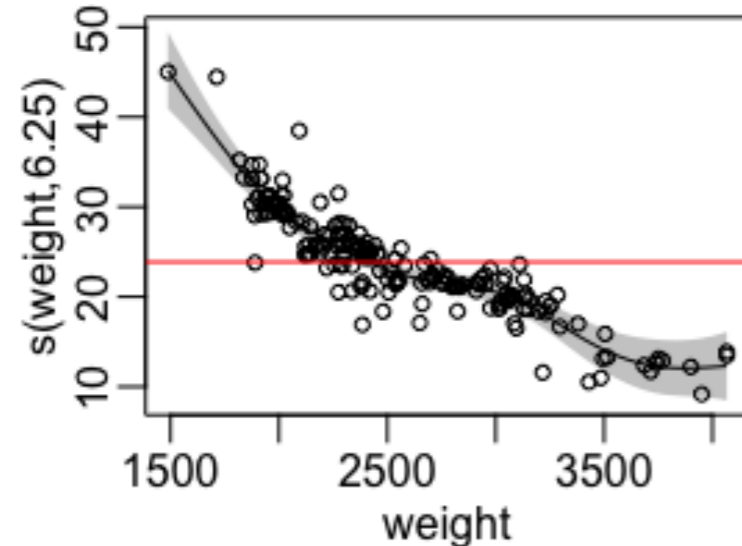
	edf	Ref.df	F	p-value	
s(weight)	6.254	7.439	20.909	< 2e-16	***
s(rpm)	7.499	8.285	8.534	2.07e-09	***
s(price)	2.681	3.421	1.678	0.155	
s(comp.ratio)	1.000	1.001	18.923	2.22e-05	***
s(width)	1.001	1.001	0.357	0.551	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Significance of smooth terms (2)

Approximate significance of smooth terms:

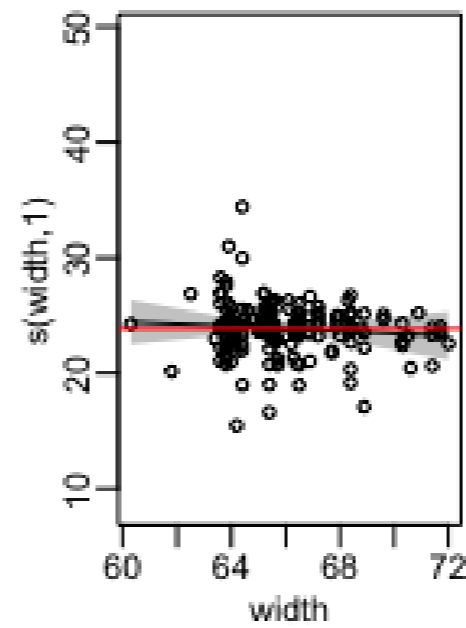
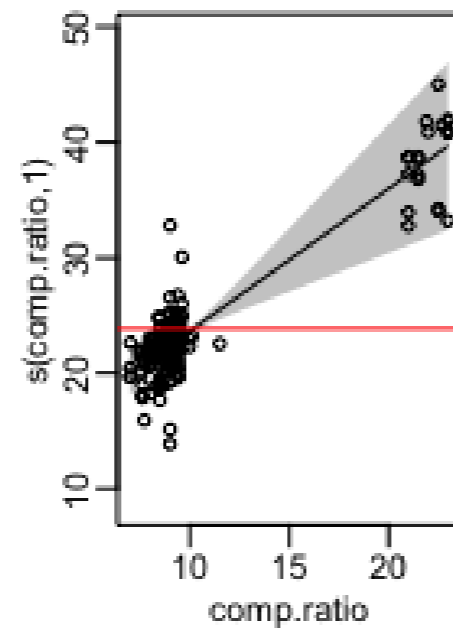
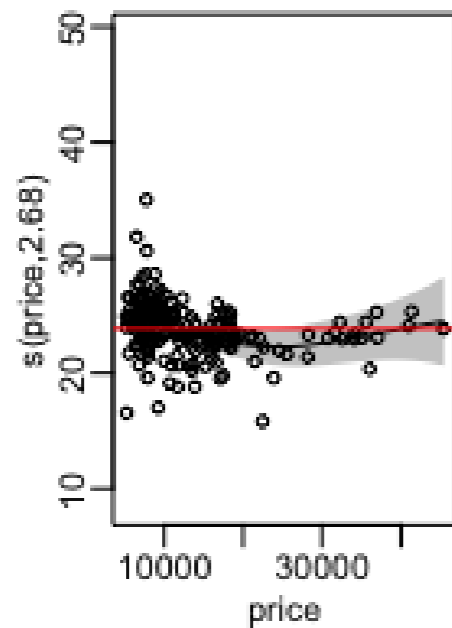
	edf	Ref.df	F	p-value		
s(weight)	6.254	7.439	20.909	< 2e-16	***	<--
s(rpm)	7.499	8.285	8.534	2.07e-09	***	
s(price)	2.681	3.421	1.678	0.155		<--
s(comp.ratio)	1.000	1.001	18.923	2.22e-05	***	
s(width)	1.001	1.001	0.357	0.551		



Significance and effective degrees of freedom

Approximate significance of smooth terms:

	edf	Ref.df	F	p-value	
s(weight)	6.254	7.439	20.909	< 2e-16	***
s(rpm)	7.499	8.285	8.534	2.07e-09	***
s(price)	2.681	3.421	1.678	0.155	<--
s(comp.ratio)	1.000	1.001	18.923	2.22e-05	*** <--
s(width)	1.001	1.001	0.357	0.551	<--



Let's practice!

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R

The plot command

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R



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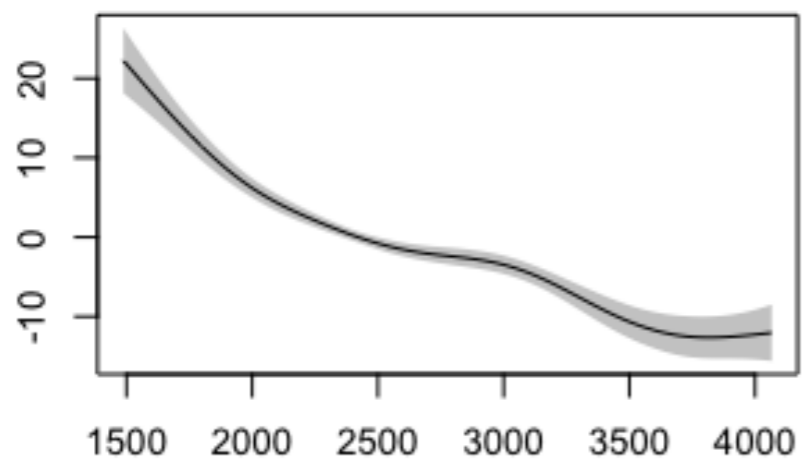
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The plot command

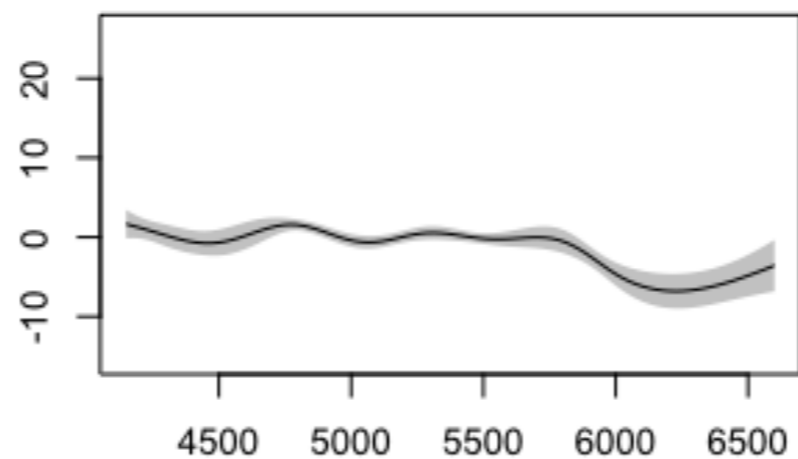
```
plot(gam_model)
```

```
?plot.gam
```

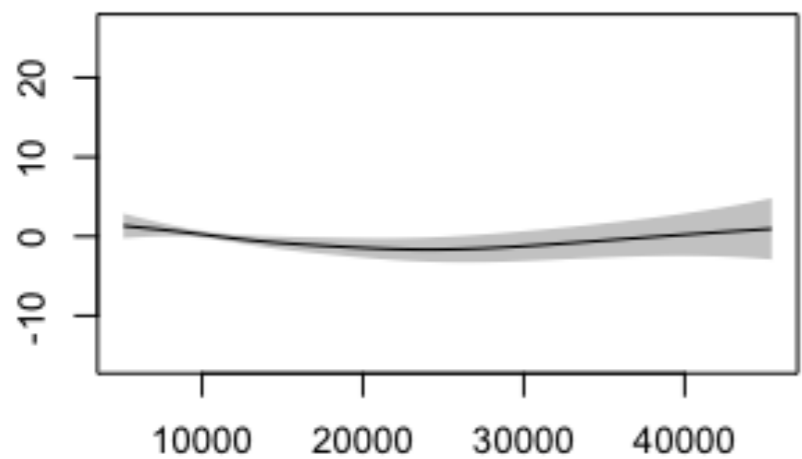
Partial Effect Plots



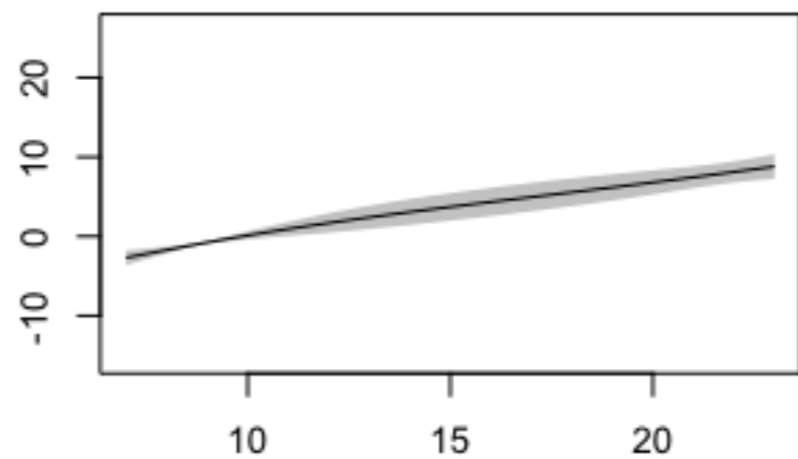
weight



rpm



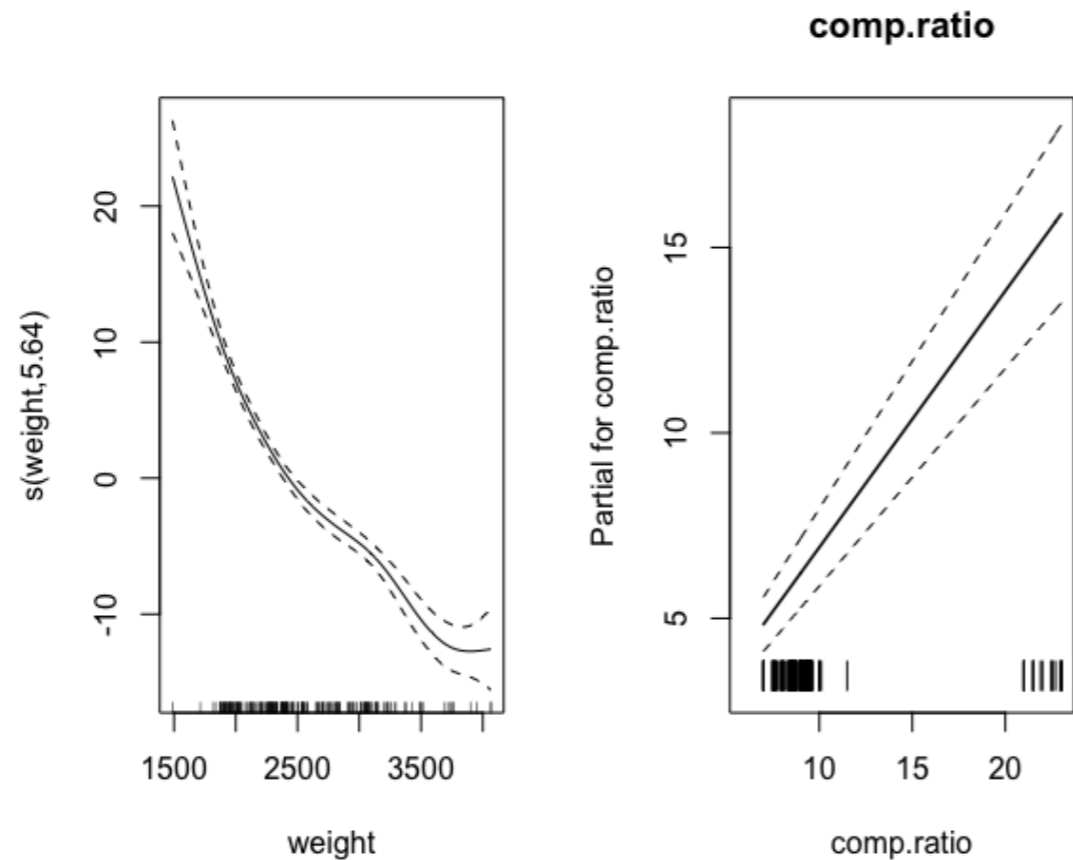
price



comp.ratio

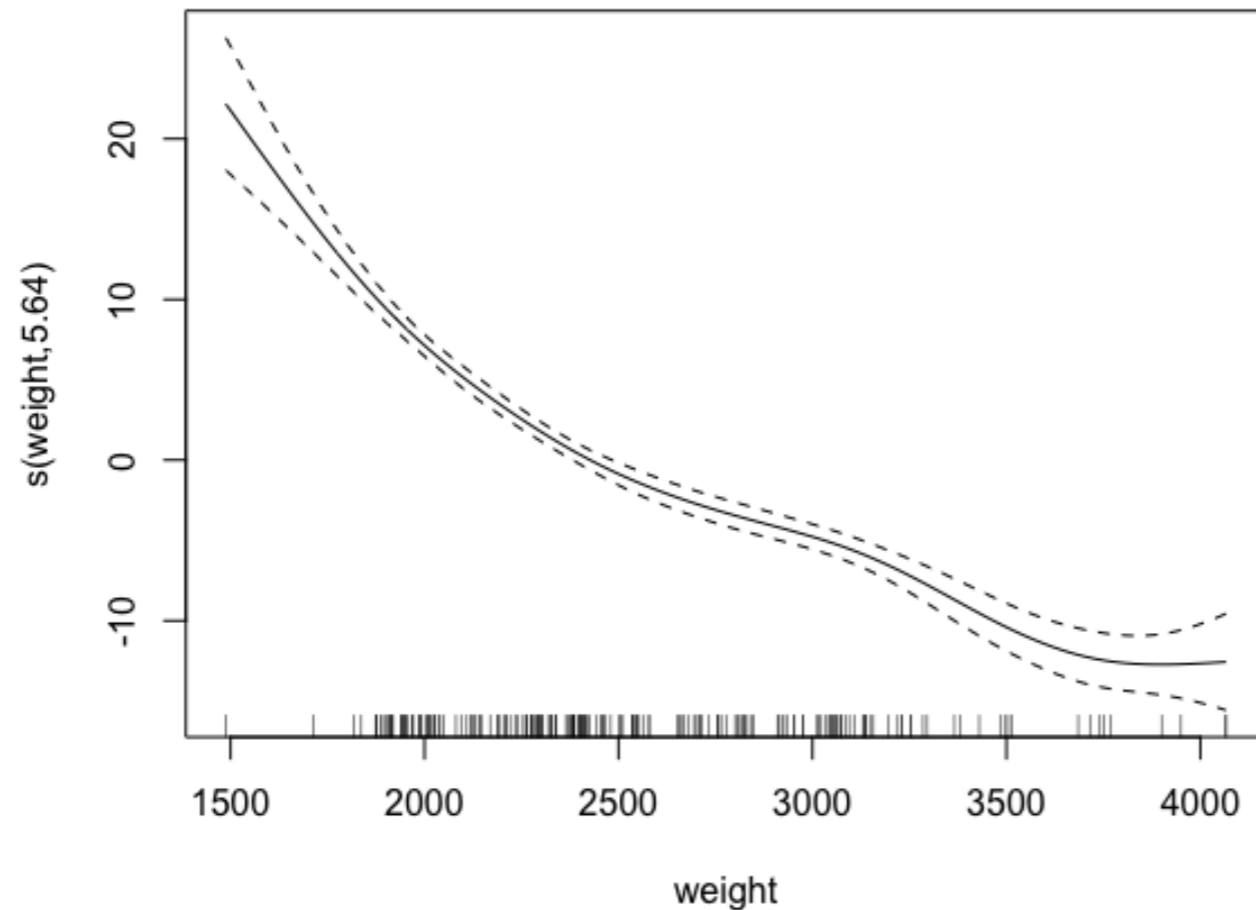
Selecting partial effects

```
plot(gam_model, select = c(2, 3))  
plot(gam_model, pages = 1)  
plot(gam_model, pages = 1, all.terms = TRUE)
```



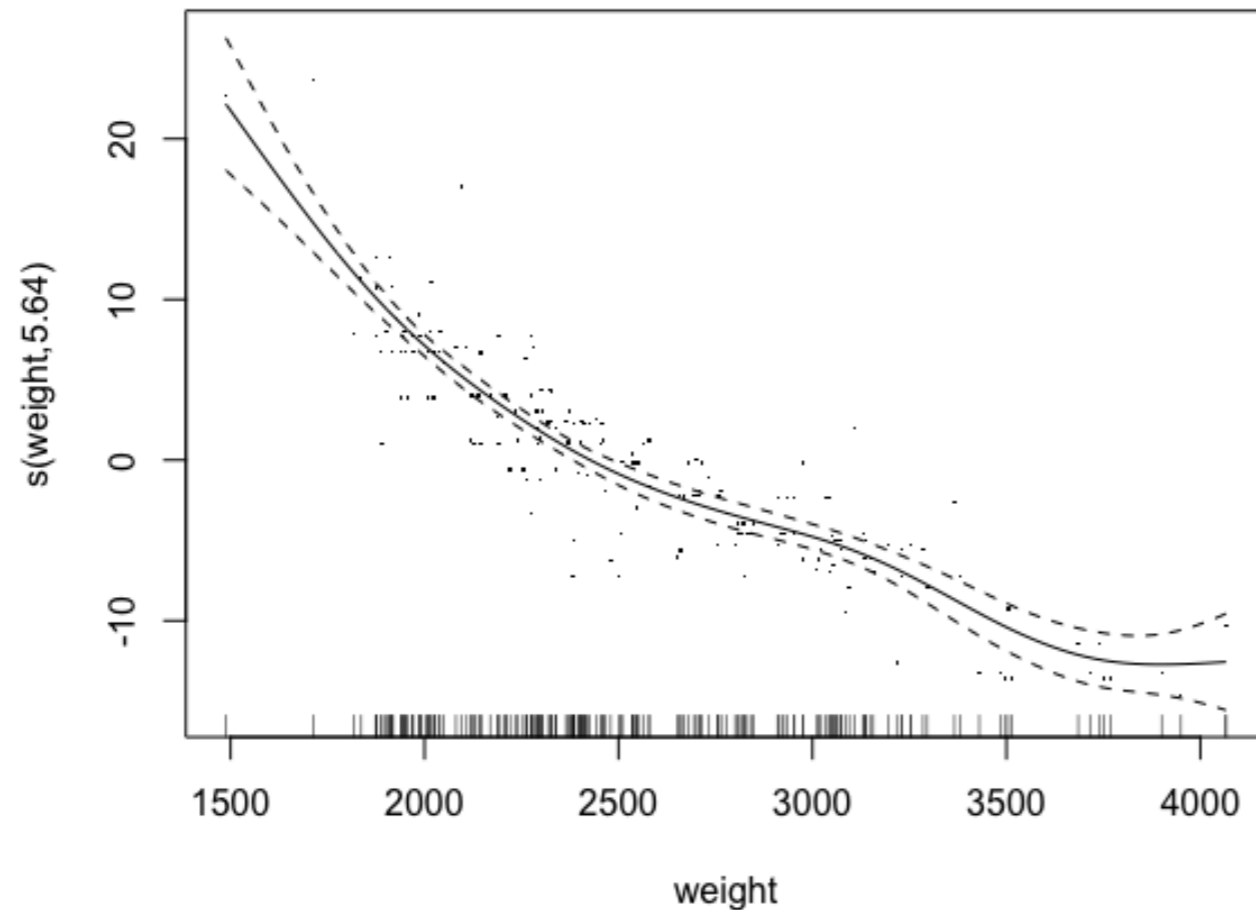
Showing data on the plots

```
plot(gam_model, rug = TRUE)
```



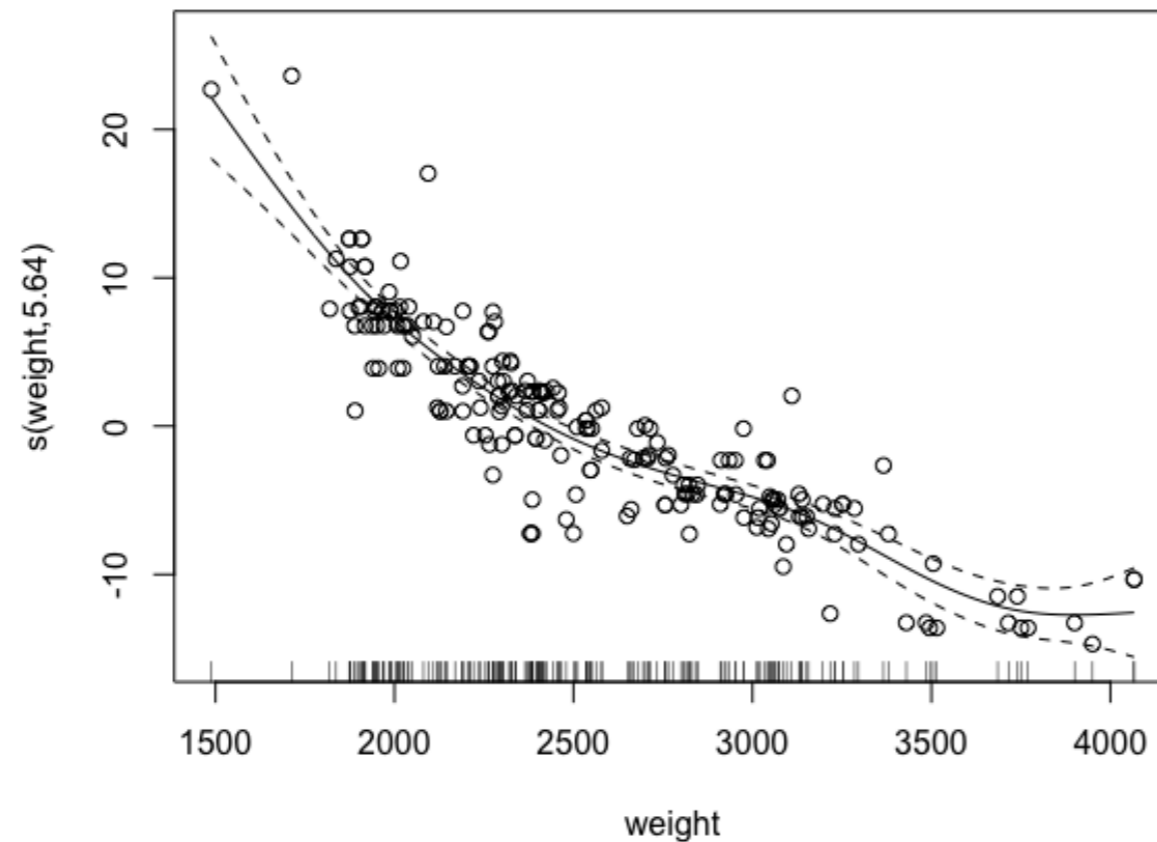
Showing data on the plots (2)

```
plot(gam_model, residuals = TRUE)
```



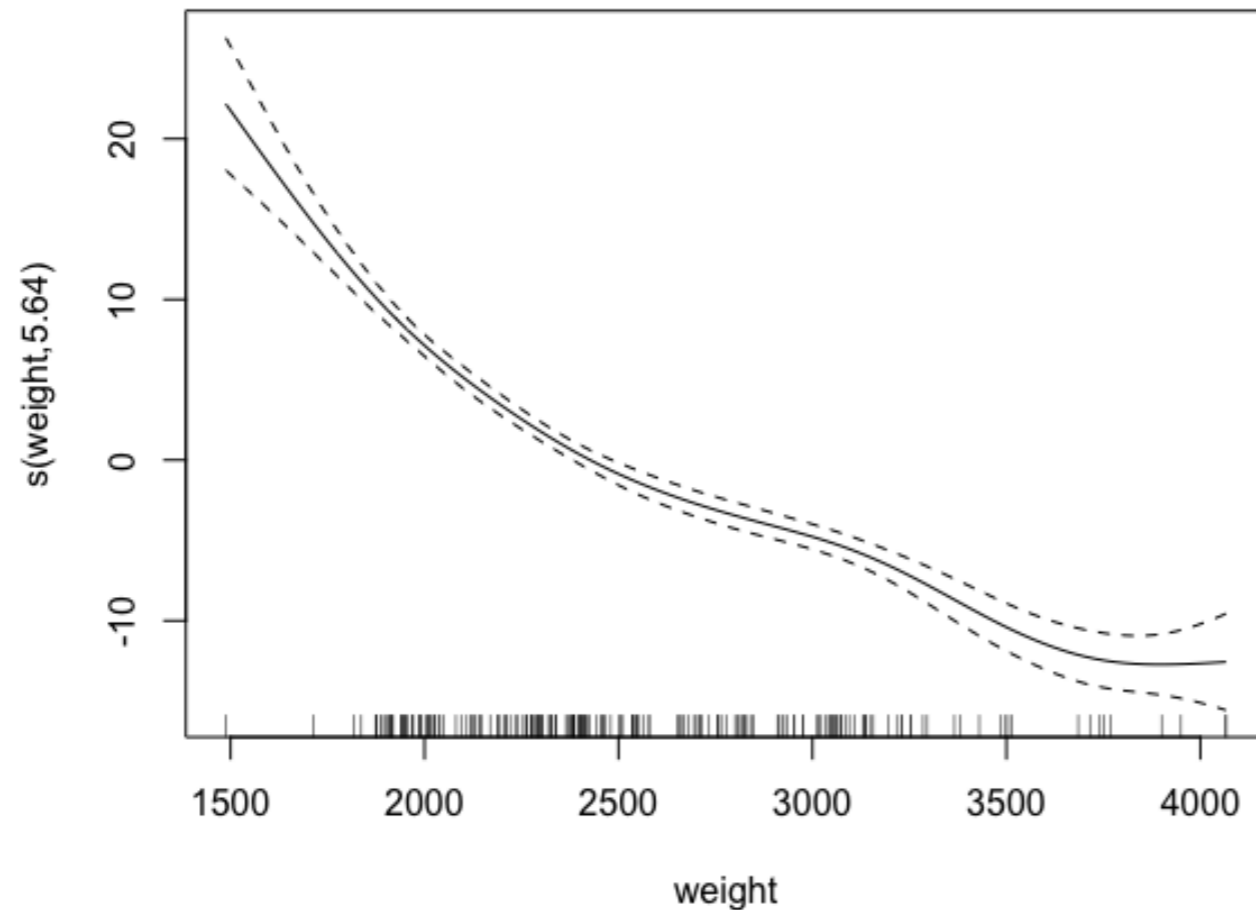
Showing data on the plots (3)

```
plot(gam_model, rug = TRUE, residuals = TRUE,  
     pch = 1, cex = 1)
```



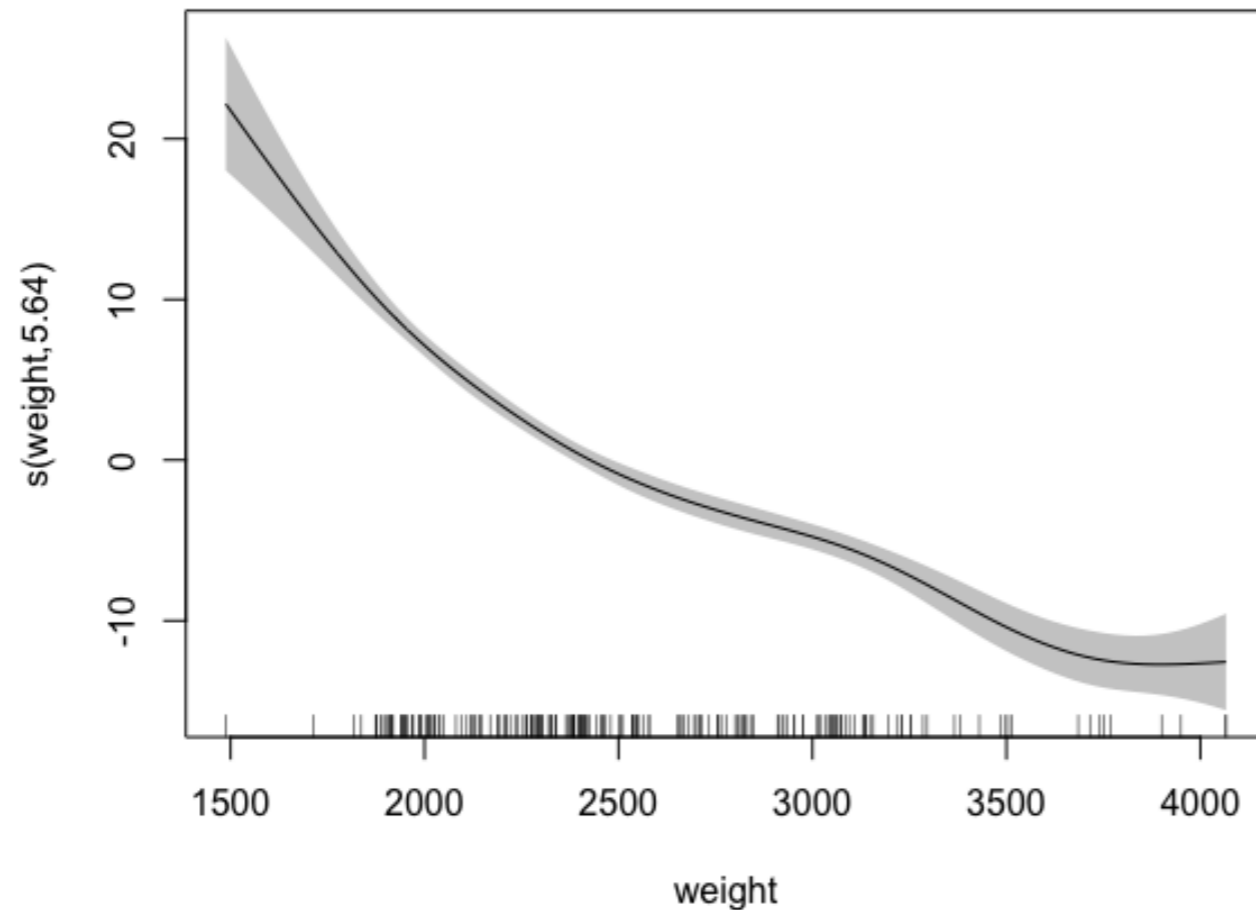
Showing standard errors

```
plot(gam_model, se = TRUE)
```



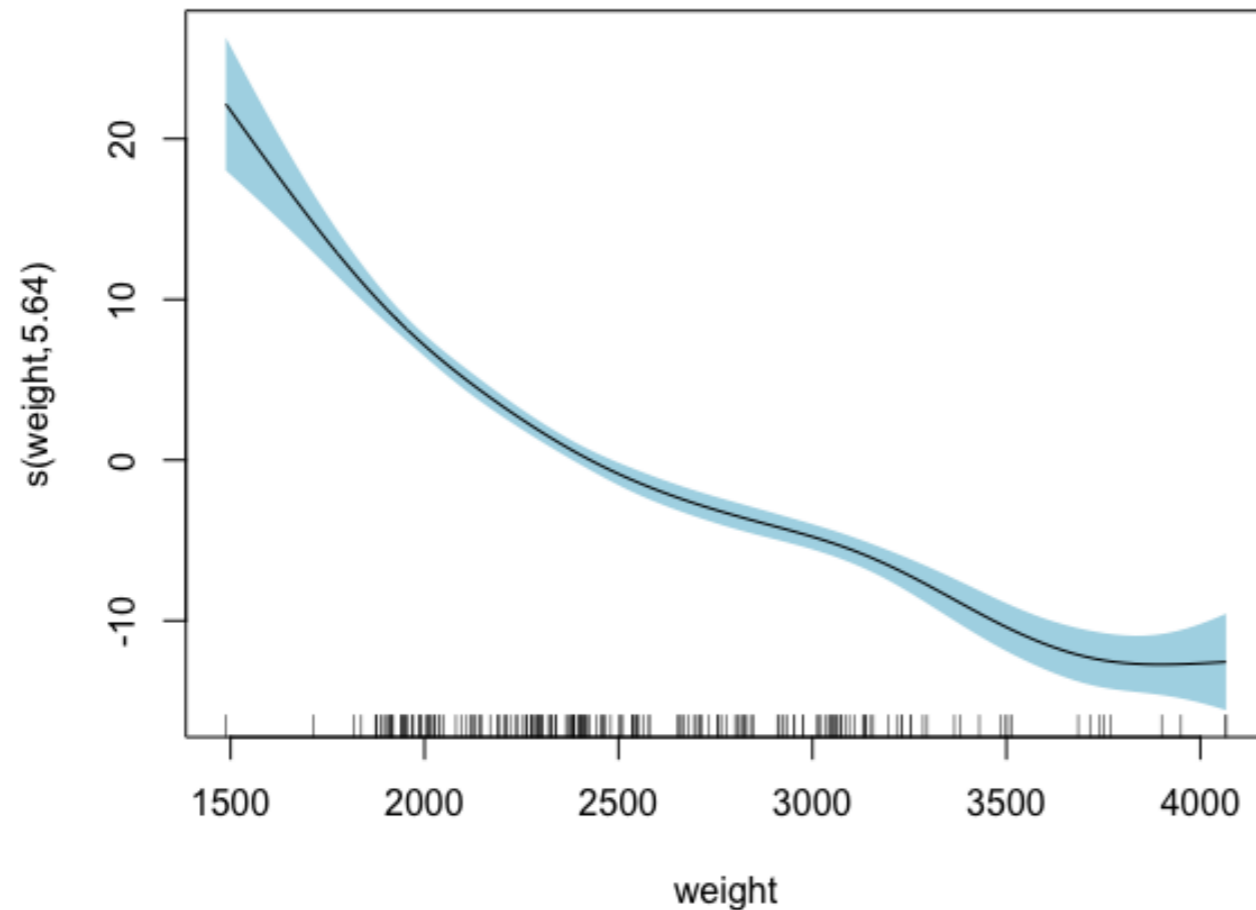
Showing standard errors (2)

```
plot(gam_model, shade = TRUE)
```



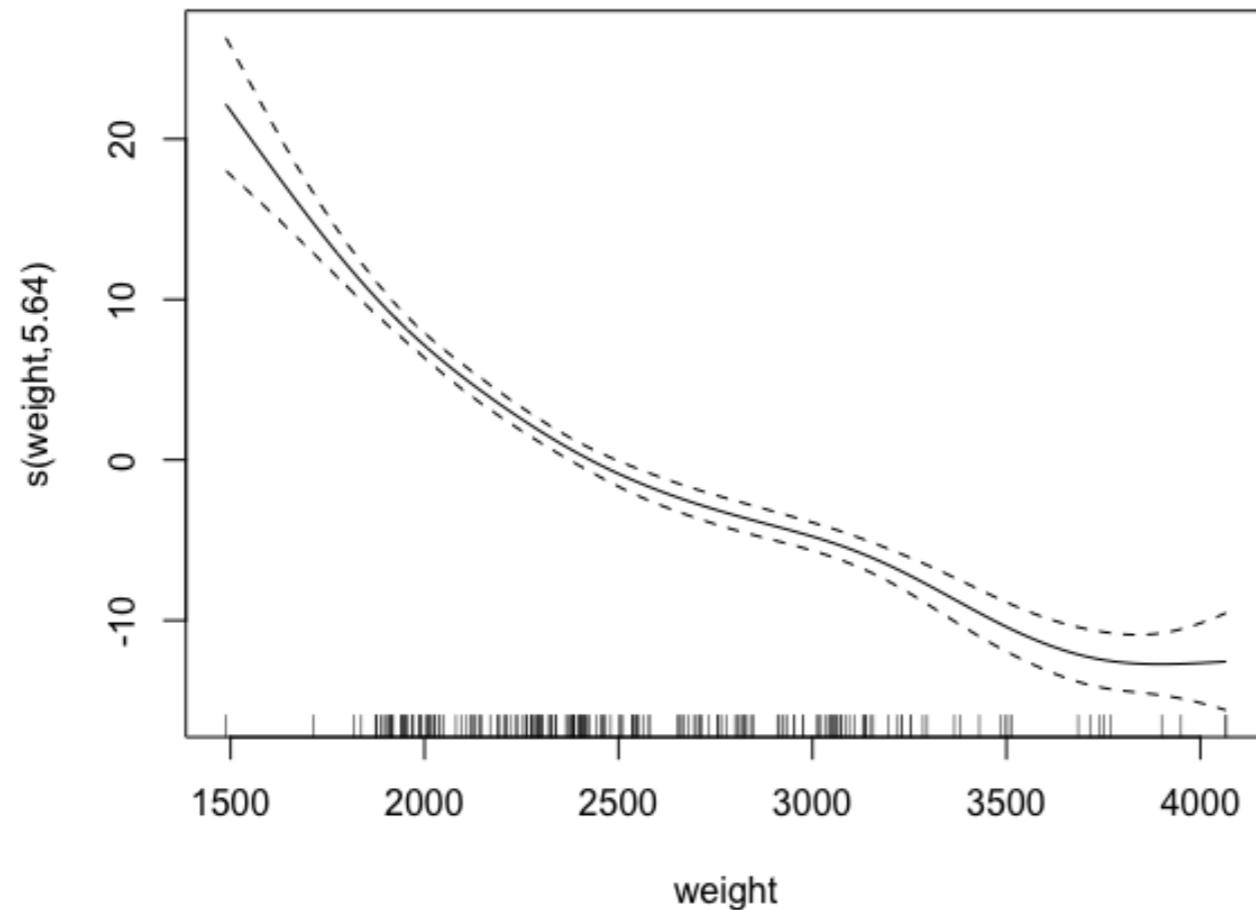
Showing standard errors

```
plot(gam_model, shade = TRUE, shade.col = "lightblue")
```



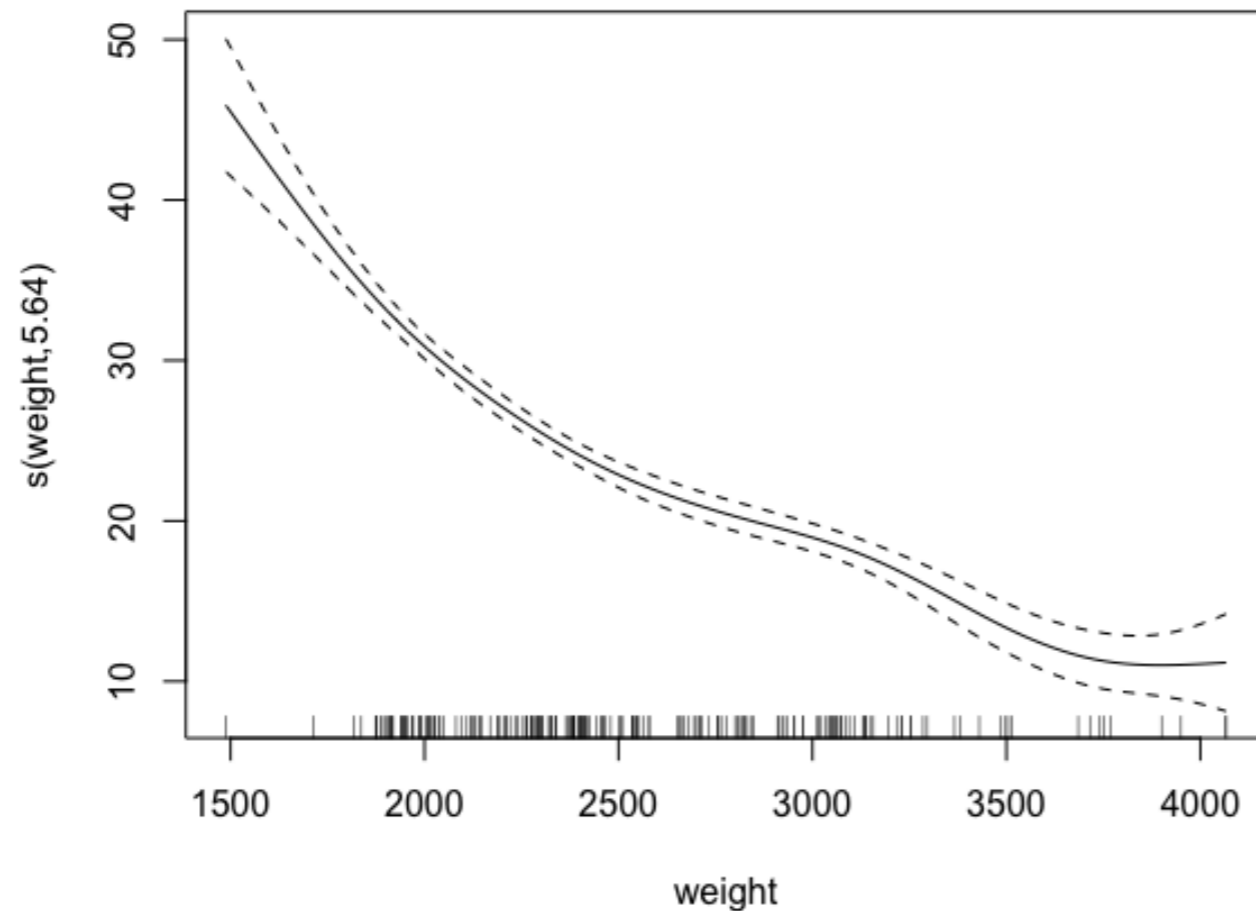
Transforming standard errors

```
plot(gam_model, seWithMean = TRUE)
```



Transforming standard errors (2)

```
plot(gam_model, seWithMean = TRUE, shift = coef(gam_model)[1])
```



**Now lets make some
plots!**

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R

Model checking with `gam.check()`

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R

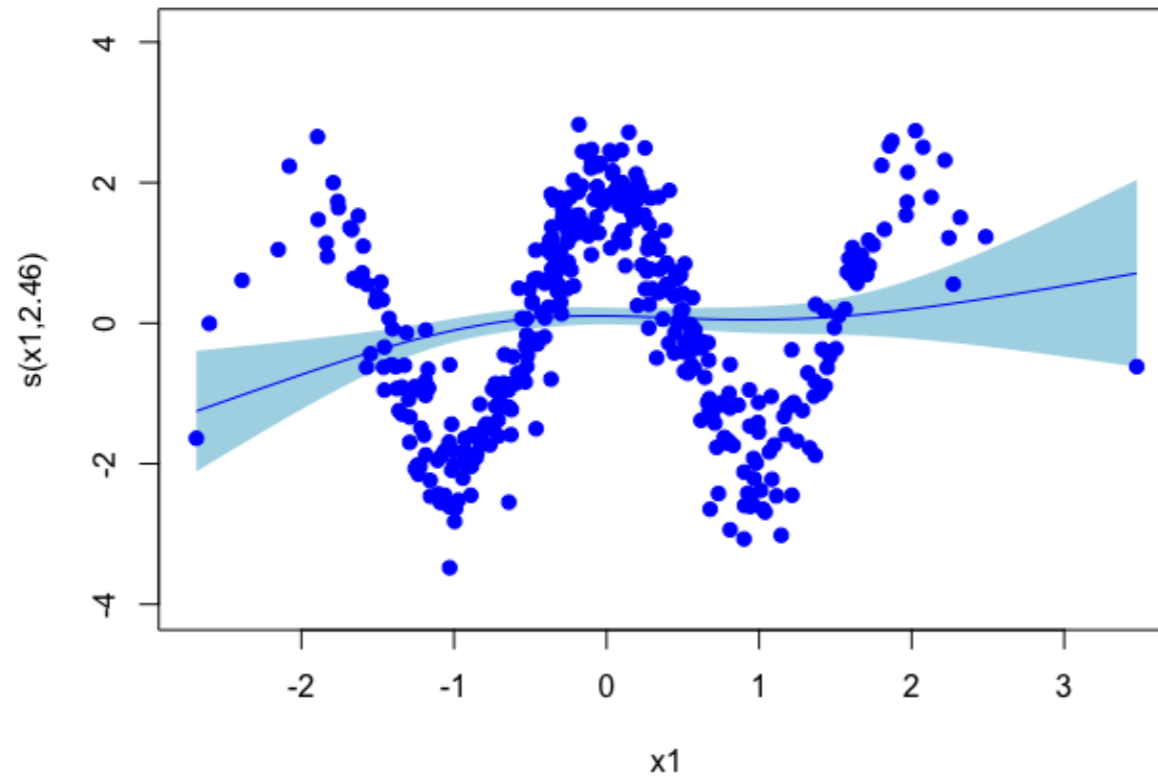


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Pitfall one: inadequate basis number

```
mod <- gam(y ~ s(x1, k = 4) + s(x2, k = 4),  
           data = check_data, method = "REML")
```



```
gam.check(mod)
```

```
Method: REML   Optimizer: outer newton  
full convergence after 9 iterations.  
Gradient range [-0.0001467222,0.00171085]  
(score 784.6012 & scale 2.868607).  
Hessian positive definite, eigenvalue range [0.00014,198.5]  
Model rank = 7 / 7
```

Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

	k'	edf	k-index	p-value
s(x1)	3.00	1.00	0.35	<2e-16 ***
s(x2)	3.00	2.88	1.00	0.52

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1

Running gam.check (2)

```
mod <- gam(y ~ s(x1, k = 12) + s(x2, k = 4),  
           data = dat, method = "REML")  
gam.check(mod)
```

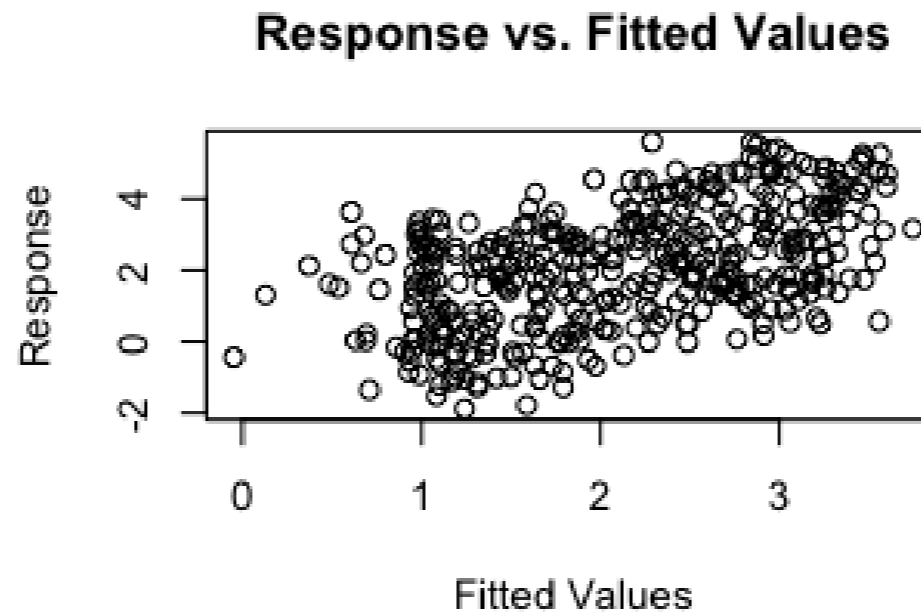
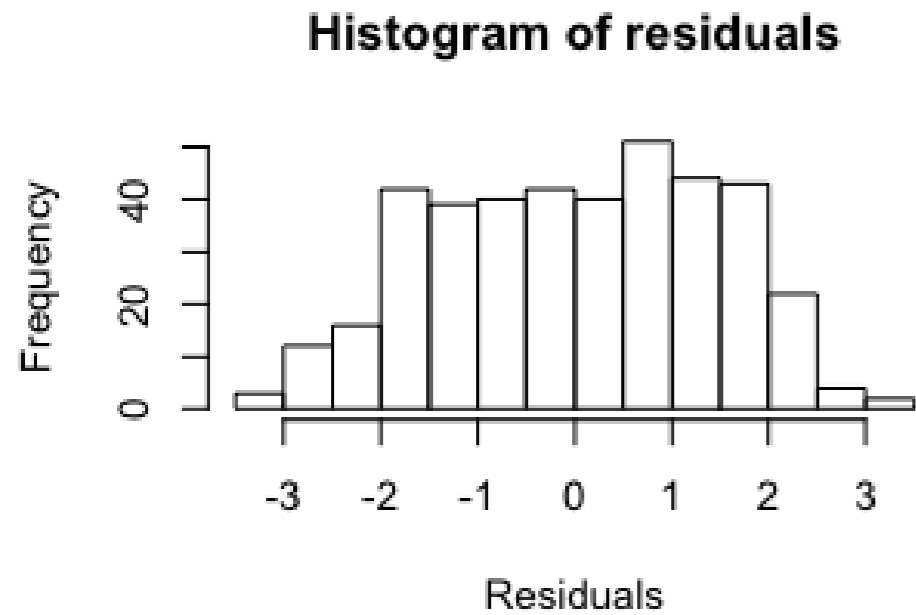
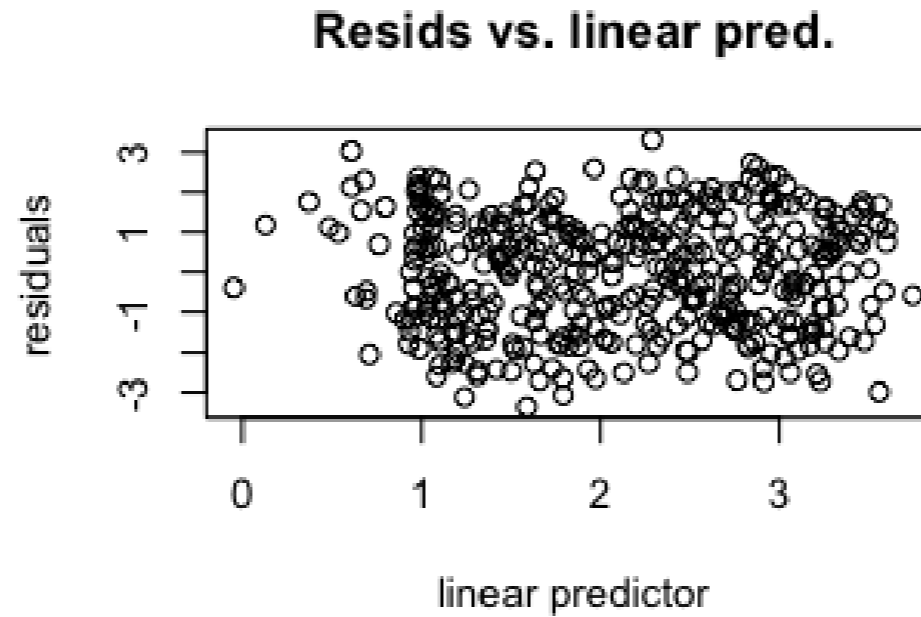
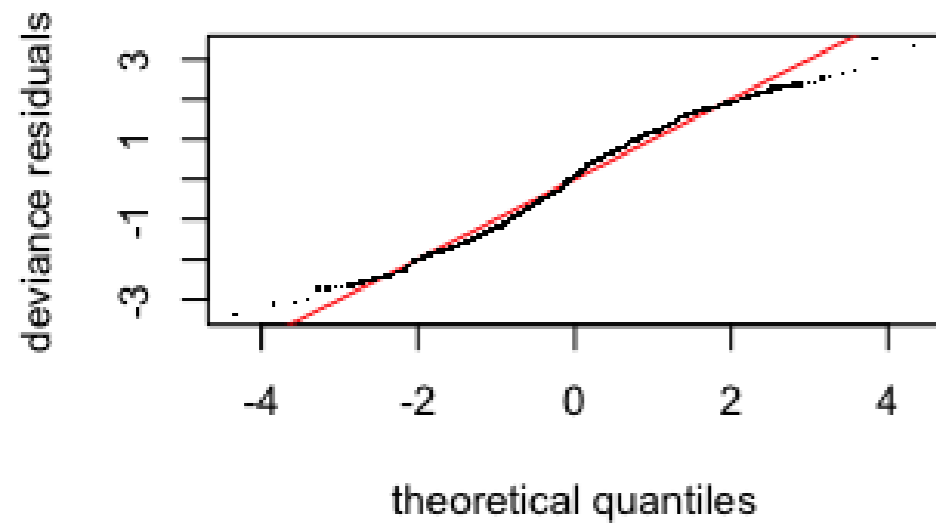
```
...  
  
      k'   edf k-index p-value  
s(x1) 11.00 10.85   1.05  0.830  
s(x2)  3.00  2.98   0.89  0.015 *
```

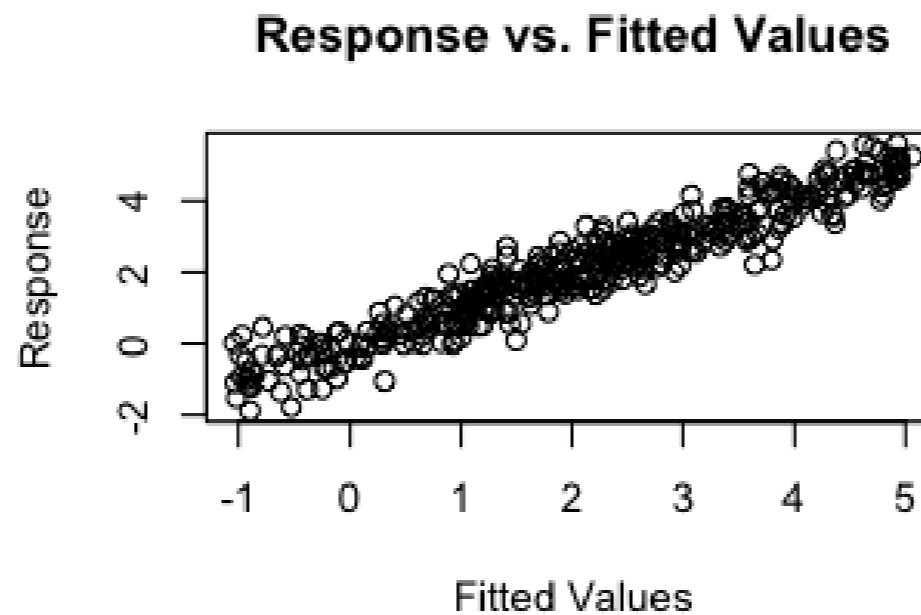
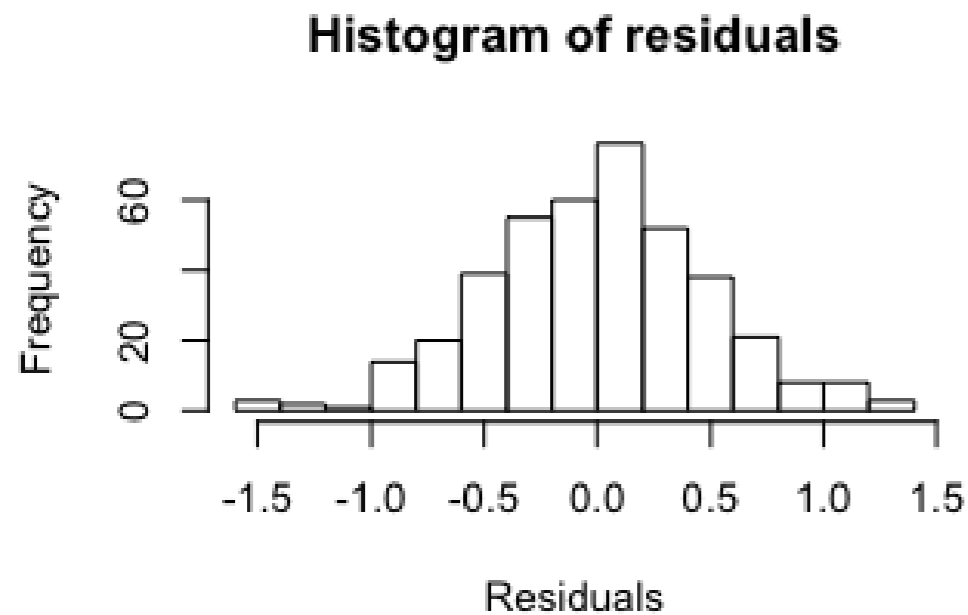
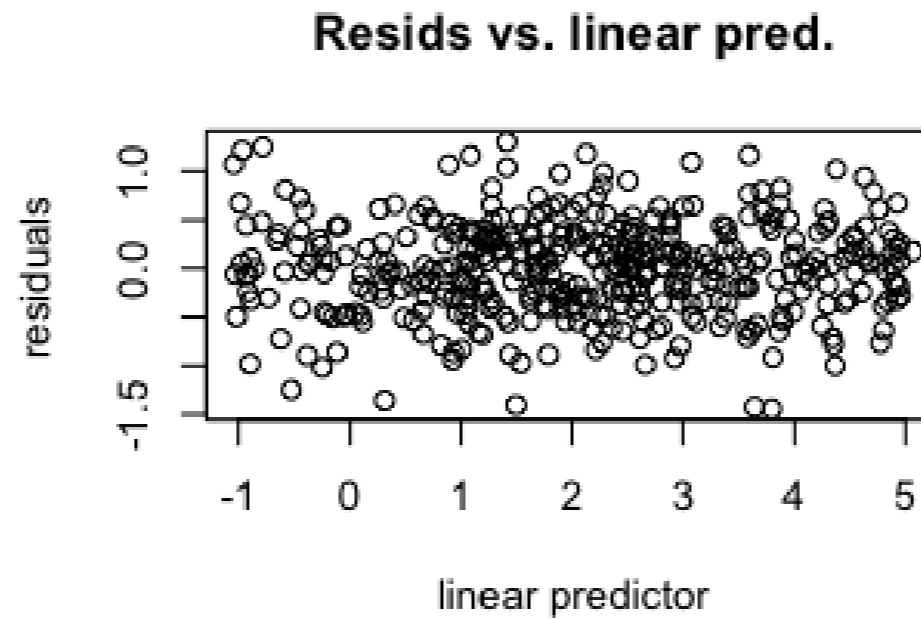
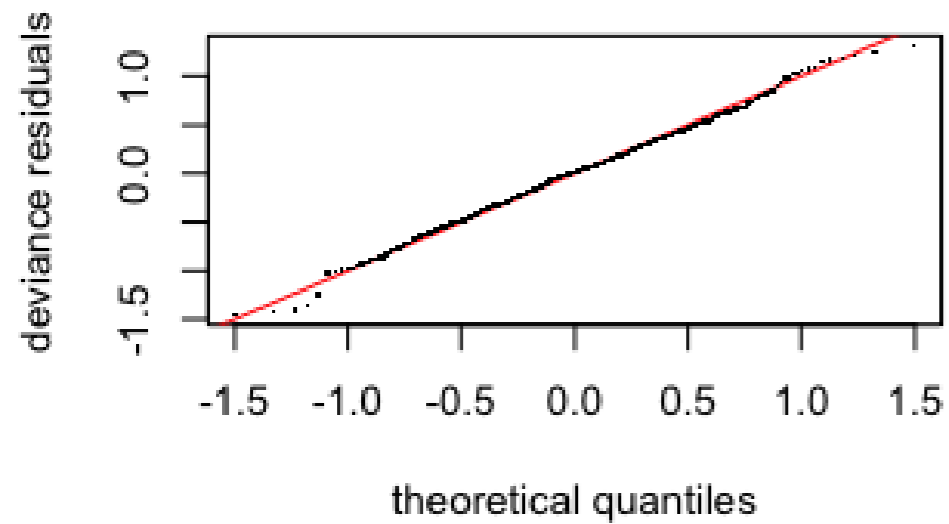
```
...
```

Running gam.check (3)

```
mod <- gam(y ~ s(x1, k = 12) + s(x2, k = 12),  
           data = dat, method = "REML")  
gam.check(mod)
```

```
...  
           k'   edf k-index p-value  
s(x1) 11.00 10.86   1.08   0.94  
s(x2) 11.00  7.78   0.94   0.12  
...
```





Let's check some models

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R

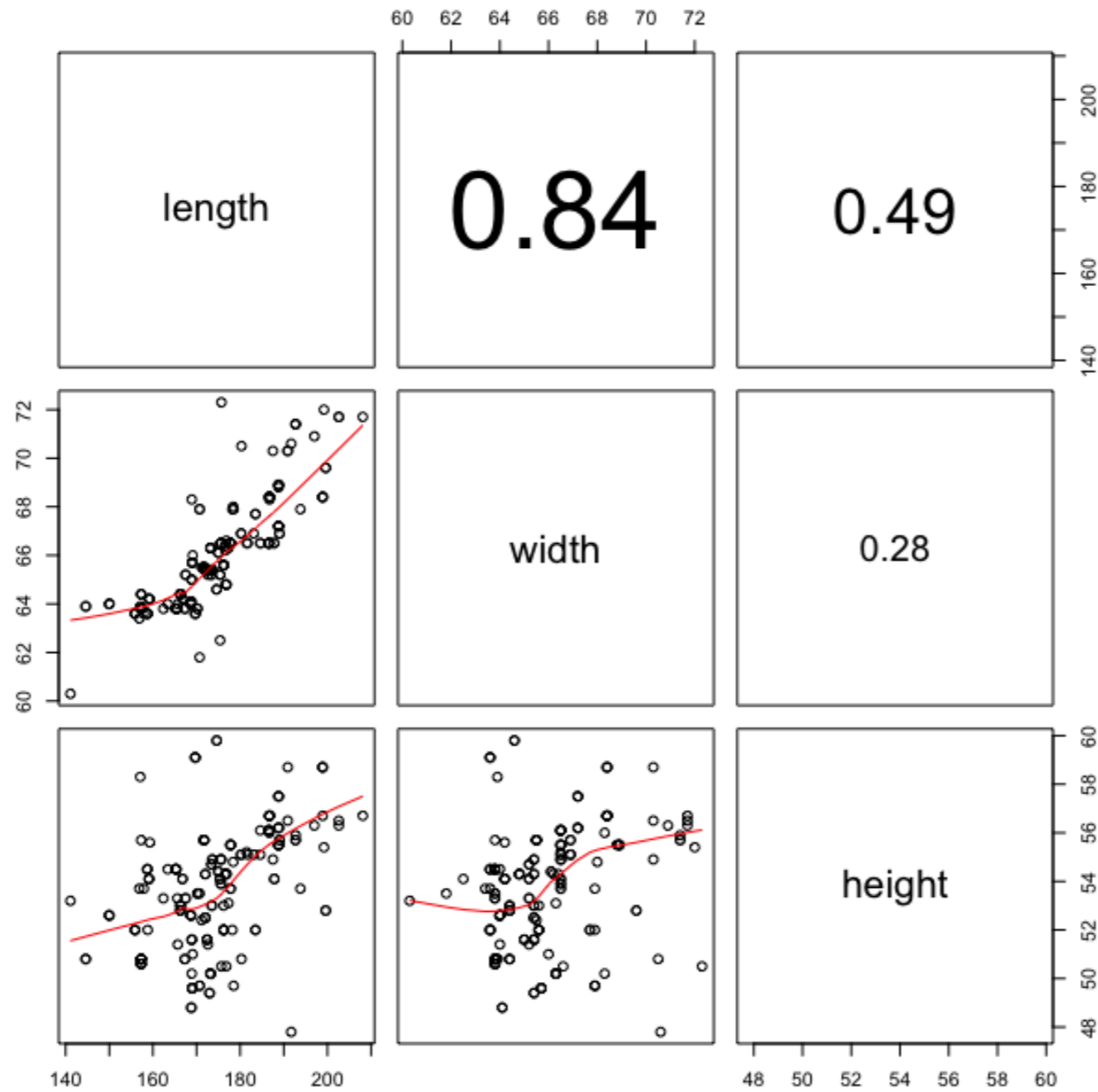
Checking concavity

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R

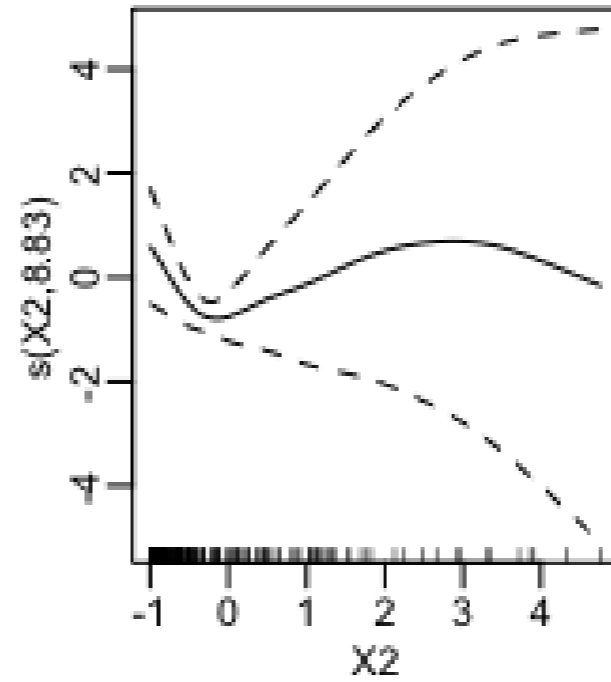
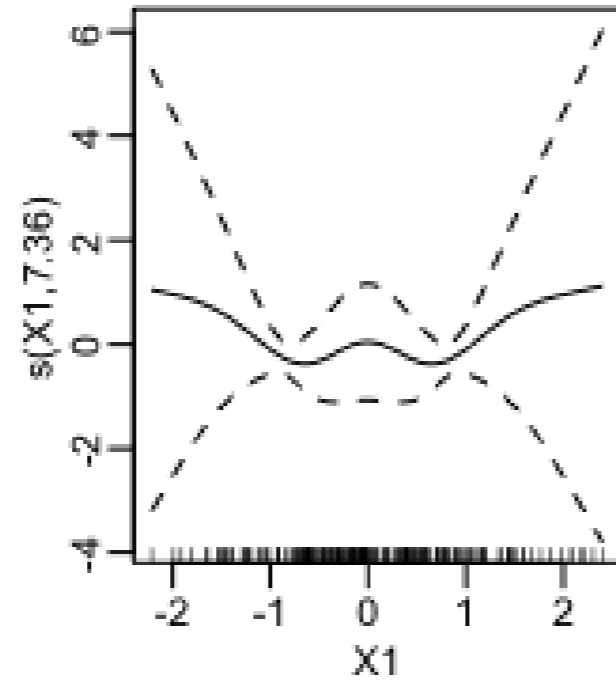
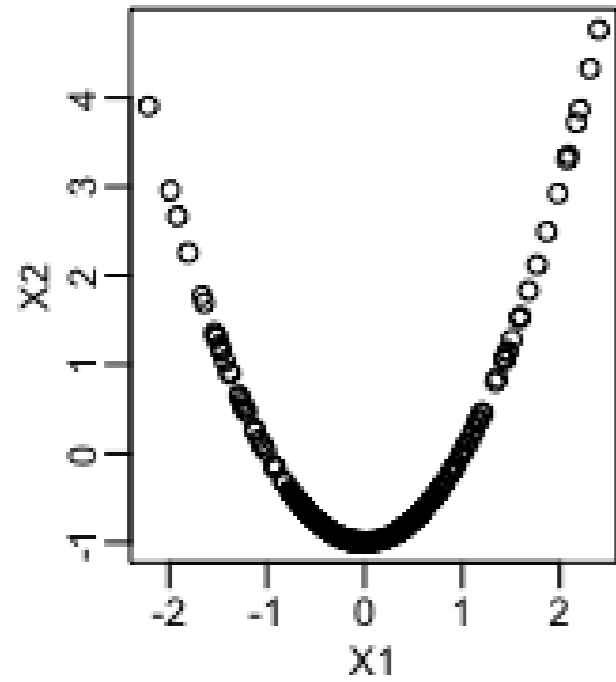


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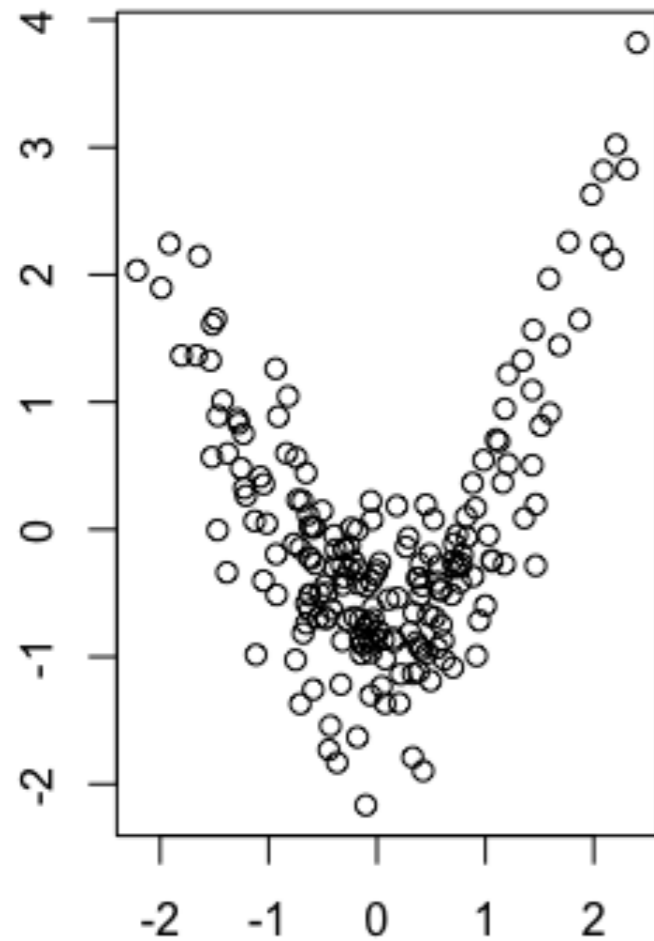
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Concurvity



The `concurvity()` function



```
concurvity(m1, full = TRUE)
```

	para	s(X1)	s(X2)
worst	0	0.84	0.84
observed	0	0.22	0.57
estimate	0	0.28	0.60

Pairwise concurvities

```
concurvity(model, full = FALSE)
```

```
$worst
```

	para	s(X1)	s(X2)
para	1	0.00	0.00
s(X1)	0	1.00	0.84
s(X2)	0	0.84	1.00

```
$observed
```

	para	s(X1)	s(X2)
para	1	0.00	0.00
s(X1)	0	1.00	0.57
s(X2)	0	0.22	1.00

```
$estimate
```

	para	s(X1)	s(X2)
para	1	0.00	0.0
s(X1)	0	1.00	0.6
s(X2)	0	0.28	1.0

Let's practice!

NONLINEAR MODELING WITH GENERALIZED ADDITIVE MODELS (GAMS) IN R