

# Model Specification

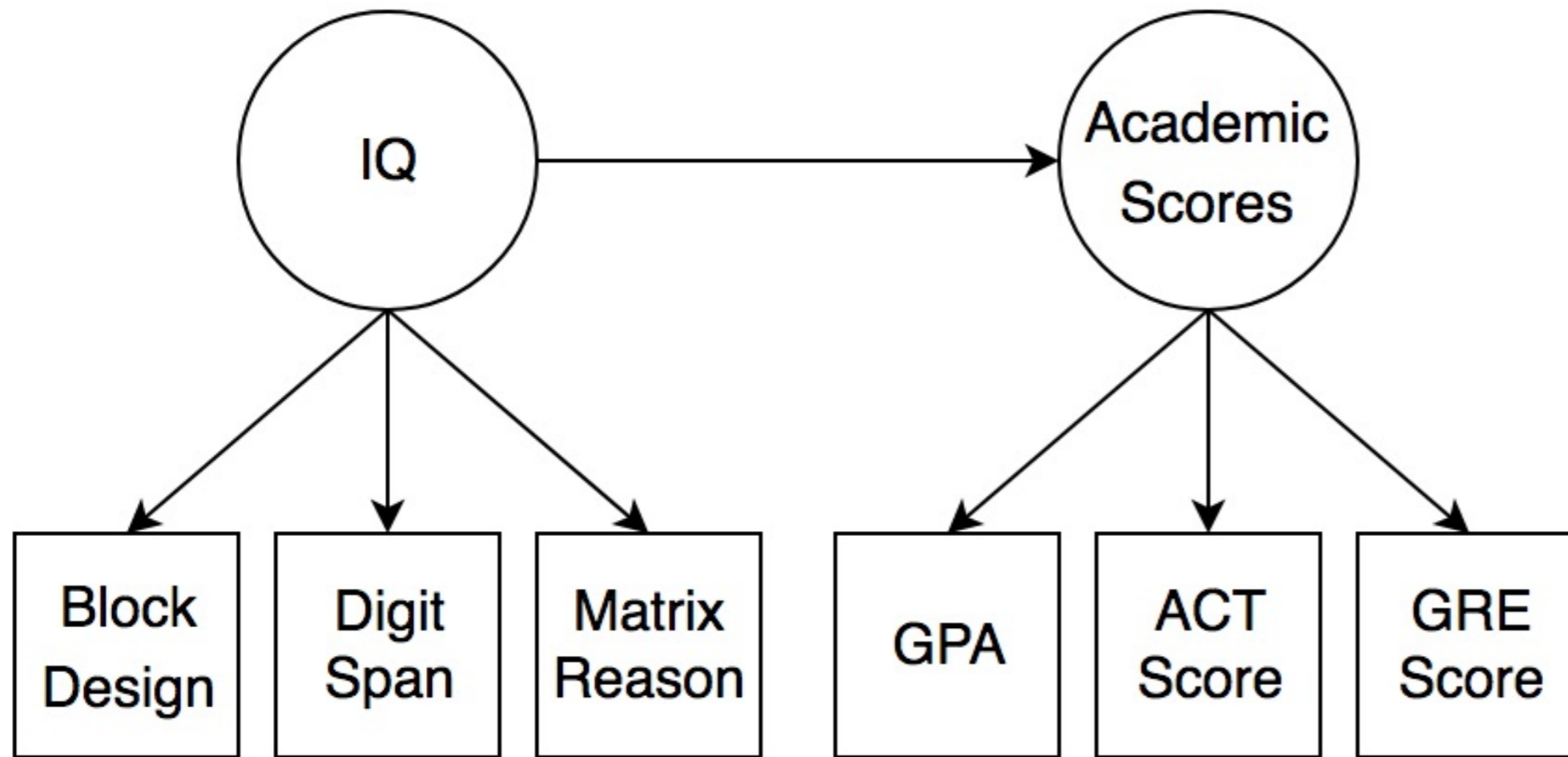
STRUCTURAL EQUATION MODELING WITH LAVAAN IN R



**Erin Buchanan**  
Professor

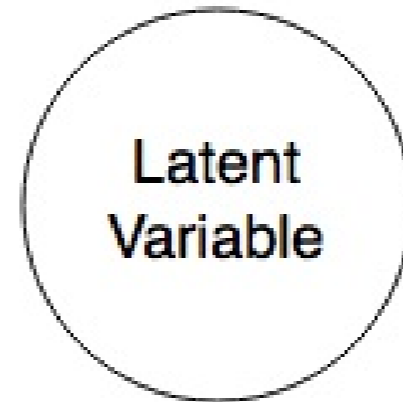
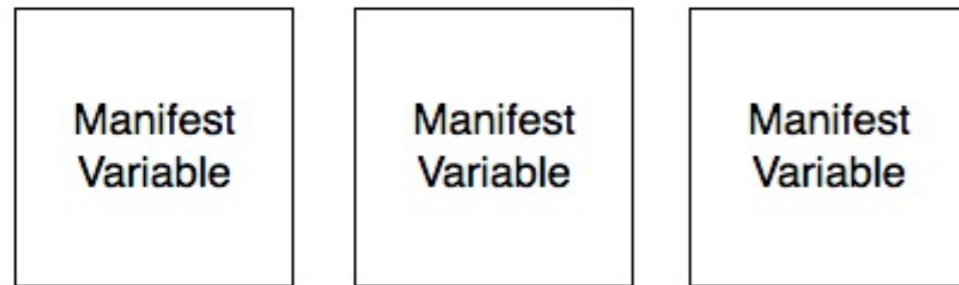
# SEM Goals

- Explore the relationship between variables
- Confirm the structure of a developed model

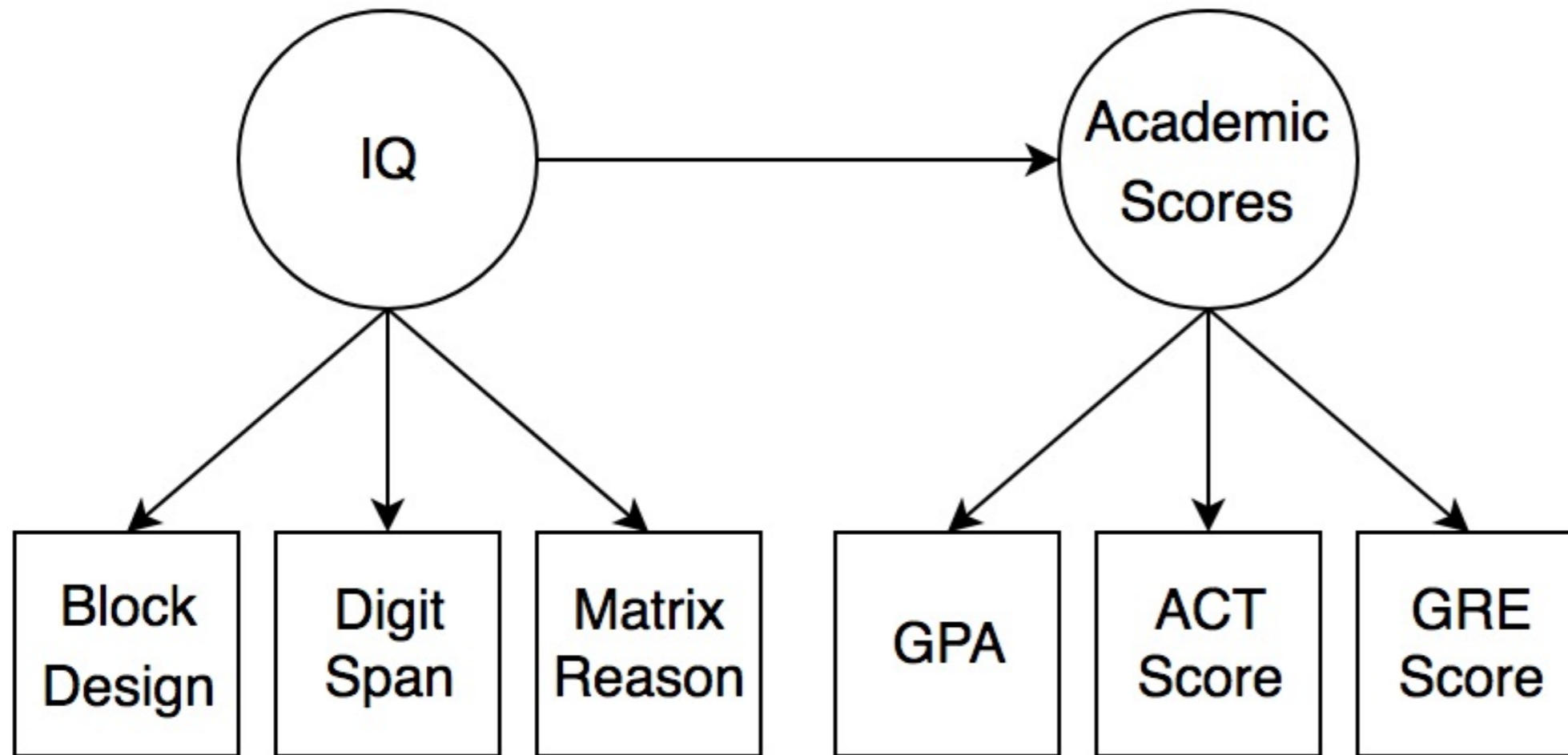


# Variables

- Manifest variables:
  - Real numbers in your dataset
  - Represented by squares
- Latent variables:
  - Phenomenon measured by manifest variables
  - Represented by circles



# Example Model



# Set Up Your Model

```
library(lavaan)  
data(HolzingerSwineford1939)
```

```
head(HolzingerSwineford1939[7:15])
```

```
      x1    x2    x3      x4    x5      x6      x7    x8      x9  
1 3.333333 7.75 0.375 2.333333 5.75 1.2857143 3.391304 5.75 6.361111  
2 5.333333 5.25 2.125 1.666667 3.00 1.2857143 3.782609 6.25 7.916667  
3 4.500000 5.25 1.875 1.000000 1.75 0.4285714 3.260870 3.90 4.416667  
4 5.333333 7.75 3.000 2.666667 4.50 2.4285714 3.000000 5.30 4.861111  
5 4.833333 4.75 0.875 2.666667 4.00 2.5714286 3.695652 6.30 5.916667  
6 5.333333 5.00 2.250 1.000000 3.00 0.8571429 4.347826 6.65 7.500000
```

# Set Up Your Model (2)

```
#an example
```

```
model <- 'latent_variable =~ manifest_variable1 + ...'
```

```
#our model
```

```
visual.model <- 'visual =~ x1 + x2 + x3 + x7 + x8 + x9'
```

# Let's practice!

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# Model Analysis

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# Model Terms

- Degrees of Freedom (df)
  - Determined by the number of manifest variables and estimated values
  - $df = \text{Possible Values} - \text{Estimated Values}$
  - $\text{Possible Values} = \text{Manifest Variables} * (\text{Manifest Variables} + 1) / 2$
- Identification
  - Include at least three manifest variables
  - Create models with  $df > 0$
  - Use scaling and constraints to control df

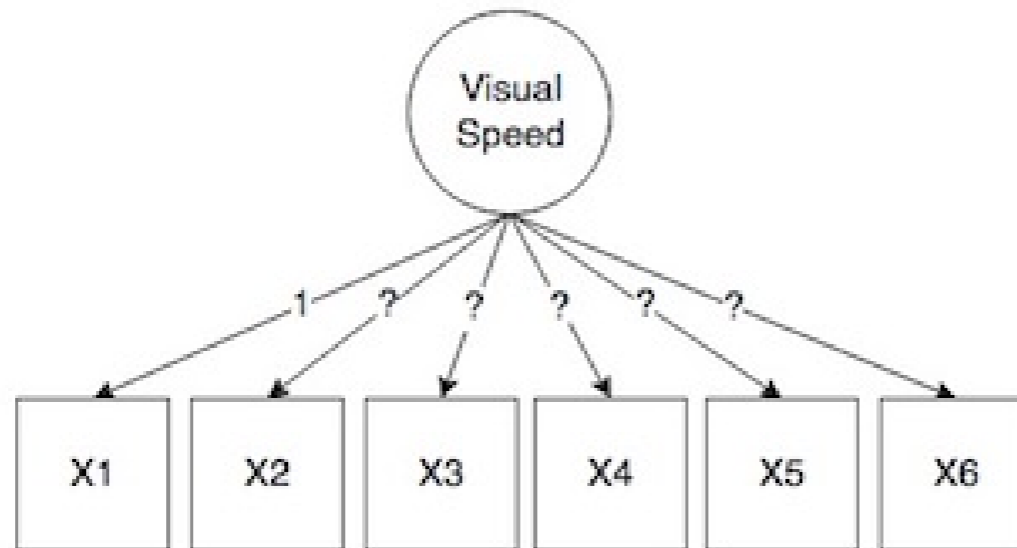
# Analyze the Model

```
#model specification
```

```
visual.model <- 'visual =~ x1 + x2 + x3 + x7 + x8 + x9'
```

```
#model analysis
```

```
visual.fit <- cfa(model = visual.model,  
                 data = HolzingerSwineford1939)
```



# Summarize the Results Overall

```
summary(visual.fit)
```

```
Lavaan (0.5-23.1097) converged normally after 27 iterations
```

```
Number of observations                301
```

```
Estimator                            ML
```

```
Minimum Function Test Statistic      106.553
```

```
Degrees of freedom                   9
```

```
P-value (Chi-square)                 0.000
```

```
Parameter Estimates:
```

# Summarize the Results Loadings

Latent Variables:

	Estimate	Std.Err	z-value	P(> z )
visual =~				
x1	1.000			
x2	0.586	0.139	4.215	0.000
x3	0.882	0.149	5.923	0.000
x7	0.728	0.137	5.320	0.000
x8	0.944	0.143	6.599	0.000
x9	1.205	0.170	7.095	0.000

# Summarize the Results Variances

Variances:

	Estimate	Std.Err	z-value	P(> z )
.x1	0.973	0.093	10.405	0.000
.x2	1.249	0.106	11.789	0.000
.x3	0.975	0.090	10.842	0.000
.x7	0.979	0.087	11.311	0.000
.x8	0.678	0.069	9.841	0.000
.x9	0.455	0.069	6.580	0.000
visual	0.386	0.092	4.201	0.000

# Let's practice!

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# Model Assessment

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# Standardized Loadings

```
summary(visual.fit, standardized = TRUE)
```

Latent Variables:

	Estimate	Std.Err	z-value	P(> z )	Std.lv	Std.all
visual =~						
x1	1.000				0.621	0.533
x2	0.586	0.139	4.215	0.000	0.364	0.310
x3	0.882	0.149	5.923	0.000	0.548	0.485
x7	0.728	0.137	5.320	0.000	0.452	0.416
x8	0.944	0.143	6.599	0.000	0.586	0.580
x9	1.205	0.170	7.095	0.000	0.748	0.742



# Fit Indices

- Model Fit - how well the data fit the specified model
  - Goodness of fit indices like the Comparative Fit Index (CFI) or the Tucker Lewis Index (TLI)
  - Badness of fit indices like Root Mean Square Error of Approximation (RMSEA) or Standardized Root Mean Square Residual (SRMR)
- **Measuring Model Fit**

# Fit Indices

```
summary(visual.fit, standardized = TRUE,  
        fit.measures = TRUE)
```

```
User model versus baseline model:
```

```
Comparative Fit Index (CFI)      0.701  
Tucker-Lewis Index (TLI)        0.502
```

```
- - -
```

```
Root Mean Square Error of Approximation:
```

```
RMSEA                            0.190
```

```
- - -
```

```
Standardized Root Mean Square Residual:
```

```
SRMR                             0.111
```

# Let's practice!

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