

Models for each category

INTERMEDIATE REGRESSION IN R



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4 categories

```
unique(fish$species)
```

```
"Bream" "Roach" "Perch" "Pike"
```

Splitting the dataset

The smart way

- **base-R**: `split()` + `lapply()`
- **dplyr**: `nest_by()` + `mutate()`

The simple way

```
bream <- fish %>%  
  filter(species == "Bream")  
perch <- fish %>%  
  filter(species == "Perch")  
pike <- fish %>%  
  filter(species == "Pike")  
roach <- fish %>%  
  filter(species == "Roach")
```

4 models

```
mdl_bream <- lm(mass_g ~ length_cm, data = bream)
```

```
Call:
lm(formula = mass_g ~ length_cm, data = bream)

Coefficients:
(Intercept)    length_cm
   -1035.35         54.55
```

```
mdl_perch <- lm(mass_g ~ length_cm, data = perch)
```

```
Call:
lm(formula = mass_g ~ length_cm, data = perch)

Coefficients:
(Intercept)    length_cm
   -619.18         38.91
```

```
mdl_pike <- lm(mass_g ~ length_cm, data = pike)
```

```
Call:
lm(formula = mass_g ~ length_cm, data = pike)

Coefficients:
(Intercept)    length_cm
  -1540.82         53.19
```

```
mdl_roach <- lm(mass_g ~ length_cm, data = roach)
```

```
Call:
lm(formula = mass_g ~ length_cm, data = roach)

Coefficients:
(Intercept)    length_cm
   -329.38         23.32
```

Explanatory data

```
explanatory_data <- tibble(  
  length_cm = seq(5, 60, 5)  
)
```

Making predictions

```
prediction_data_bream <- explanatory_data %>%
  mutate(
    mass_g = predict mdl_bream, explanatory_data),
    species = "Bream"
  )
```

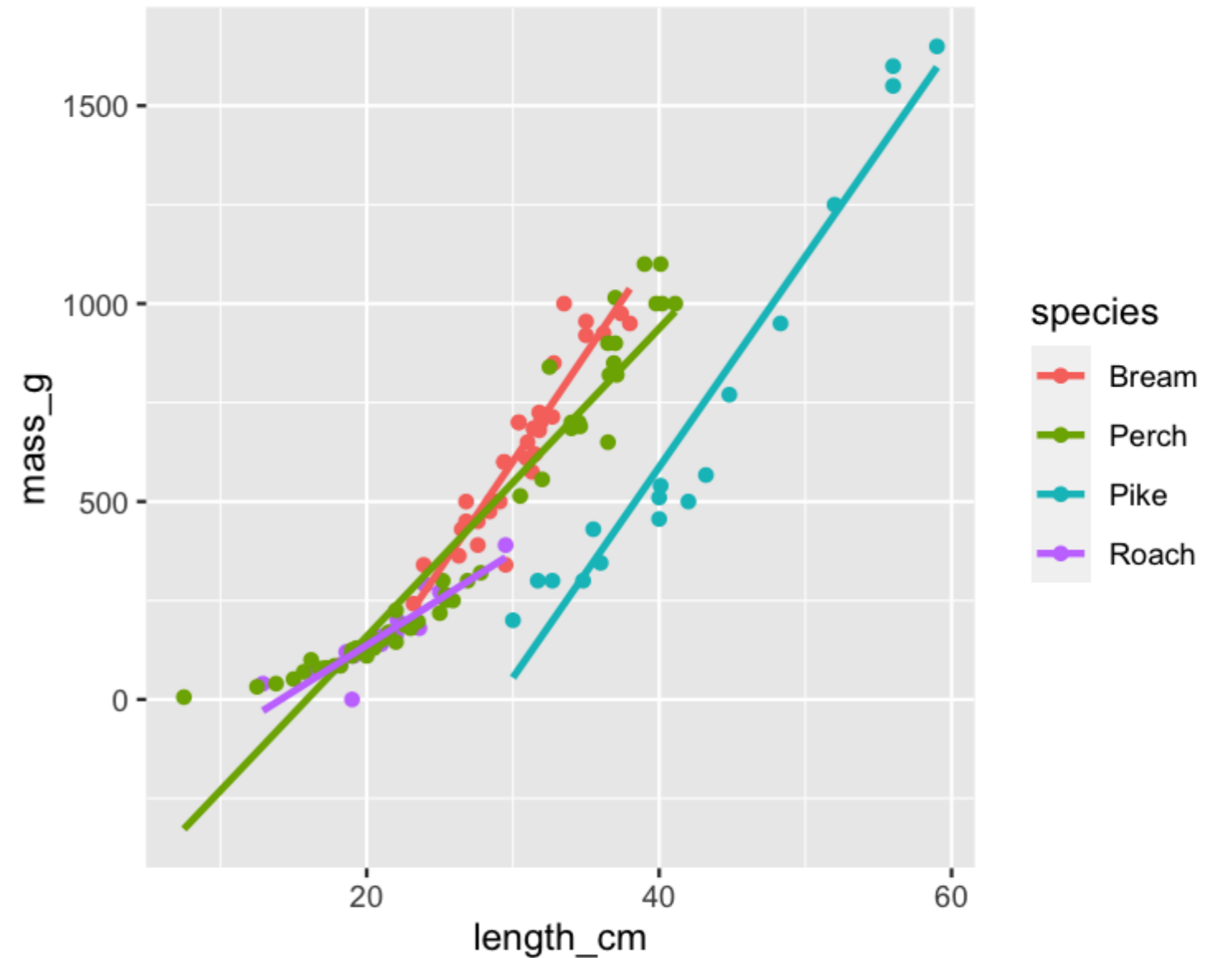
```
prediction_data_pike <- explanatory_data %>%
  mutate(
    mass_g = predict mdl_perch, explanatory_data),
    species = "Perch"
  )
```

```
prediction_data_perch <- explanatory_data %>%
  mutate(
    mass_g = predict mdl_pike, explanatory_data),
    species = "Pike"
  )
```

```
prediction_data_roach <- explanatory_data %>%
  mutate(
    mass_g = predict mdl_roach, explanatory_data),
    species = "Roach"
  )
```

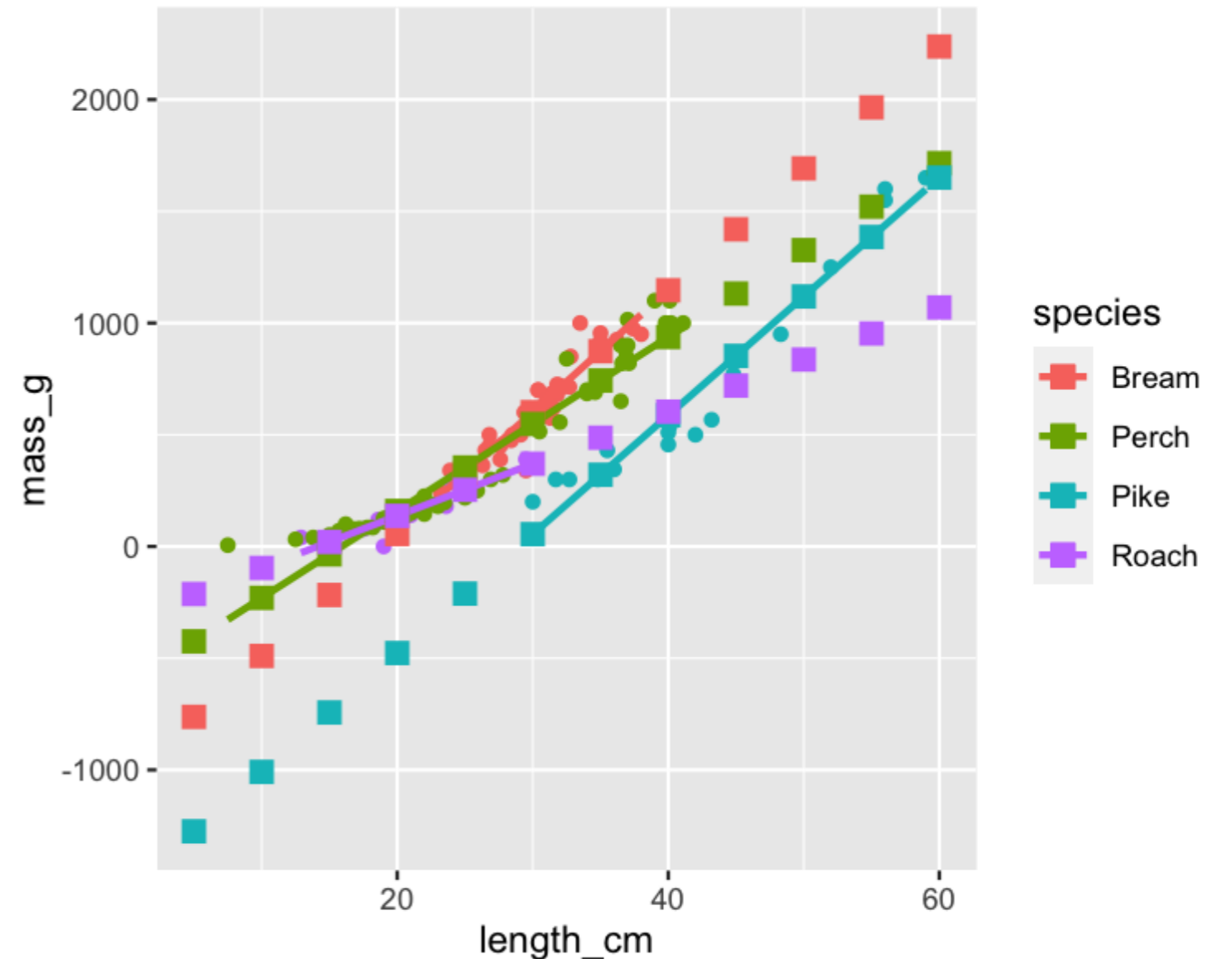
Visualizing predictions

```
ggplot(fish, aes(length_cm, mass_g, color = species)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE)
```



Adding in your predictions

```
ggplot(fish,aes(length_cm, mass_g, color = species)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE) +  
  geom_point(data = prediction_data_bream, size = 3, shape = 15) +  
  geom_point(data = prediction_data_perch, size = 3, shape = 15) +  
  geom_point(data = prediction_data_pike, size = 3, shape = 15) +  
  geom_point(data = prediction_data_roach, size = 3, shape = 15)
```



Coefficient of determination

```
mdl_fish <- lm(mass_g ~ length_cm + species, data = fish)
```

```
mdl_fish %>%  
  glance() %>%  
  pull(adj.r.squared)
```

0.917

```
mdl_bream %>% glance() %>% pull(adj.r.squared)
```

0.874

```
mdl_perch %>% glance() %>% pull(adj.r.squared)
```

0.917

```
mdl_pike %>% glance() %>% pull(adj.r.squared)
```

0.941

```
mdl_roach %>% glance() %>% pull(adj.r.squared)
```

0.815

Residual standard error

```
mdl_fish %>%  
  glance() %>%  
  pull(sigma)
```

103

```
mdl_bream %>% glance() %>% pull(sigma)
```

74.2

```
mdl_perch %>% glance() %>% pull(sigma)
```

100

```
mdl_pike %>% glance() %>% pull(sigma)
```

120

```
mdl_roach %>% glance() %>% pull(sigma)
```

38.2

Let's practice!

INTERMEDIATE REGRESSION IN R

One model with an interaction

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What is an interaction?

In the fish dataset

The effect of length on the expected mass is different for different species.

More generally

The effect of one explanatory variable on the expected response changes depending on the value of another explanatory variable.

Specifying interactions

No interactions

```
response ~ explntry1 + explntry2
```

With interactions (implicit)

```
response_var ~ explntry1 * explntry2
```

With interactions (explicit)

```
response ~ explntry1 + explntry2 + explntry1:explntry2
```

No interactions

```
mass_g ~ length_cm + species
```

With interactions (implicit)

```
mass_g ~ length_cm * species
```

With interactions (explicit)

```
mass_g ~ length_cm + species + length_cm:species
```

Running the model

```
lm(mass_g ~ length_cm * species, data = fish)
```

Call:

```
lm(formula = mass_g ~ length_cm * species, data = fish)
```

Coefficients:

(Intercept)	length_cm	speciesPerch	speciesPike
-1035.348	54.550	416.172	-505.477
speciesRoach	length_cm:speciesPerch	length_cm:speciesPike	length_cm:speciesRoach
705.971	-15.639	-1.355	-31.231

Easier to understand coefficients

```
mdl_inter <- lm(mass_g ~ species + species:length_cm + 0, data = fish)
```

Call:

```
lm(formula = mass_g ~ species + species:length_cm + 0, data = fish)
```

Coefficients:

speciesBream	speciesPerch	speciesPike	speciesRoach
-1035.35	-619.18	-1540.82	-329.38
speciesBream:length_cm	speciesPerch:length_cm	speciesPike:length_cm	speciesRoach:length_cm
54.55	38.91	53.19	23.32

Familiar numbers

```
speciesBream      speciesPerch      speciesPike      speciesRoach
-1035.35          -619.18           -1540.82         -329.38
speciesBream:length_cm speciesPerch:length_cm speciesPike:length_cm speciesRoach:length_cm
54.55            38.91             53.19            23.32
```

```
coefficients mdl_bream)
```

```
(Intercept) length_cm
-1035.34757  54.54998
```

Let's practice!

INTERMEDIATE REGRESSION IN R

Making predictions with interactions

INTERMEDIATE REGRESSION IN R



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The model with the interaction

```
mdl_mass_vs_both_inter <- lm(mass_g ~ species + species:length_cm + 0, data = fish)
```

Call:

```
lm(formula = mass_g ~ species + species:length_cm + 0, data = fish)
```

Coefficients:

speciesBream	speciesPerch	speciesPike	speciesRoach
-1035.35	-619.18	-1540.82	-329.38
speciesBream:length_cm	speciesPerch:length_cm	speciesPike:length_cm	speciesRoach:length_cm
54.55	38.91	53.19	23.32

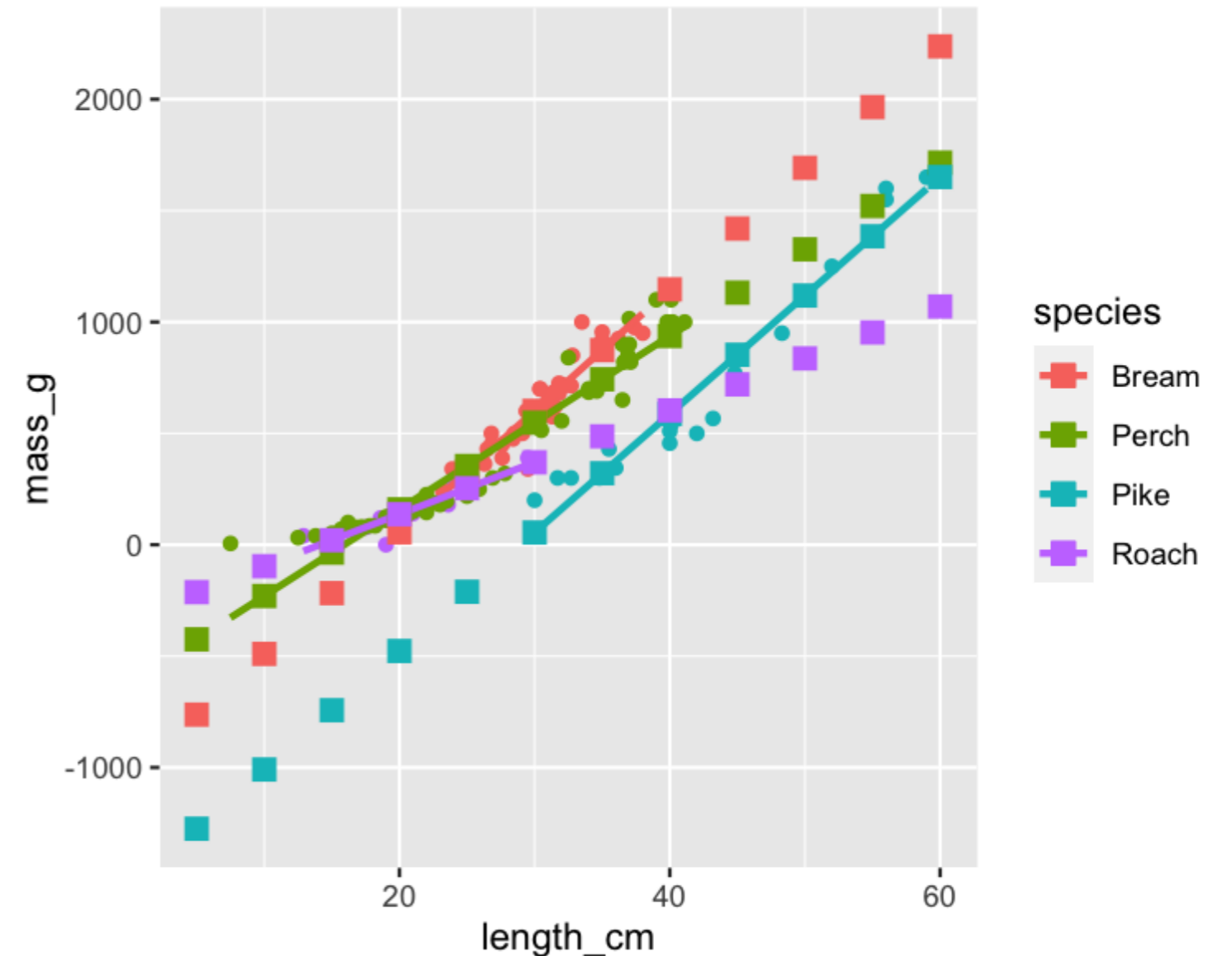
The prediction flow, again

```
library(dplyr)
library(tidyr)
explanatory_data <- expand_grid(
  length_cm = seq(5, 60, 5),
  species = unique(fish$species)
)

prediction_data <- explanatory_data %>%
  mutate(mass_g = predict mdl_mass_vs_both_inter, explanatory_data))
```

Visualizing the predictions

```
ggplot(fish, aes(length_cm, mass_g, color = species)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE) +  
  geom_point(data = prediction_data, size = 3, shape = 15)
```



Manually calculating the predictions

```
coeffs <- coefficients mdl_mass_vs_both_inter)
```

```
      speciesBream      speciesPerch      speciesPike      speciesRoach  
      -1035.34757      -619.17511      -1540.82427      -329.37621  
speciesBream:length_cm speciesPerch:length_cm speciesPike:length_cm speciesRoach:length_cm  
      54.54998      38.91147      53.19487      23.31926
```

```
intercept_bream <- coeffs[1]  
intercept_perch <- coeffs[2]  
intercept_pike <- coeffs[3]  
intercept_roach <- coeffs[4]
```

```
slope_bream <- coeffs[5]  
slope_perch <- coeffs[6]  
slope_pike <- coeffs[7]  
slope_roach <- coeffs[8]
```

Manually calculating the predictions

```
explanatory_data %>%  
  mutate(  
    mass_g = case_when(  
  
    )  
  )  
)
```


Manually calculating the predictions

```
explanatory_data %>%  
  mutate(  
    mass_g = case_when(  
      species == "Bream" ~  
  
    )  
  )  
)
```

Manually calculating the predictions

```
explanatory_data %>%  
  mutate(  
    mass_g = case_when(  
      species == "Bream" ~ intercept_bream + slope_bream * length_cm  
    )  
  )  
)
```

Manually calculating the predictions

```
explanatory_data %>%
  mutate(
    mass_g = case_when(
      species == "Bream" ~ intercept_bream + slope_bream * length_cm,
      species == "Perch" ~ intercept_perch + slope_perch * length_cm,
      species == "Pike" ~ intercept_pike + slope_pike * length_cm,
      species == "Roach" ~ intercept_roach + slope_roach * length_cm
    )
  )
```

Let's practice!

INTERMEDIATE REGRESSION IN R

Simpson's Paradox

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A most ingenious paradox!

Simpson's Paradox occurs when the trend of a model on the whole dataset is very different from the trends shown by models on subsets of the dataset.

trend = slope coefficient

Synthetic Simpson data

x	y	group
62.24344	70.60840	D
52.33499	14.70577	B
56.36795	46.39554	C
66.80395	66.17487	D
66.53605	89.24658	E
62.38129	91.45260	E

- 5 groups of data, labeled "A" to "E"

¹ https://www.rdocumentation.org/packages/datasauRus/topics/simpsons_paradox

Linear regressions

Whole dataset

```
mdl_whole <- lm(  
  y ~ x,  
  data = simpsons_paradox  
)  
coefficients(mdl_whole)
```

```
(Intercept)      x  
-38.554         1.751
```

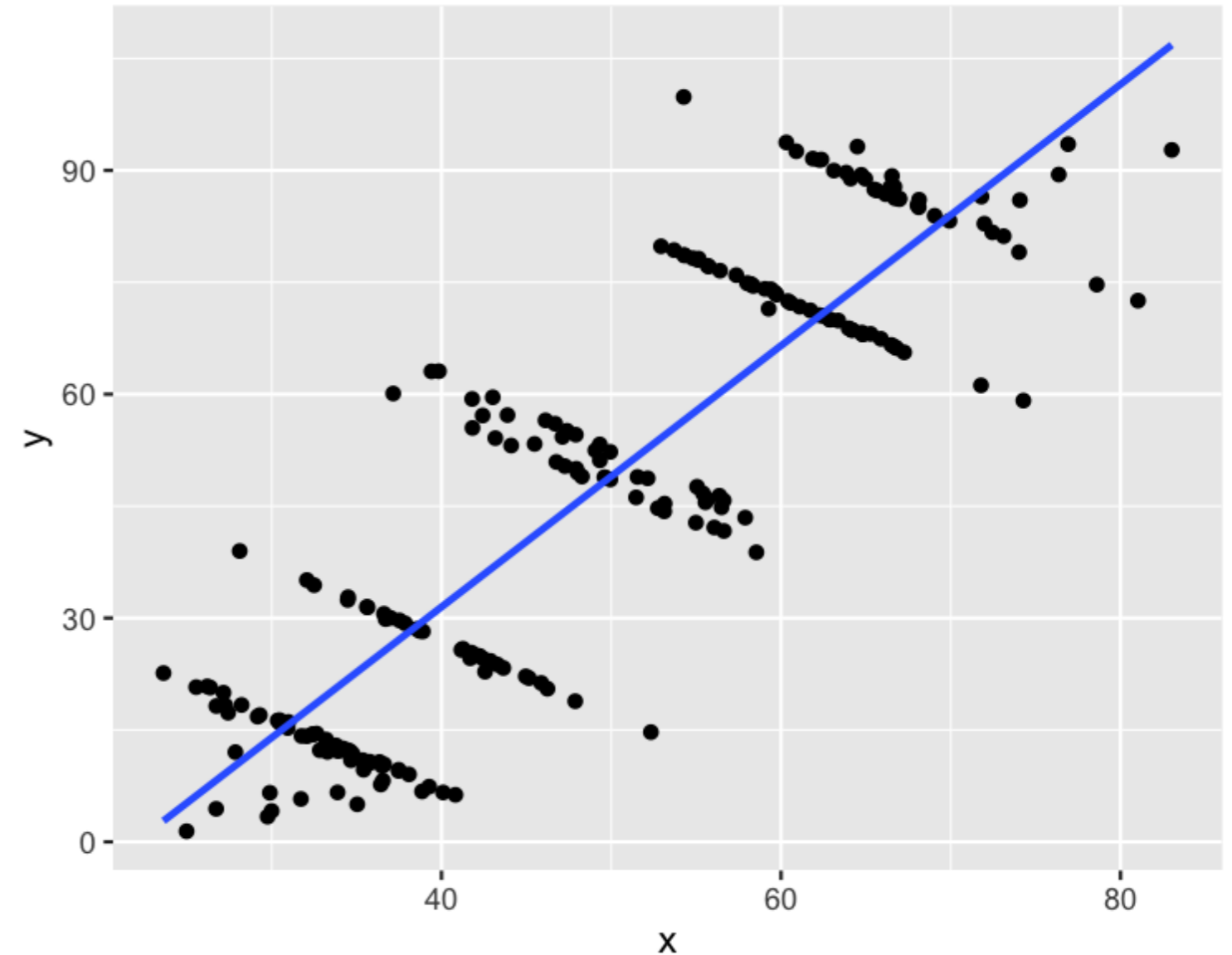
By group

```
mdl_by_group <- lm(  
  y ~ group + group:x + 0,  
  data = simpsons_paradox  
)  
coefficients(mdl_by_group)
```

```
groupA  groupB  groupC  groupD  groupE  
32.5051  67.3886  99.6333  132.3932  123.8242  
groupA:x  groupB:x  groupC:x  groupD:x  groupE:x  
-0.6266  -1.0105  -0.9940  -0.9908  -0.5364
```

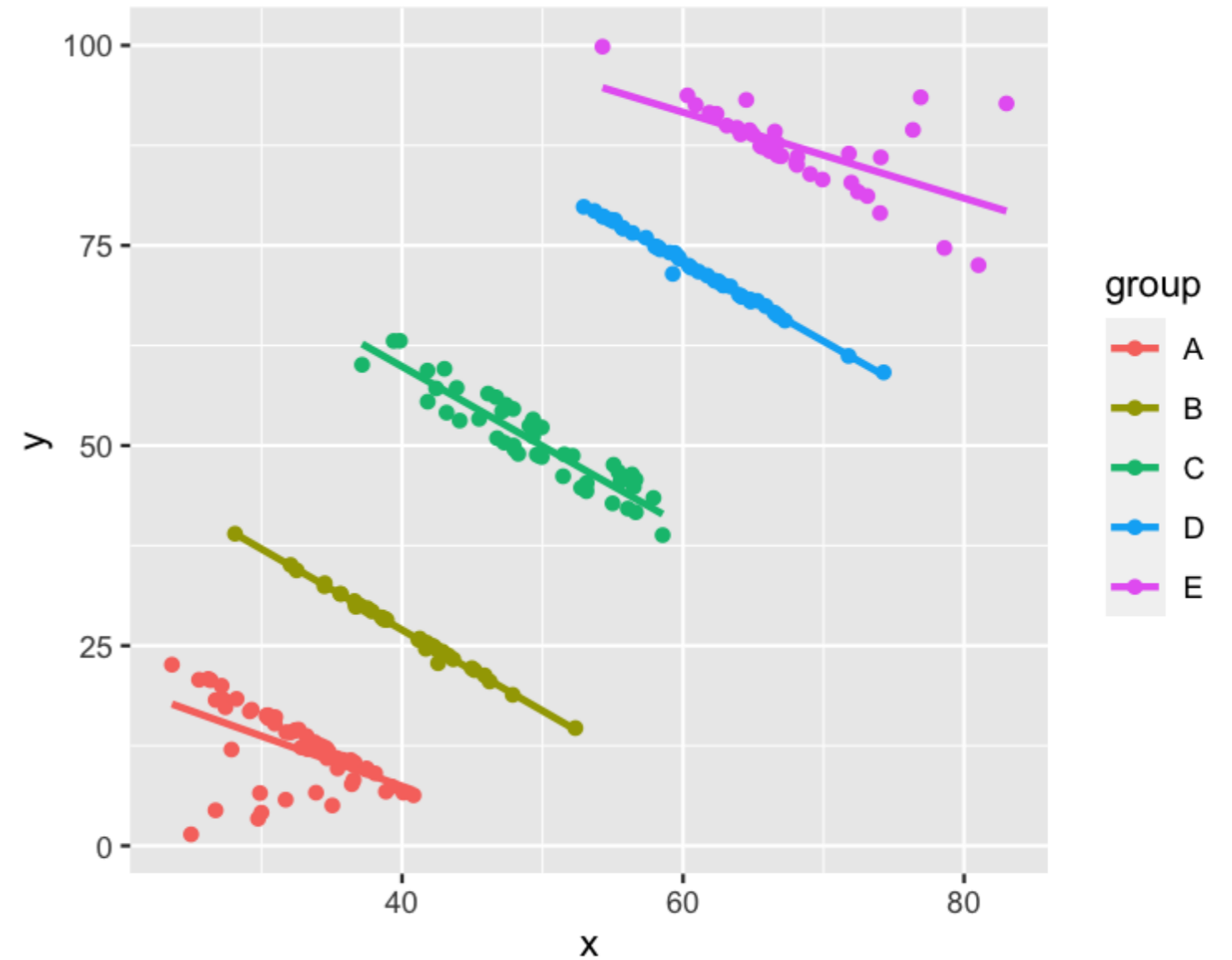

Plotting the whole dataset

```
ggplot(simpsons_paradox, aes(x, y)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE)
```



Plotting by group

```
ggplot(simpsons_paradox, aes(x, y, color = group)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE)
```



Reconciling the difference

Good advice

If possible, try to plot the dataset.

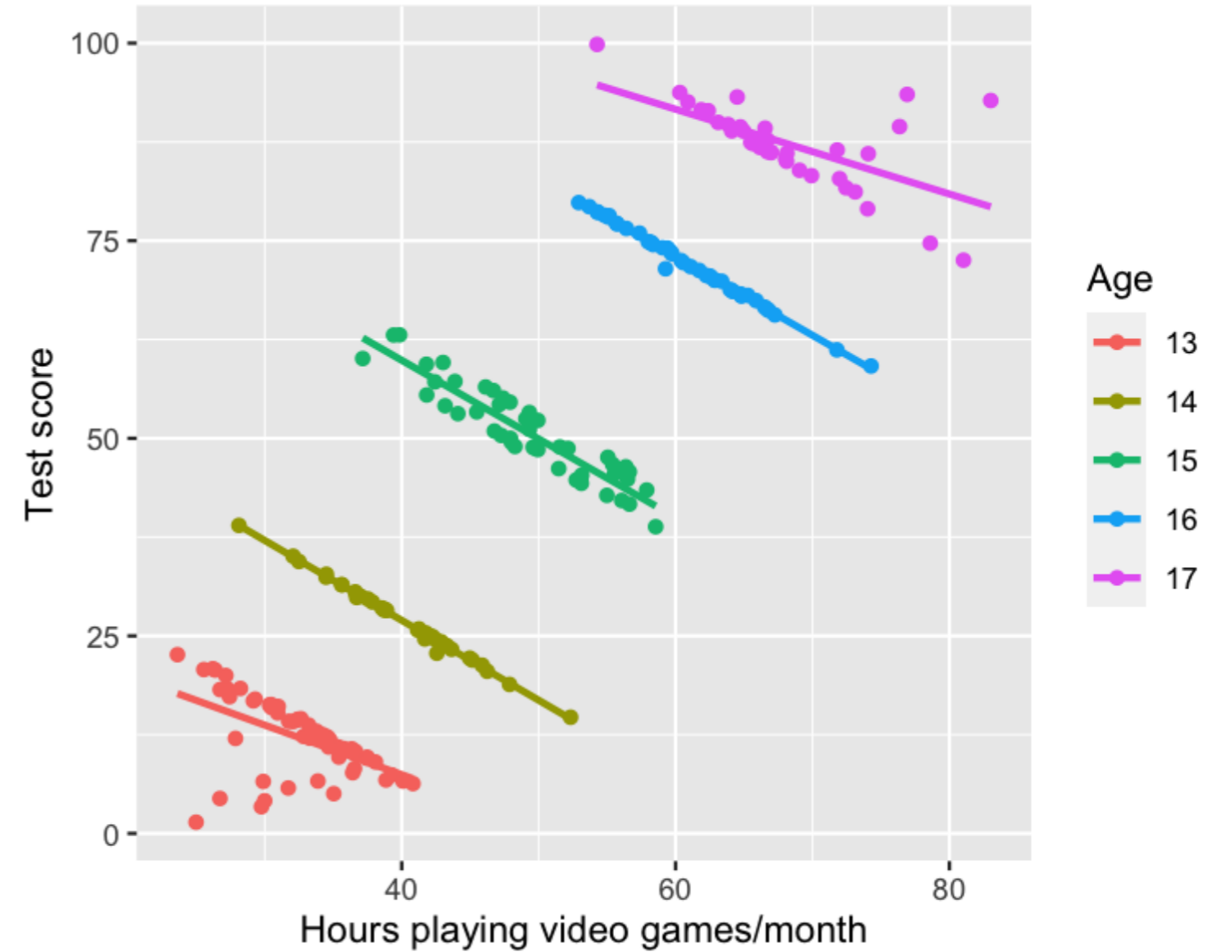
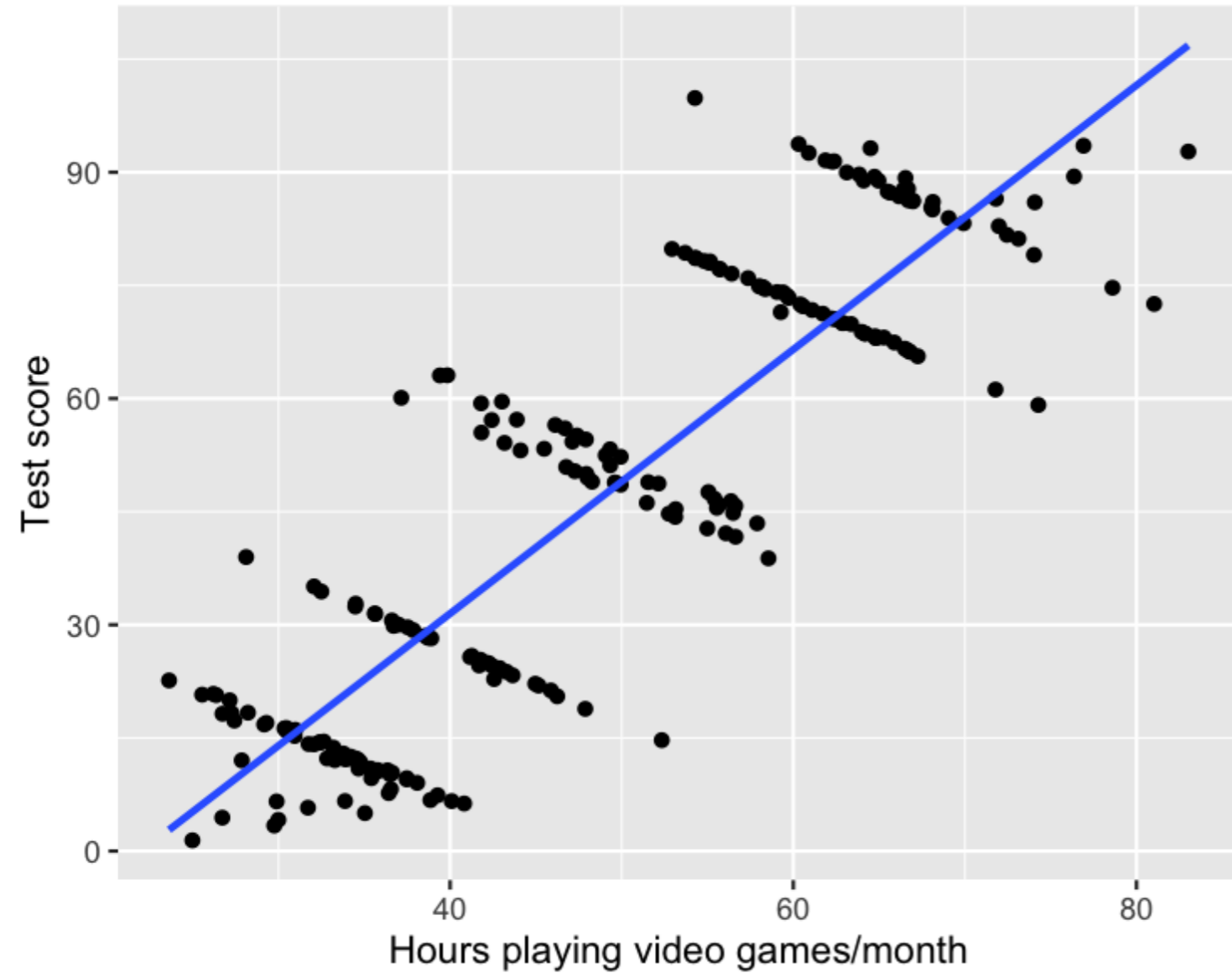
Common advice

You can't choose the best model in general—it depends on the dataset and the question you are trying to answer.

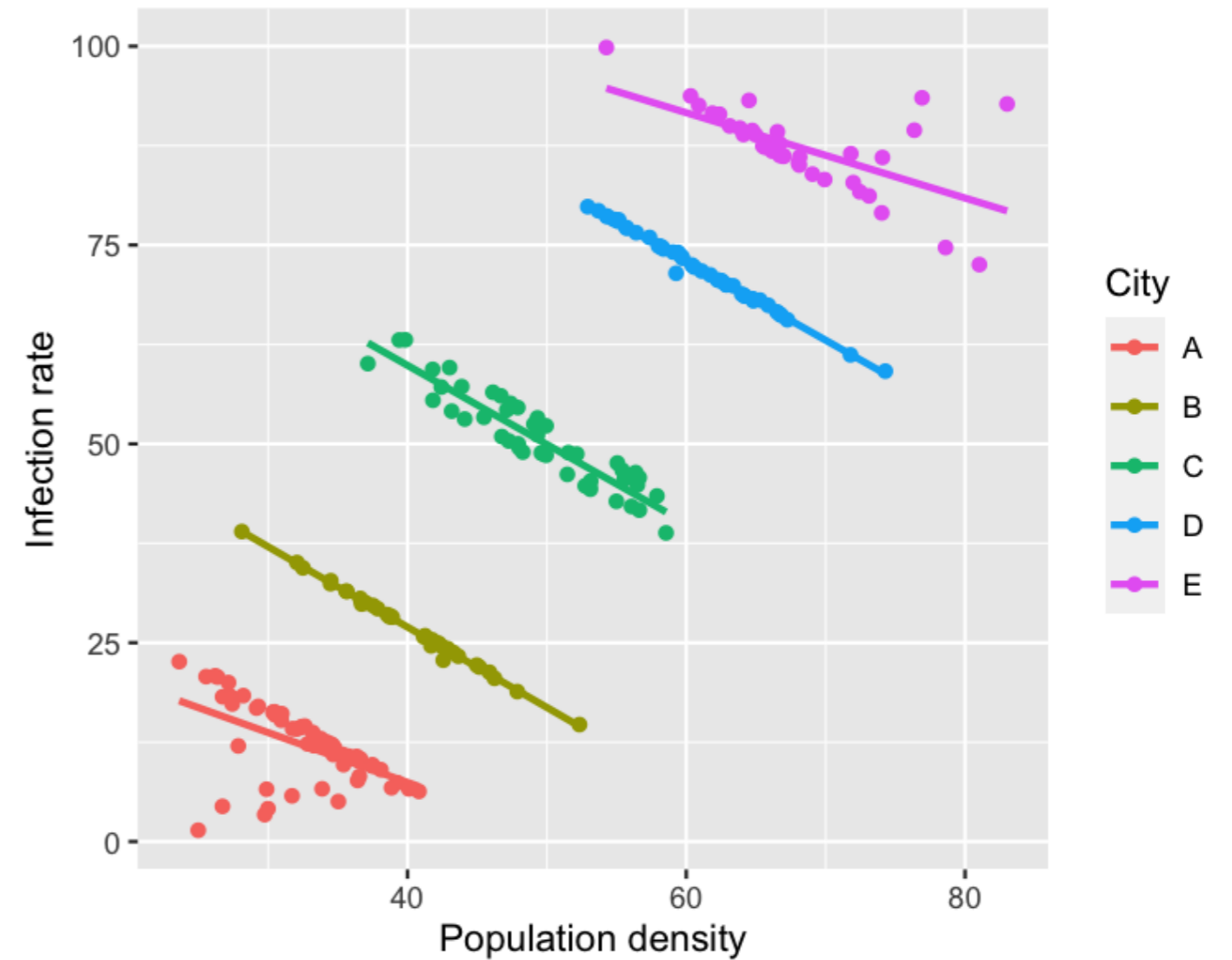
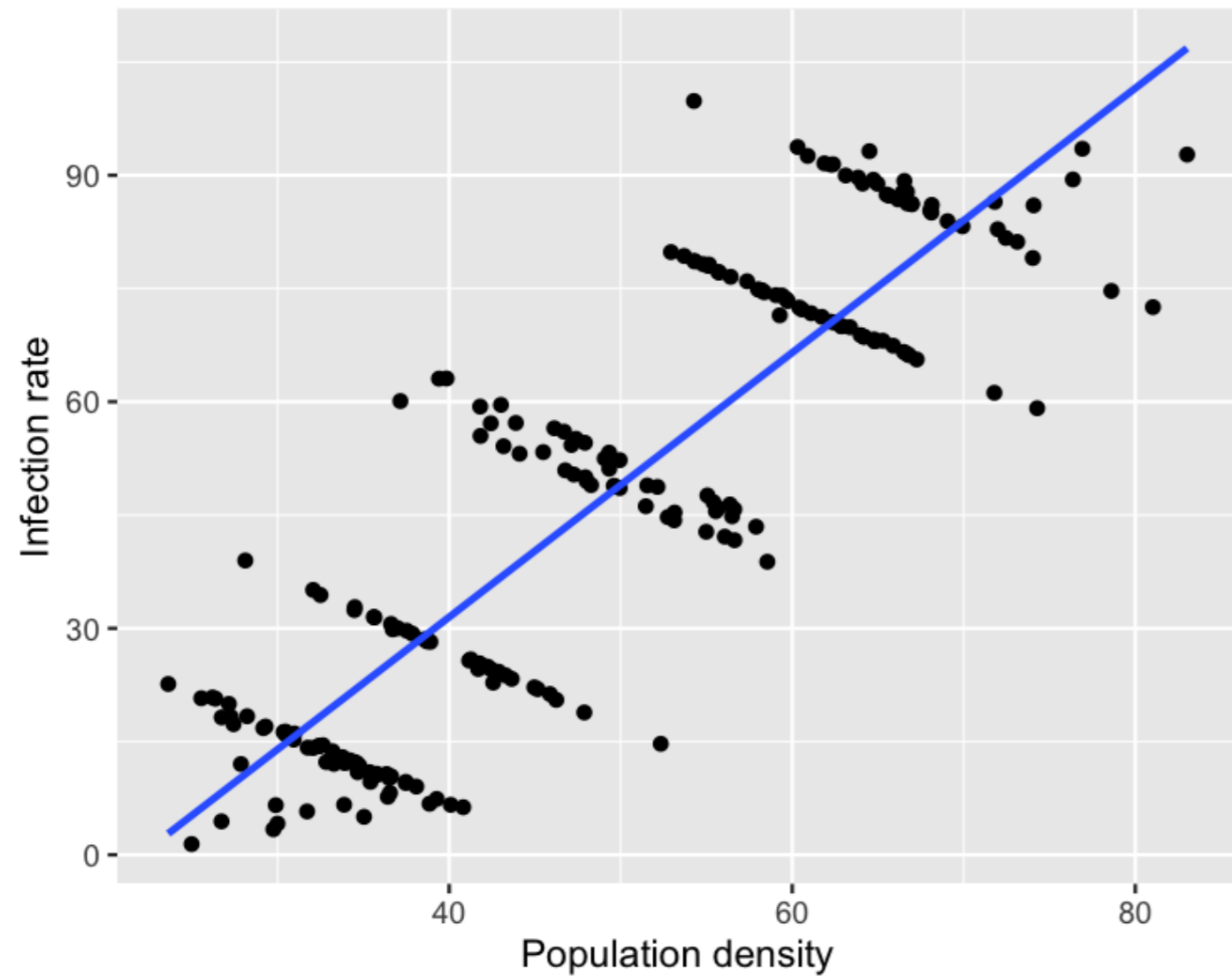
More good advice

Articulate a question before you start modeling.

Test score example



Infectious disease example



¹ <https://stats.stackexchange.com/questions/478463/examples-of-simpsons-paradox-being-resolved-by-choosing-the-aggregate-data>

Reconciling the difference, again

- Usually (but not always) the grouped model contains more insight.
- Are you missing explanatory variables?
- Context is important.

Simpson's paradox in real datasets

- The paradox is usually less obvious.
- You may see a zero slope rather than a complete change in direction.
- It may not appear in every group.

Let's practice!

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