

# Introduction to hierarchical clustering

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**Hank Roark**

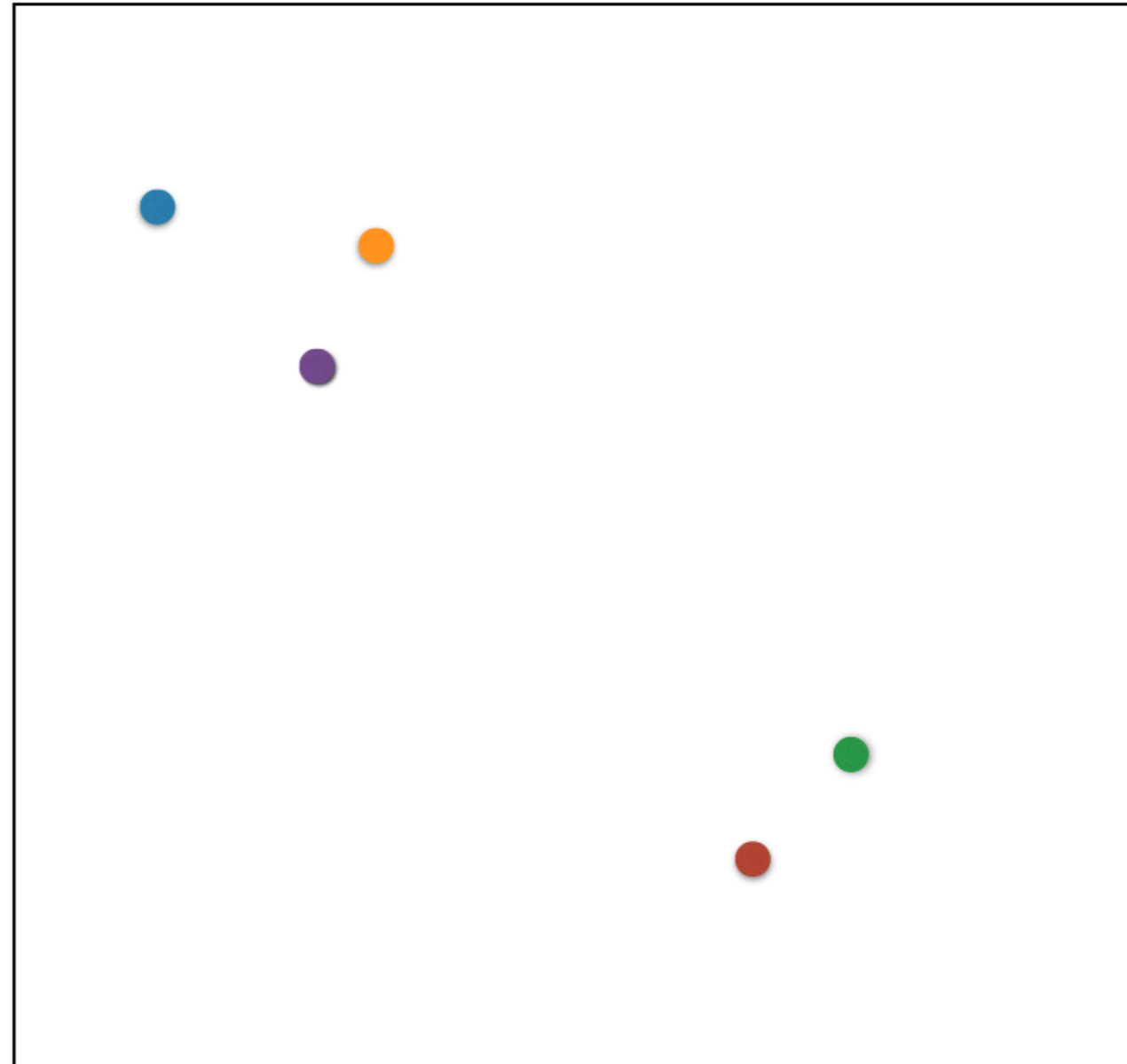
Senior Data Scientist at Boeing

# Hierarchical clustering

- Number of clusters is not known ahead of time
- Two kinds: bottom-up and top-down, this course bottom-up

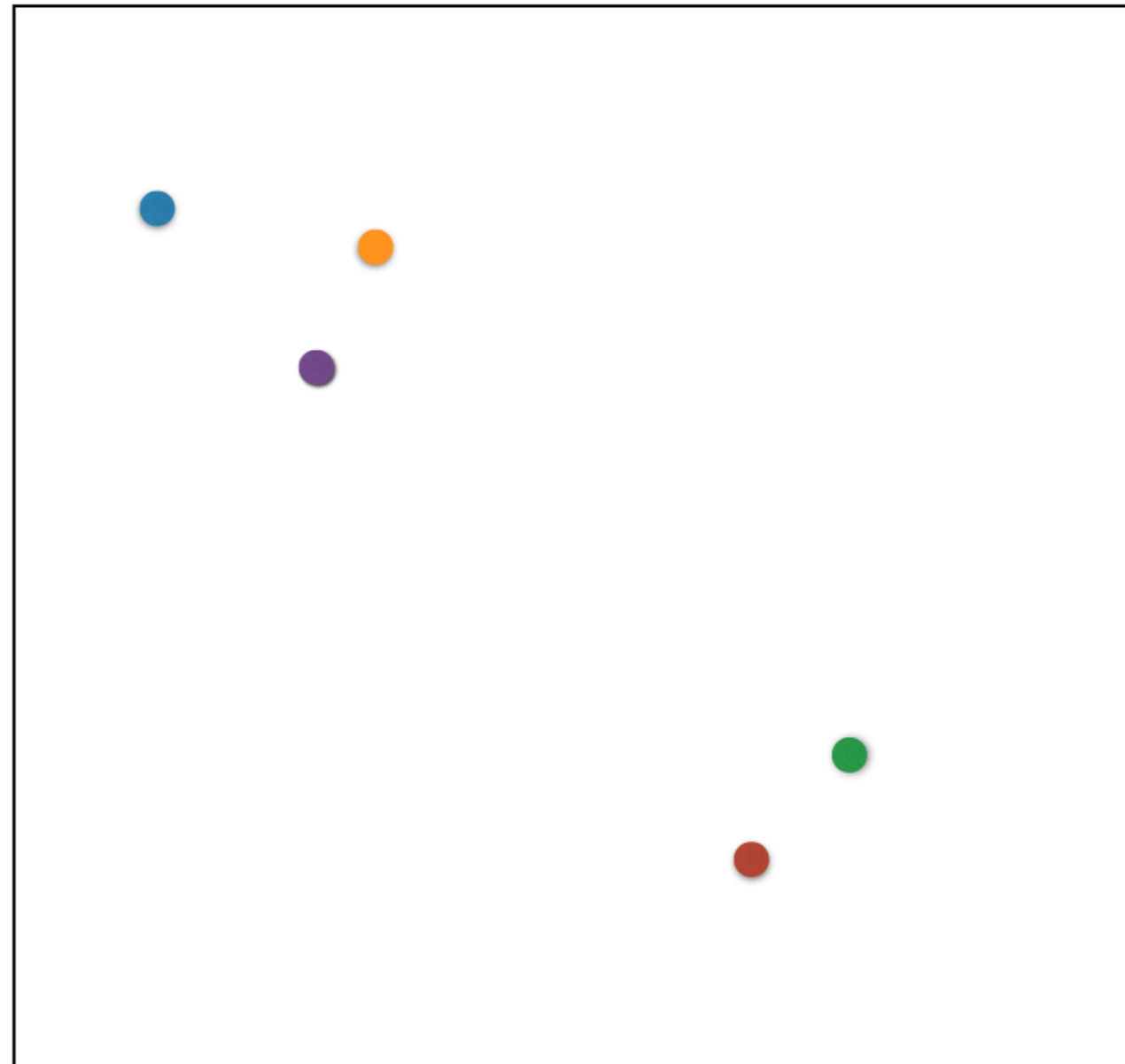
# Simple example

Simple Example



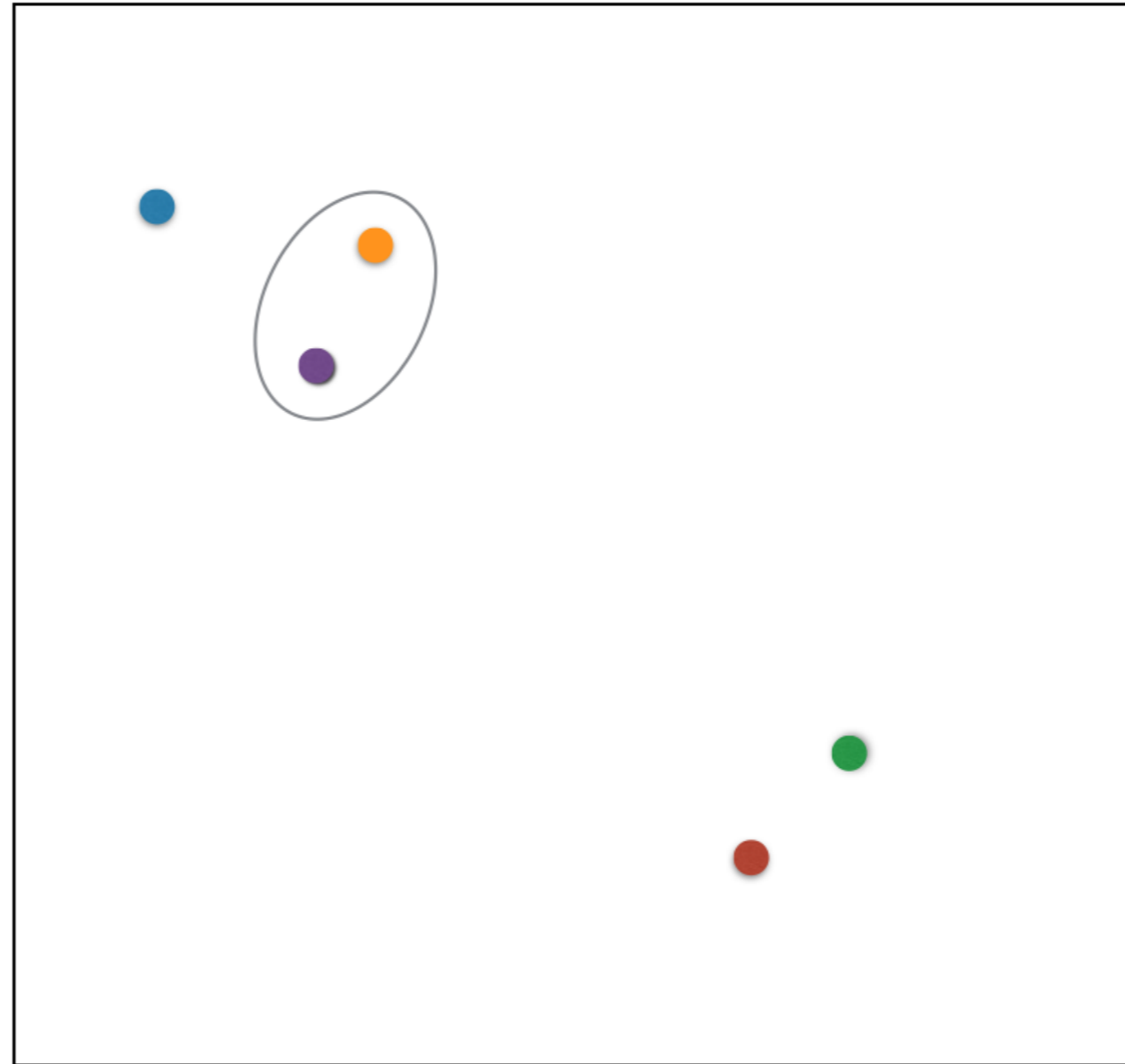
# Five clusters

5 Clusters  
Each point a cluster



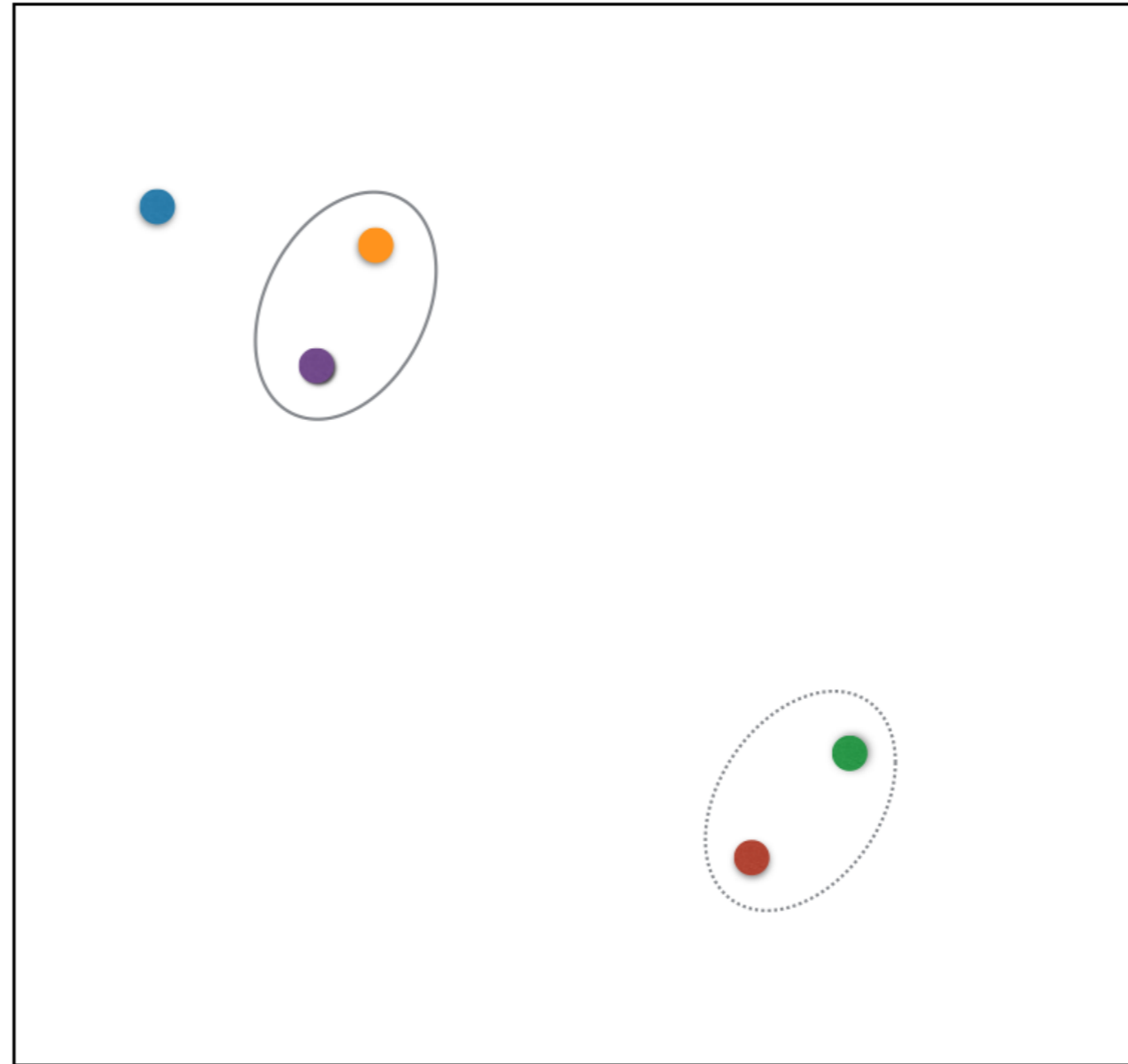
# Four clusters

4 Clusters



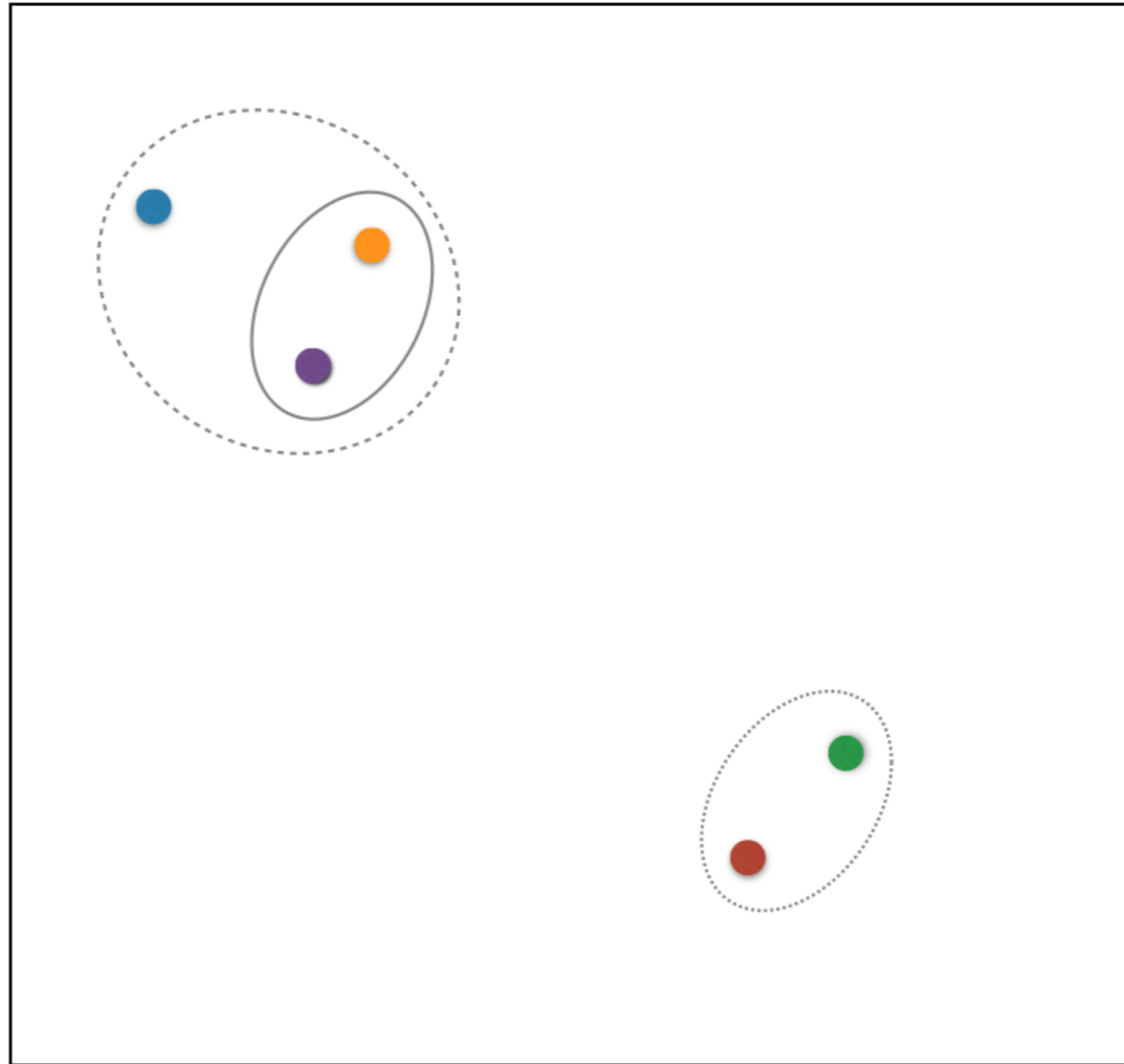
# Three clusters

3 Clusters



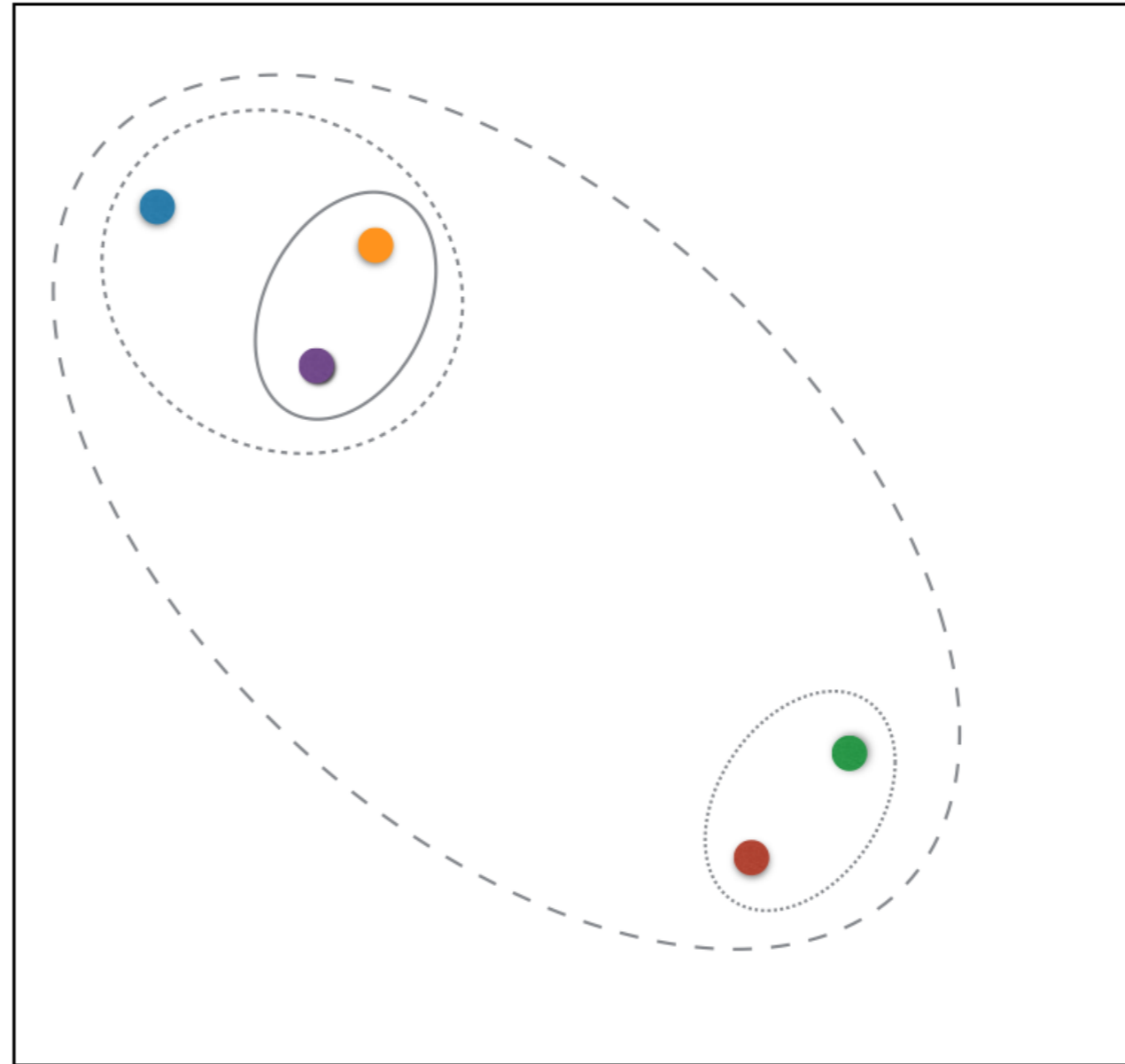
# Two clusters

2 Clusters



# One cluster

1 Cluster





# Hierarchical clustering in R

```
# Calculates similarity as Euclidean distance  
# between observations  
dist_matrix <- dist(x)  
# Returns hierarchical clustering model  
hclust(d = dist_matrix)
```

```
Call:  
hclust(d = s)  
  
Cluster method : complete  
Distance       : euclidean  
Number of objects: 50
```

# Let's practice!

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# Selecting number of clusters

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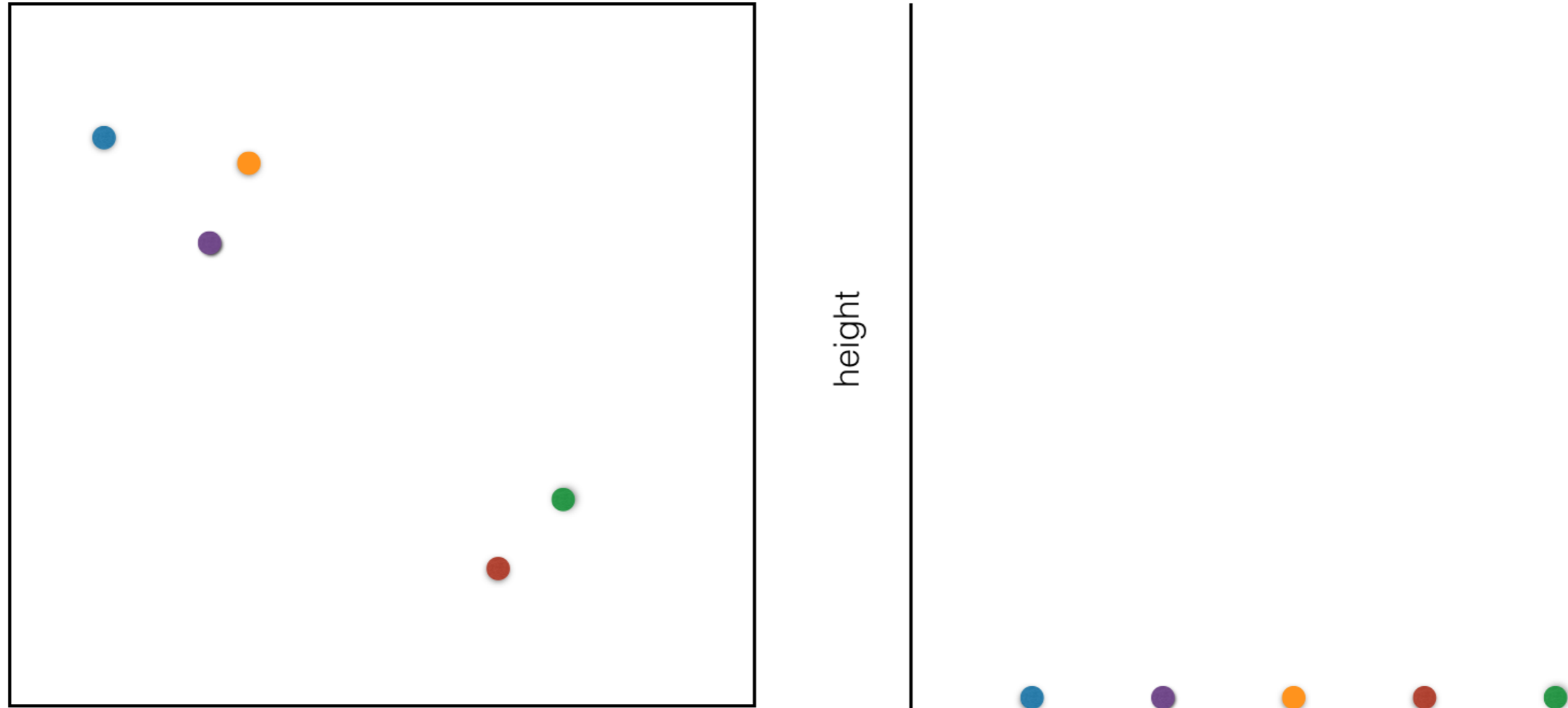
# Interpreting results

```
# Create hierarchical cluster model: hclust.out
hclust.out <- hclust(dist(x))
# Inspect the result
summary(hclust.out)
```

```
      Length Class  Mode
merge      98  -none- numeric
height     49  -none- numeric
order      50  -none- numeric
labels      0  -none-  NULL
method      1  -none- character
call        2  -none-  call
dist.method  1  -none- character
```

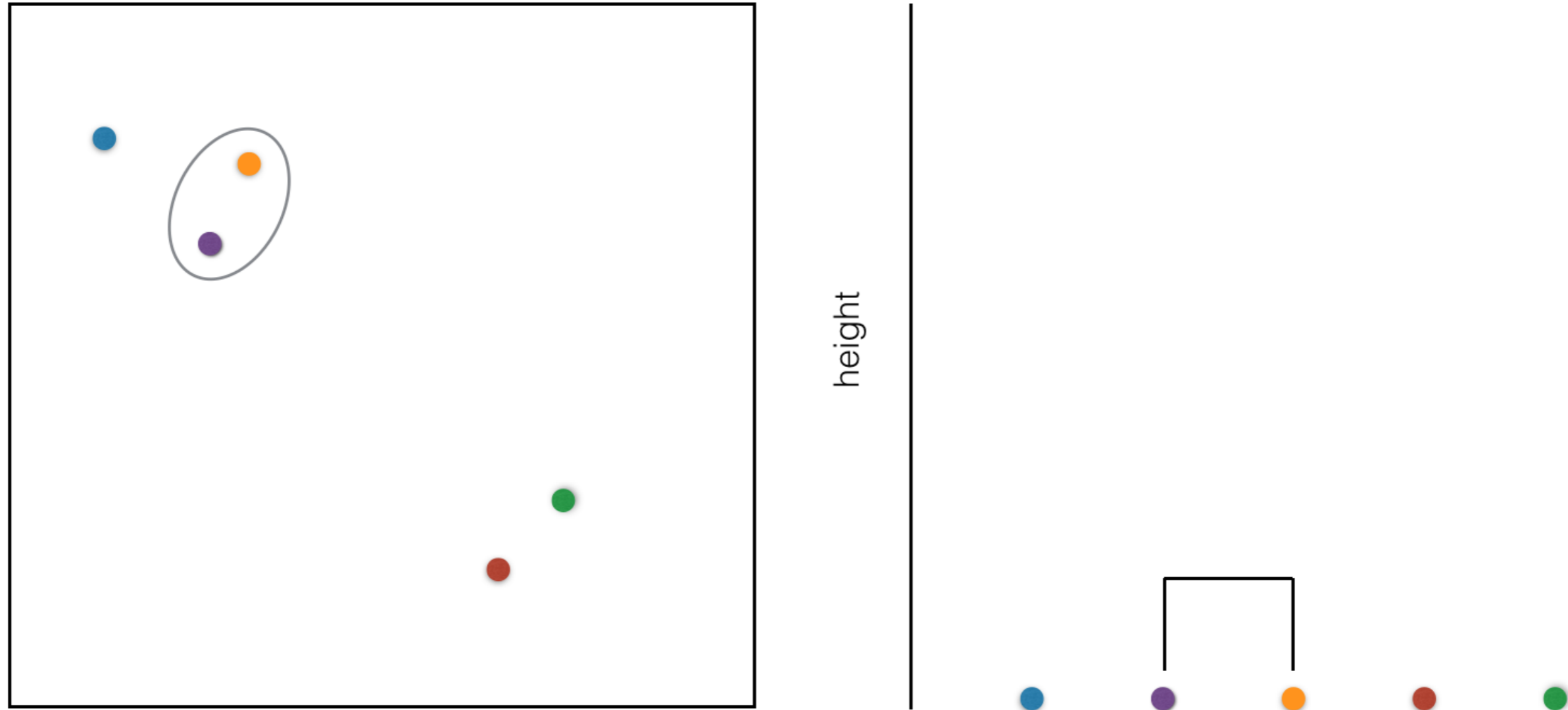
# Dendrogram

- Tree shaped structure used to interpret hierarchical clustering models



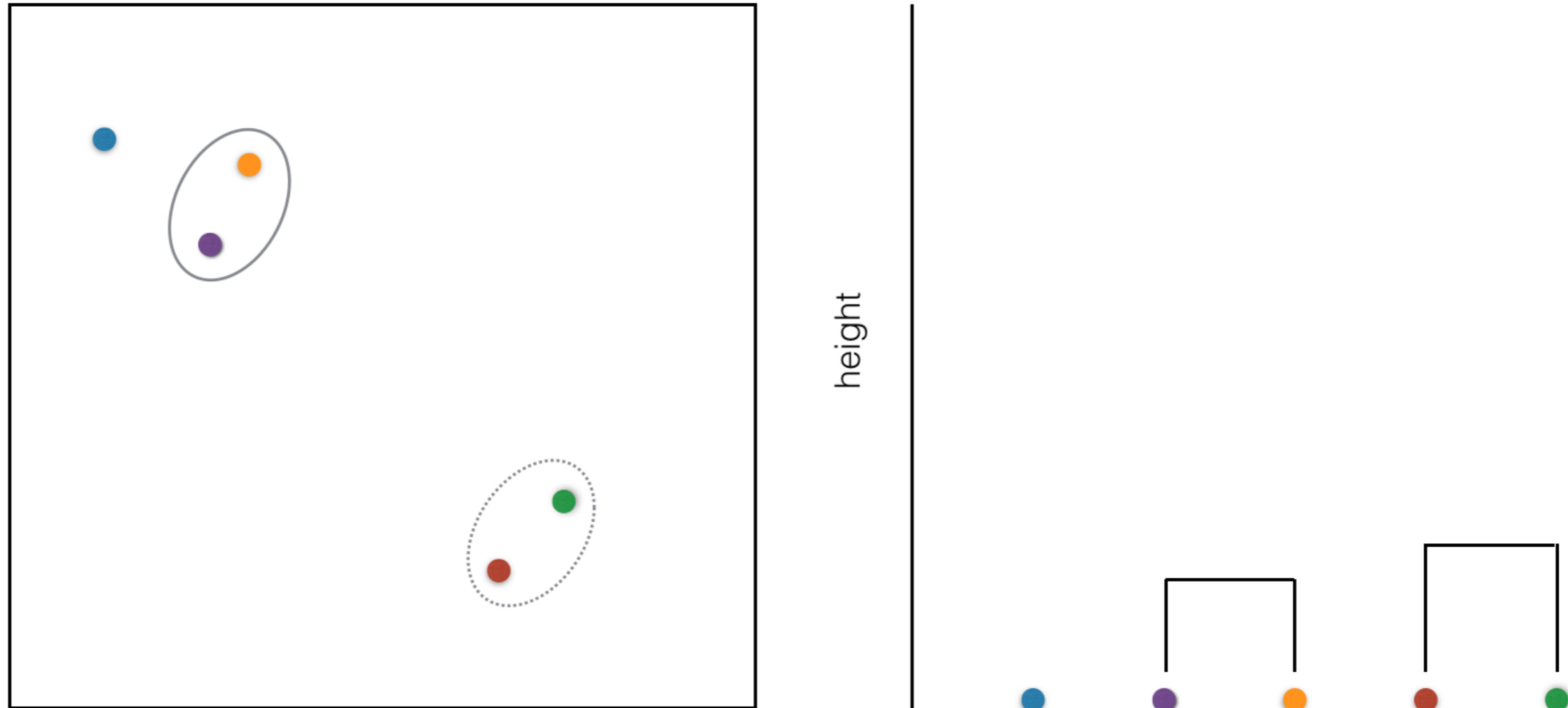
# Dendrogram

- Tree shaped structure used to interpret hierarchical clustering models



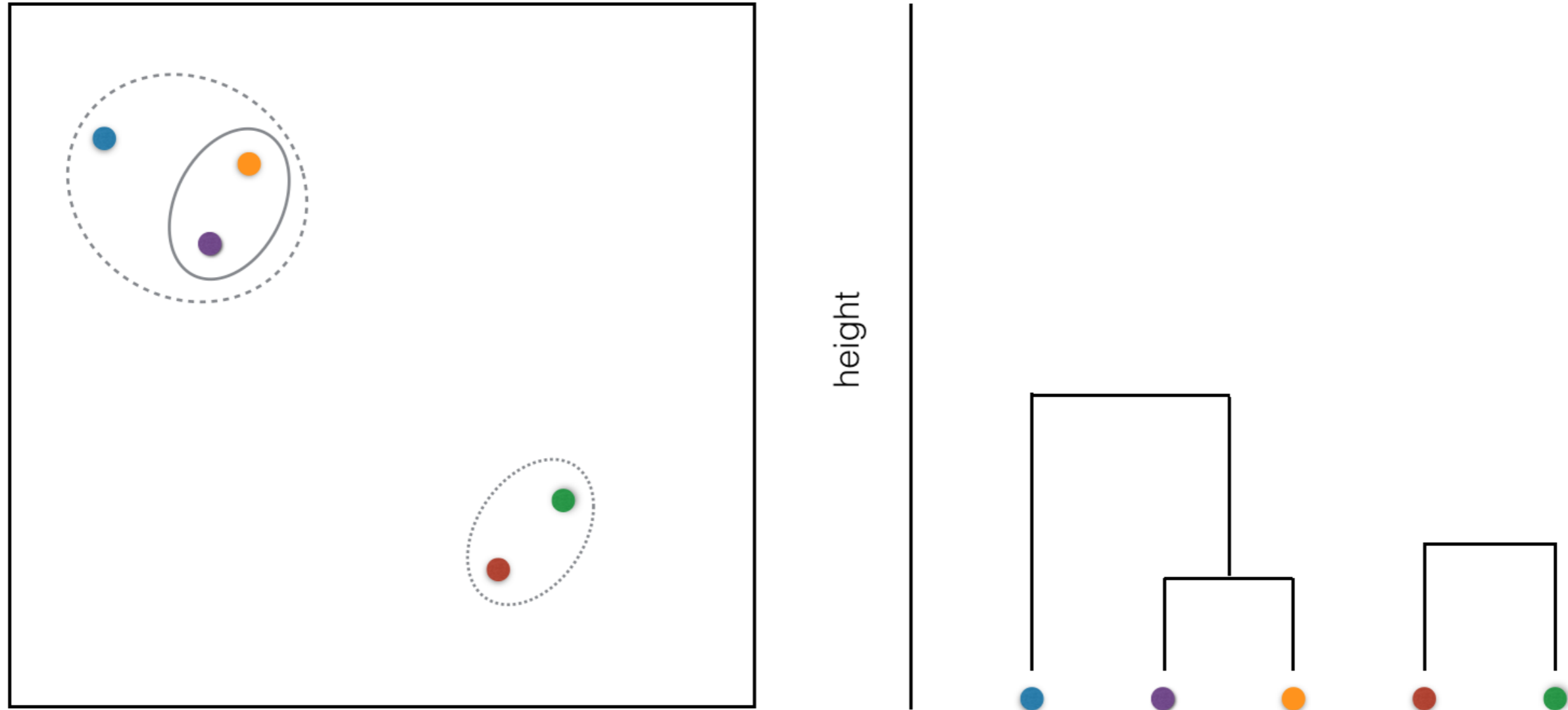
# Dendrogram

- Tree shaped structure used to interpret hierarchical clustering models



# Dendrogram

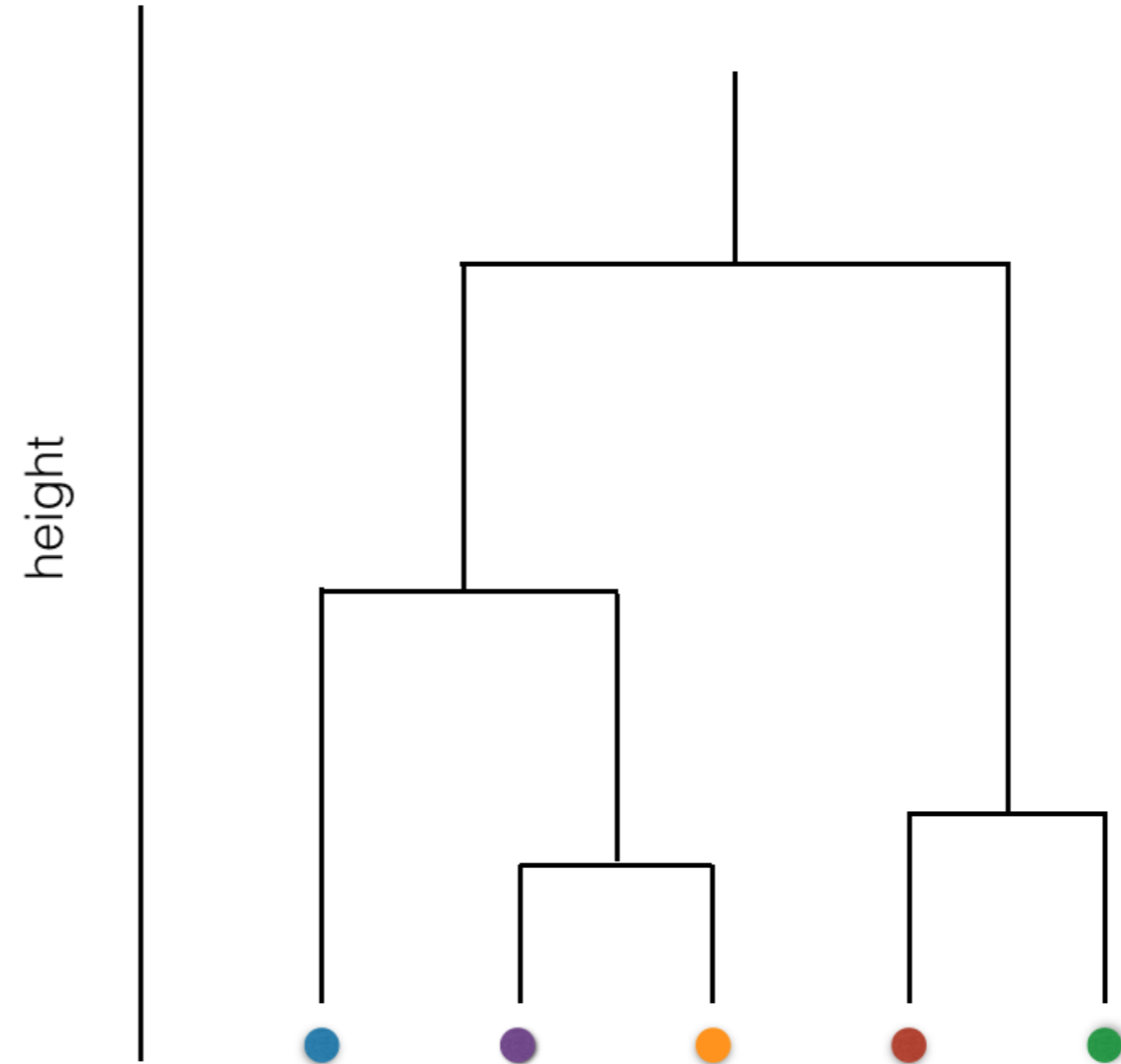
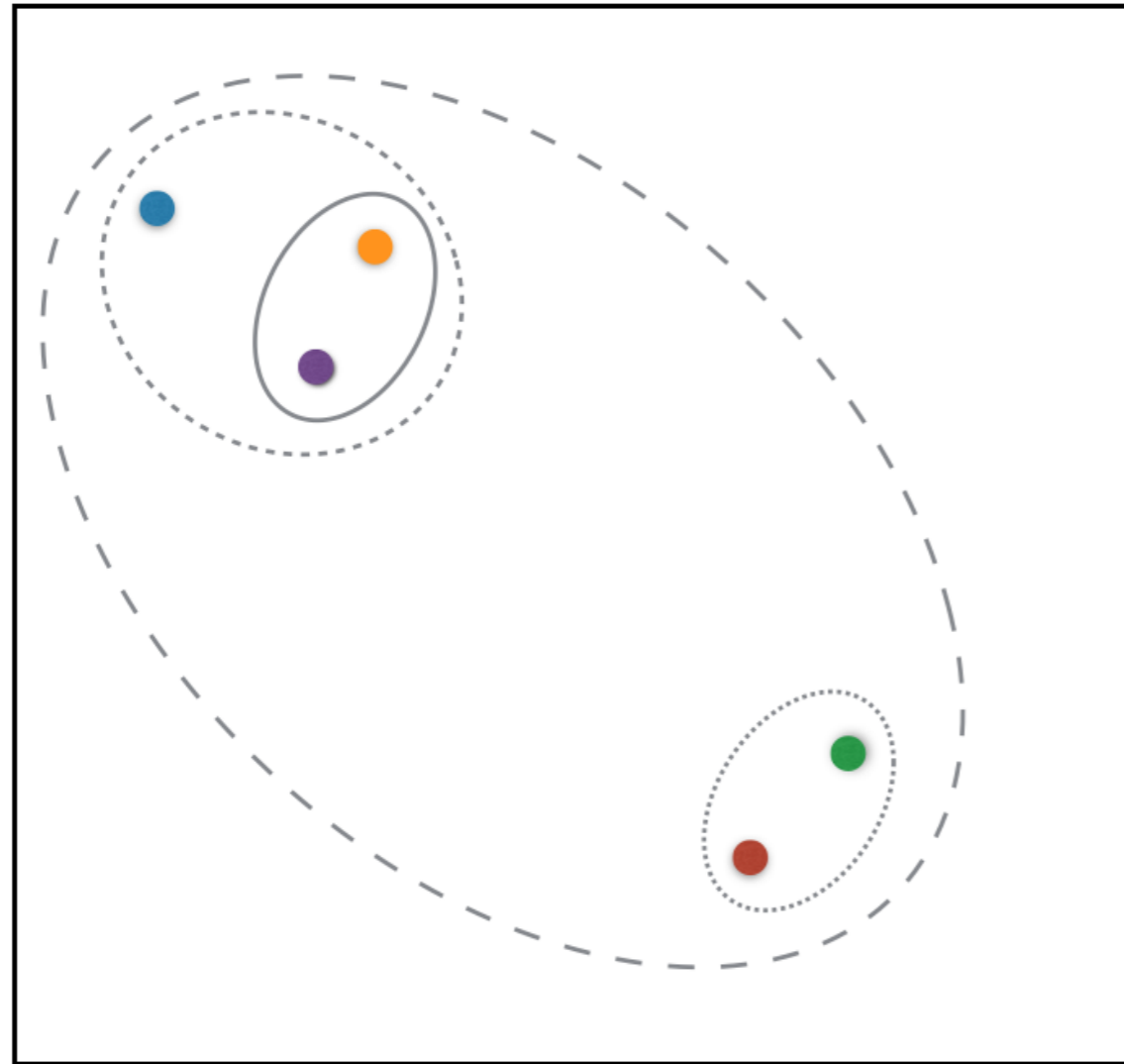
- Tree shaped structure used to interpret hierarchical clustering models





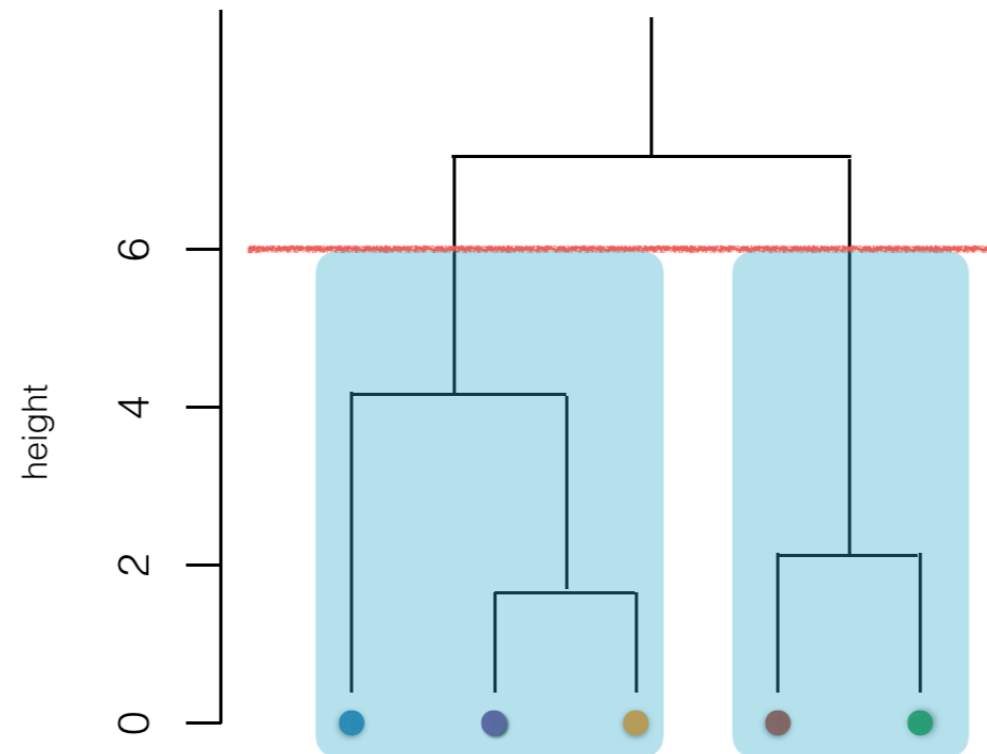
# Dendrogram

- Tree shaped structure used to interpret hierarchical clustering models



# Dendrogram plotting in R

```
# Draws a dendrogram  
plot(hclust.out)  
abline(h = 6, col = "red")
```



# Tree "cutting" in R

```
# Cut by height h  
cutree(hclust.out, h = 6)
```

```
1 1 1 1 1 1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 3 3 3  
3 3 3 3 3 3 3 4 4 4 4 4 4 4 4 4 2 4 2 4 4
```

```
# Cut by number of clusters k  
cutree(hclust.out, k = 2)
```

```
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 2 2  
2 2 2 2 2 2 2 1 1 1 1 1 1 1 1 2 1 1 1 1 1
```

# Let's practice!

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# Clustering linkage and practical matters

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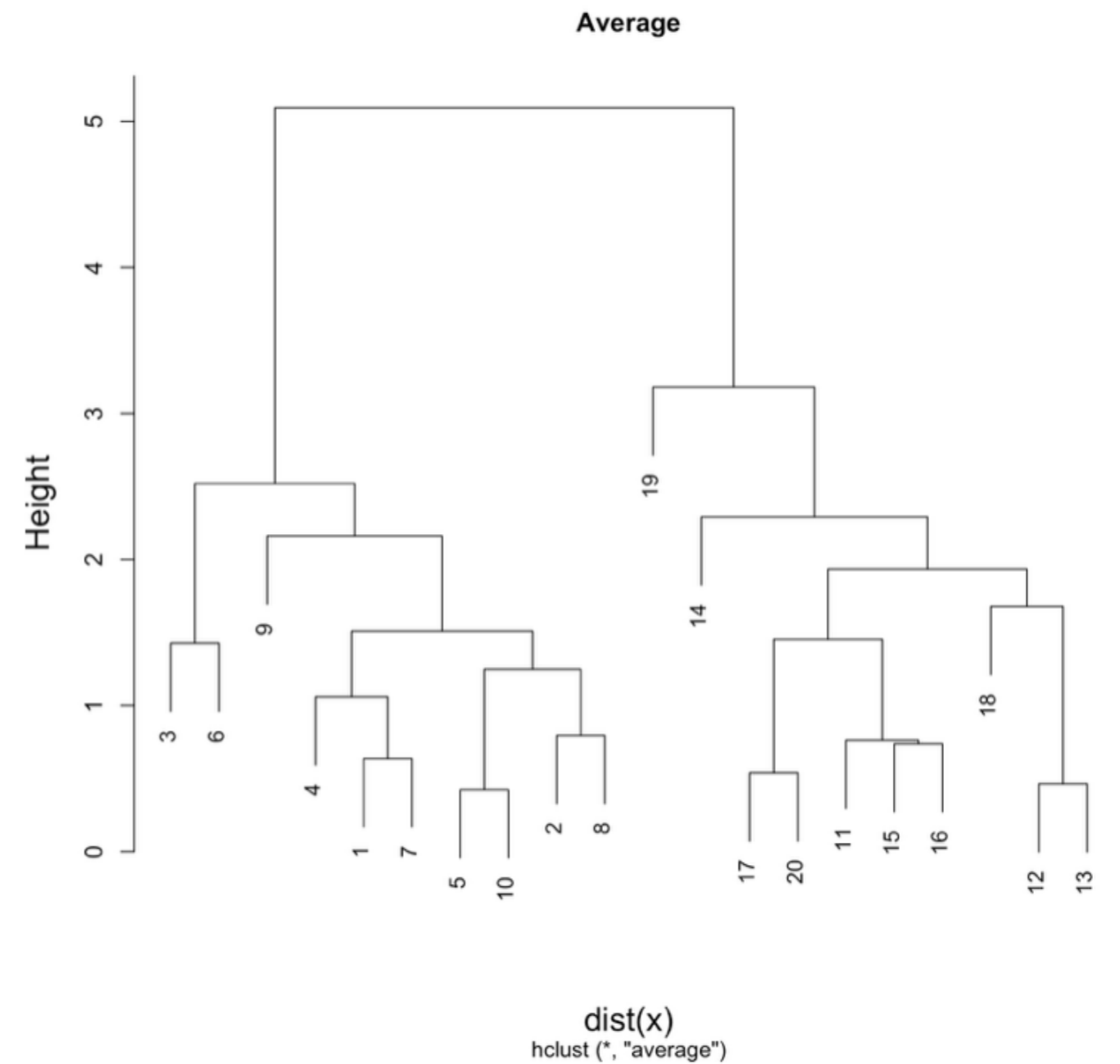
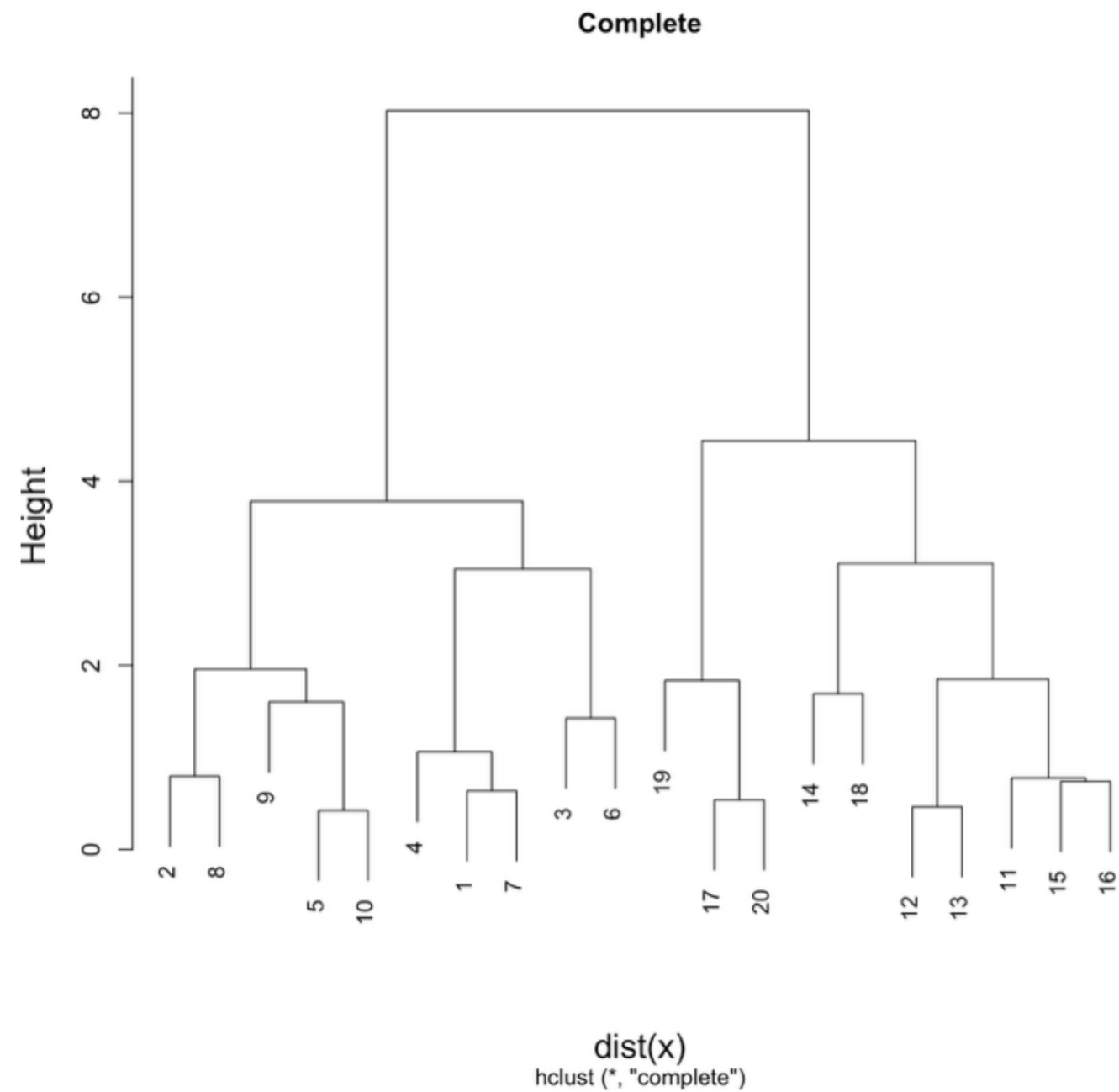
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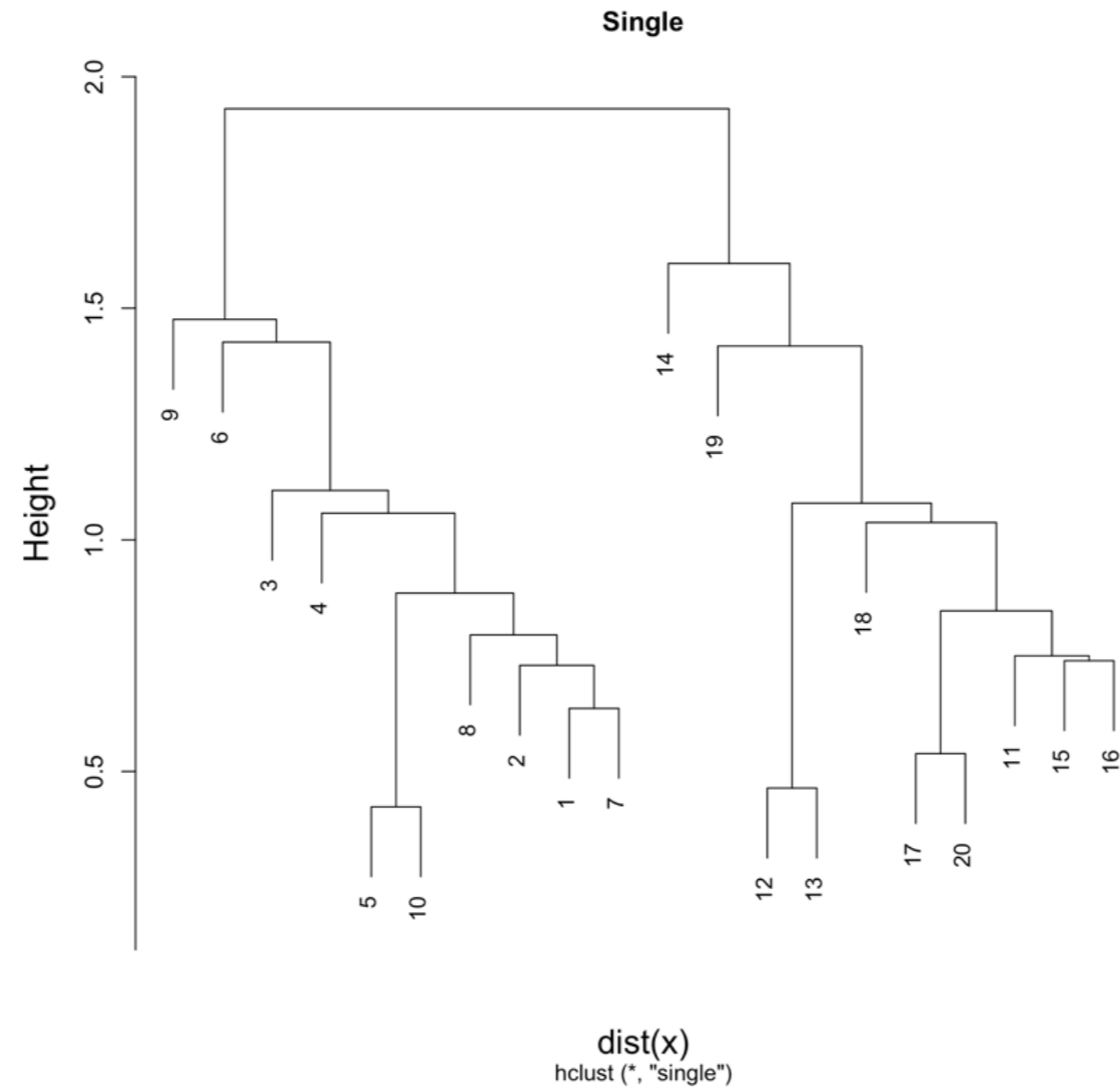
# Linking clusters in hierarchical clustering

- How is distance between clusters determined? Rules?
- Four methods to determine which cluster should be linked
  - *Complete*: pairwise similarity between all observations in cluster 1 and cluster 2, and uses **largest of similarities**
  - *Single*: same as above but uses **smallest of similarities**
  - *Average*: same as above but uses **average of similarities**
  - *Centroid*: finds centroid of cluster 1 and centroid of cluster 2, and uses **similarity between two centroids**

# Linking methods: complete and average

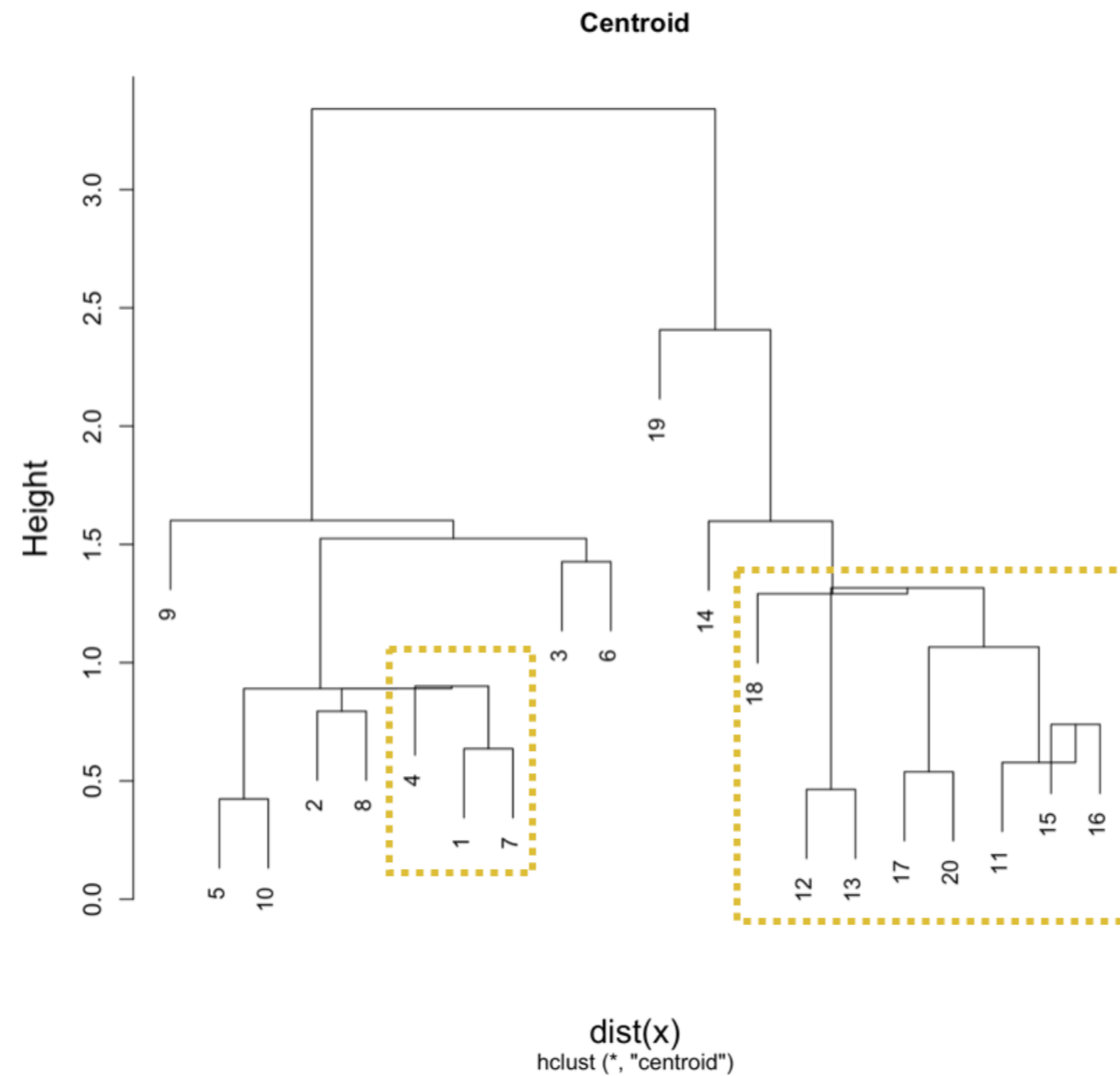


# Linking method: single





# Linking method: centroid



# Linkage in R

```
# Fitting hierarchical clustering models using different methods  
hclust.complete <- hclust(d, method = "complete")  
hclust.average <- hclust(d, method = "average")  
hclust.single <- hclust(d, method = "single")
```

# Practical matters

- Data on different scales can cause undesirable results in clustering methods
- Solution is to scale data so that features have same mean and standard deviation
  - Subtract mean of a feature from all observations
  - Divide each feature by the standard deviation of the feature
  - Normalized features have a mean of zero and a standard deviation of one

# Practical matters

```
# Check if scaling is necessary  
colMeans(x)
```

```
-0.1337828  0.0594019
```

```
apply(x, 2, sd)
```

```
1.974376 2.112357
```

# Practical matters

```
# Produce new matrix with columns of mean of 0 and sd of 1  
scaled_x <- scale(x)  
colMeans(scaled_x)
```

```
2.775558e-17 3.330669e-17
```

```
apply(scaled_x, 2, sd)
```

```
1 1
```

# Let's practice!

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# Review of hierarchical clustering

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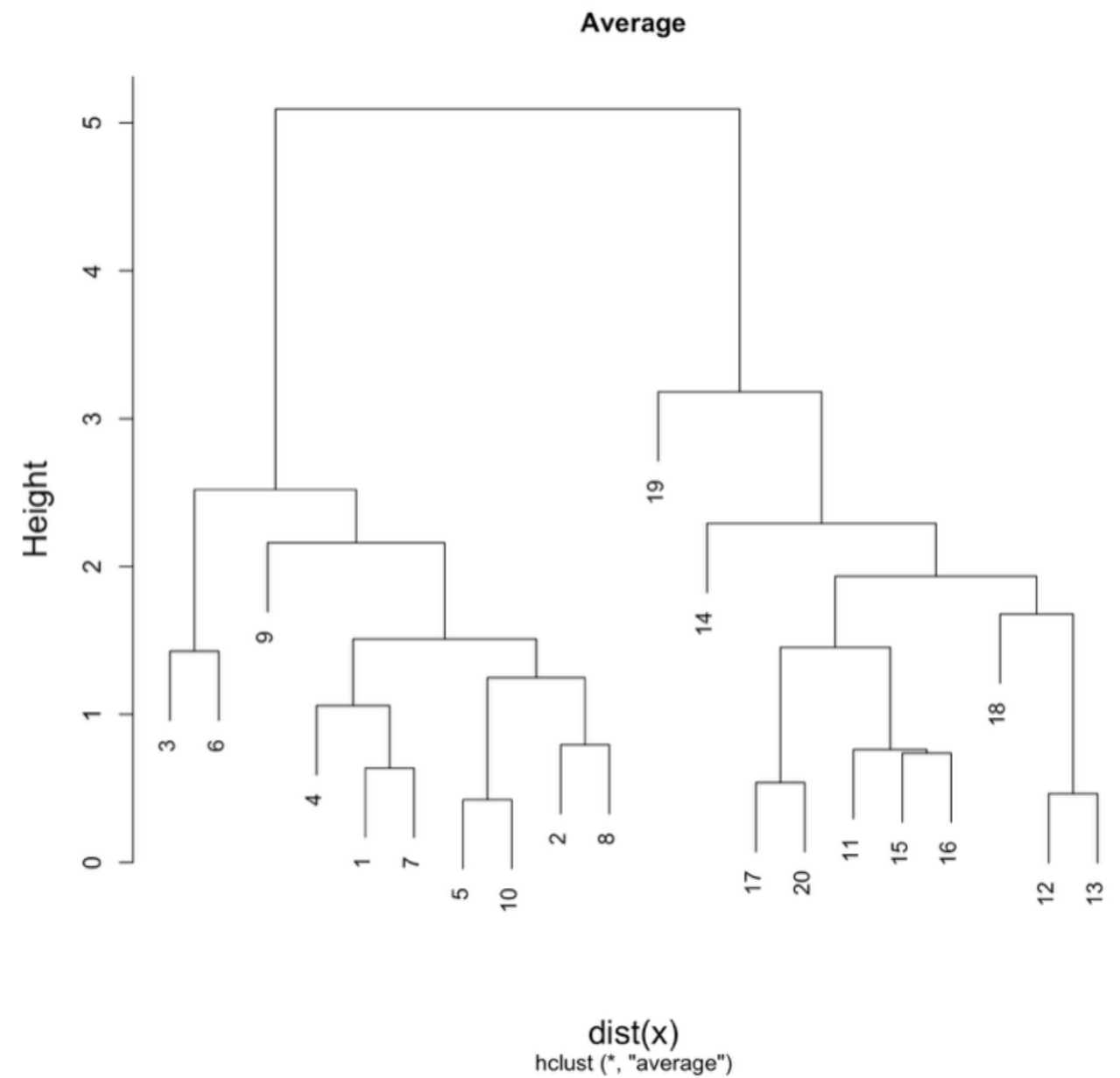
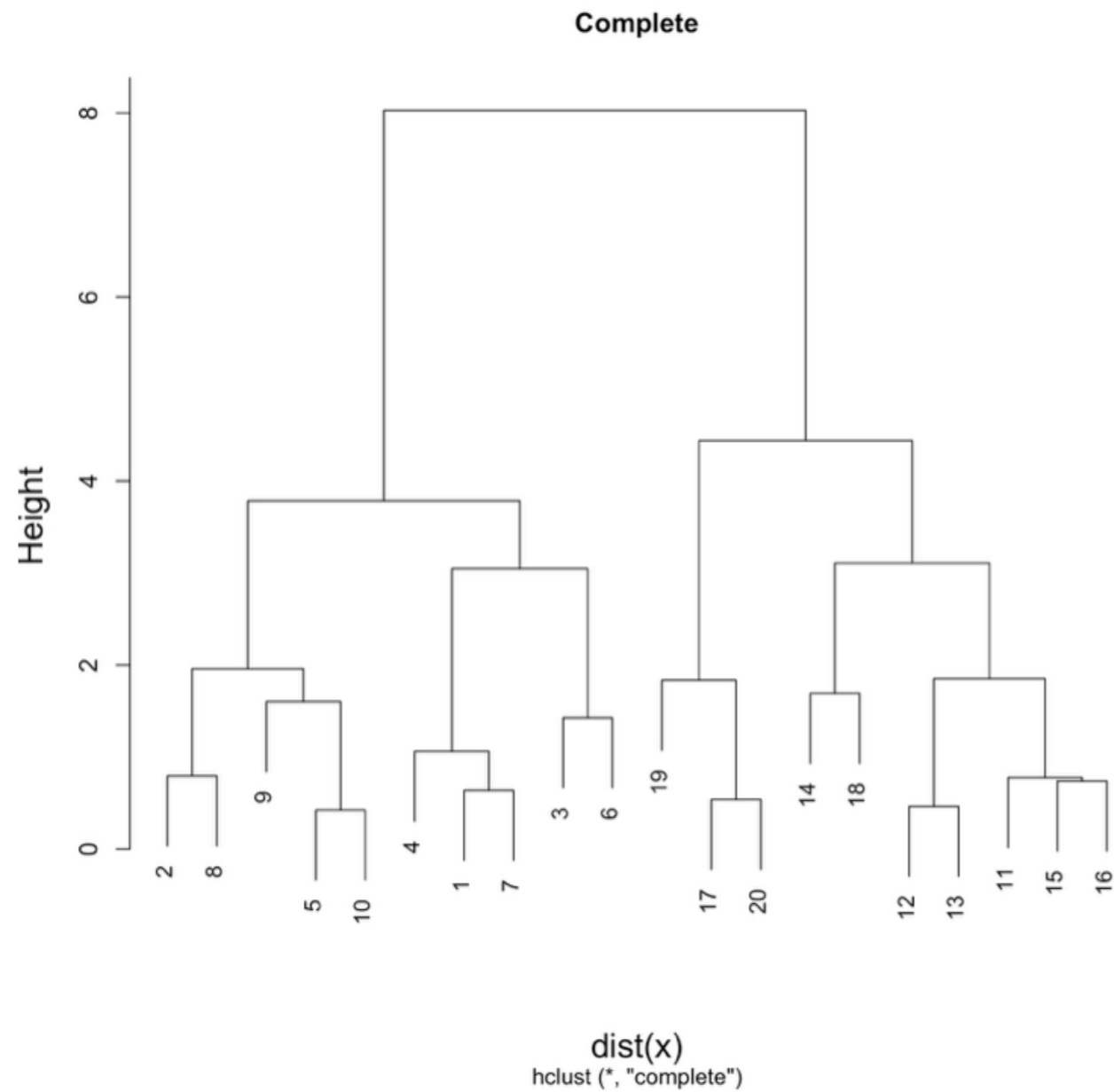
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# Hierarchical clustering review

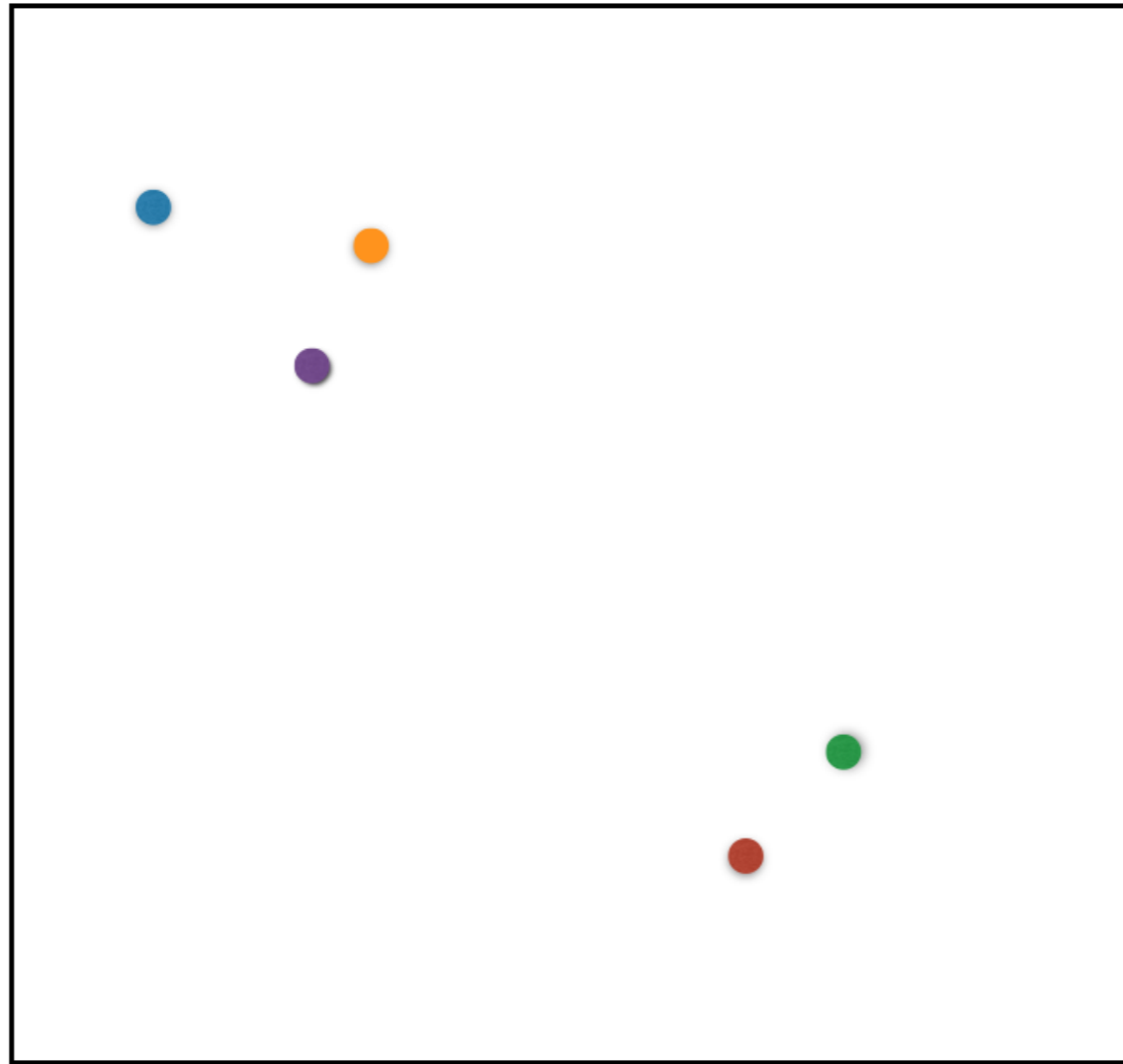
```
# Fitting various hierarchical clustering models  
hclust.complete <- hclust(d, method = "complete")  
hclust.average <- hclust(d, method = "average")  
hclust.single <- hclust(d, method = "single")
```



# Linking methods: complete and average



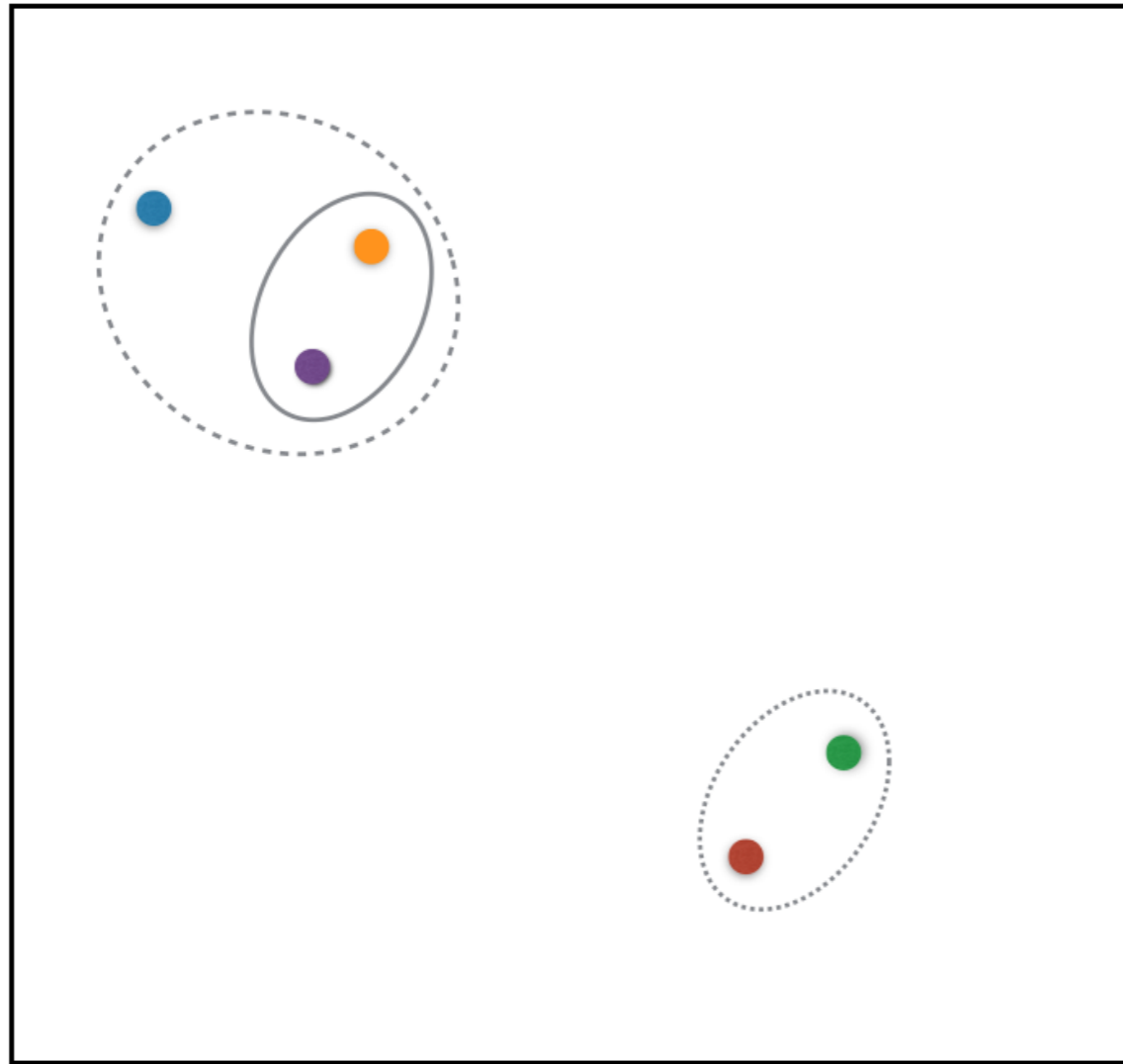
# Hierarchical clustering



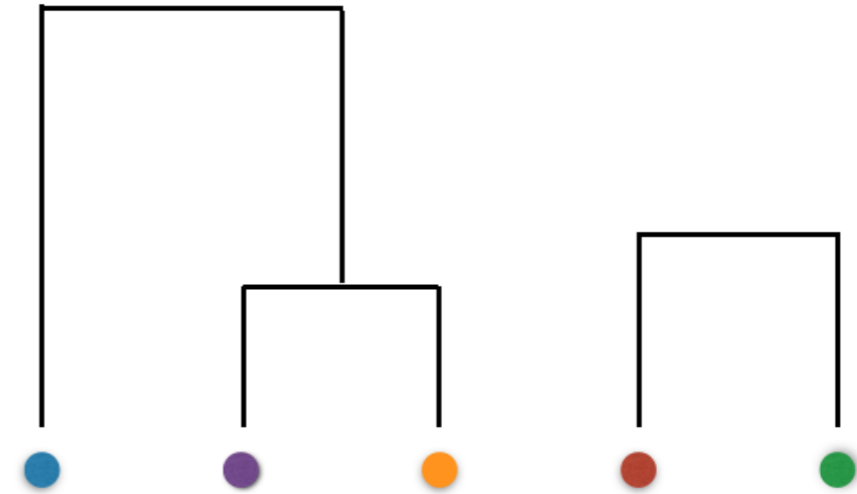
height



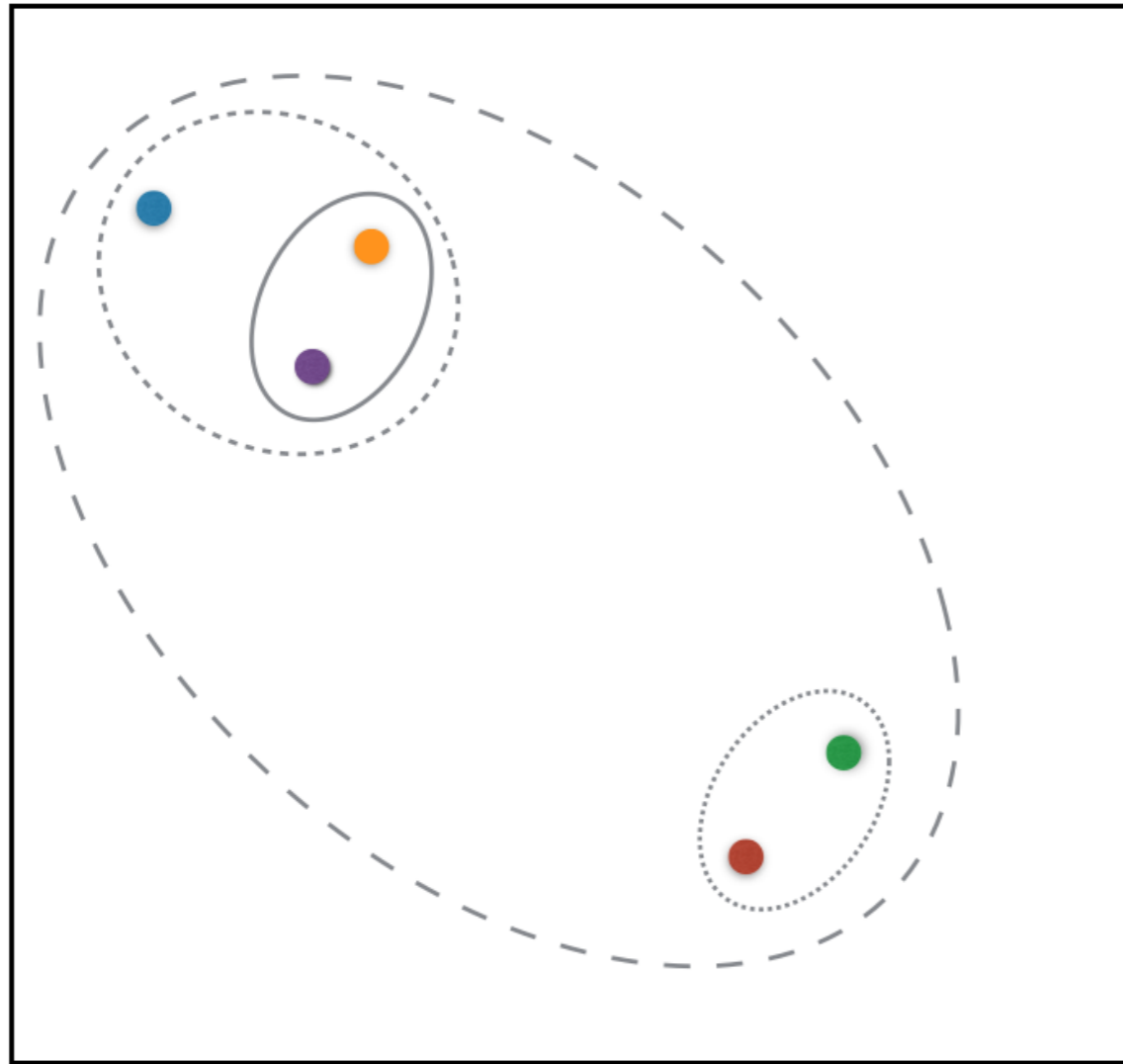
# Iterating



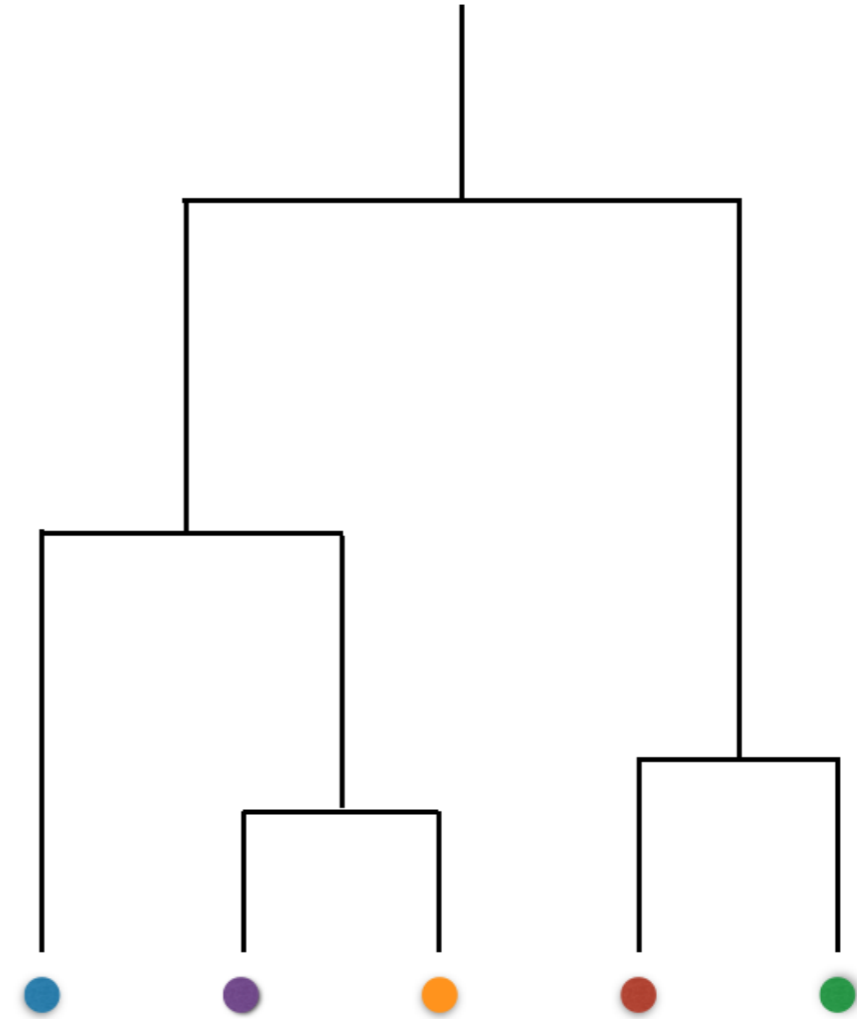
height



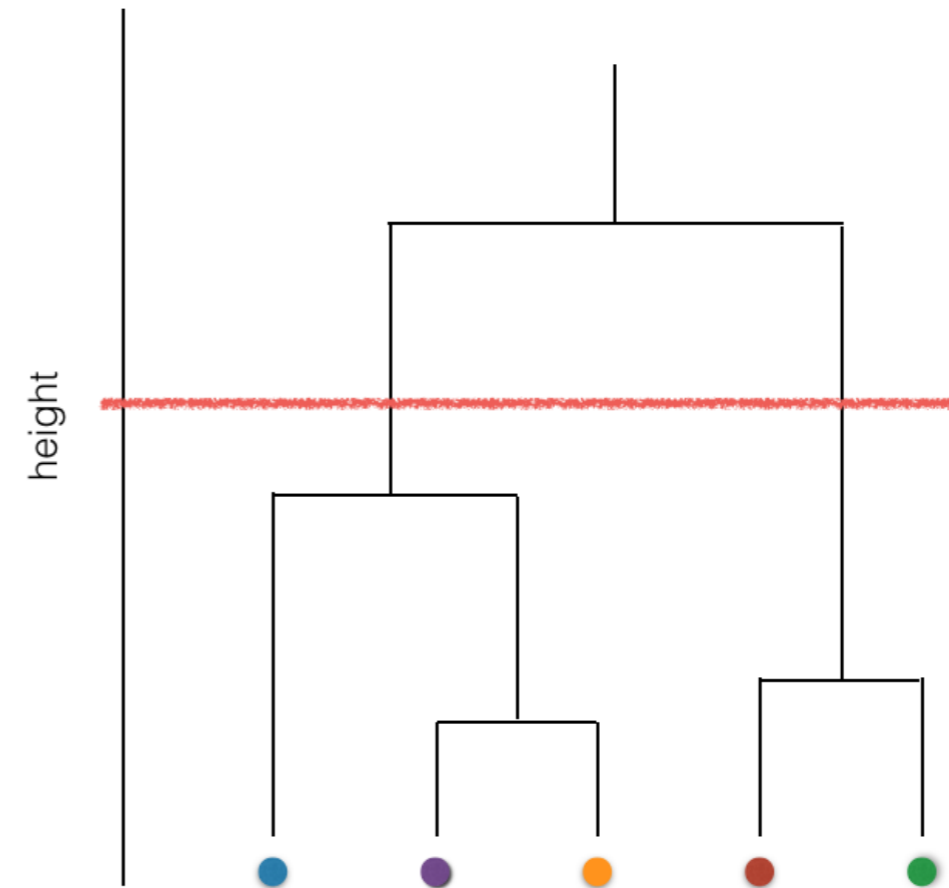
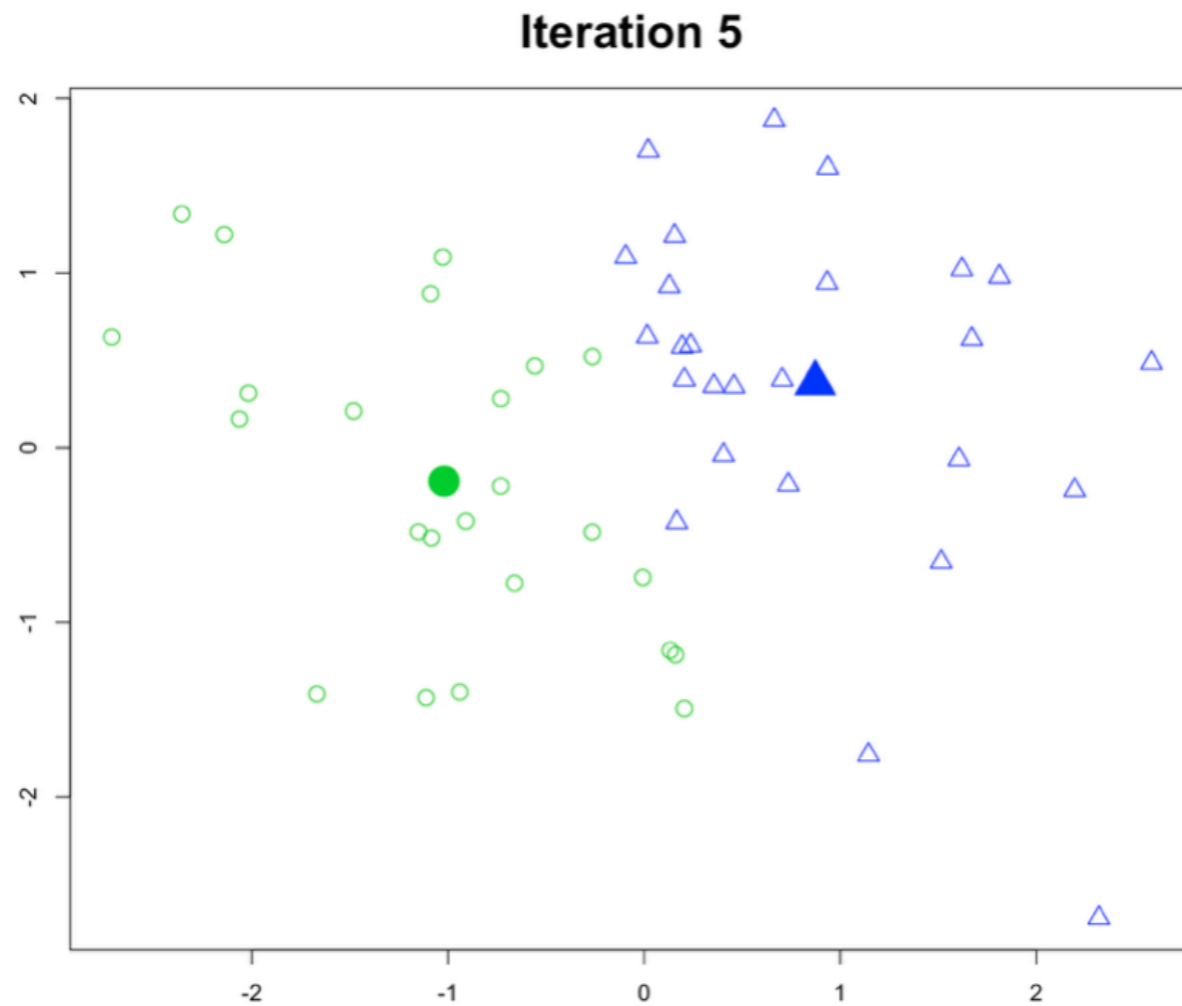
# Dendrogram



height



# How k-means and hierarchical clustering differ



# Practical matters

```
# Scale the data
pokemon.scaled <- scale(pokemon)

# Create hierarchical and k-means clustering models
hclust.pokemon <- hclust(dist(pokemon.scaled), method = "complete")
km.pokemon <- kmeans(pokemon.scaled, centers = 3,
                    nstart = 20, iter.max = 50)

# Compare results of the models
cut.pokemon <- cutree(hclust.pokemon, k = 3)
table(km.pokemon$cluster, cut.pokemon)
cut.pokemon
```

```
      1  2  3
1 242  1  0
2 342  1  0
3 204  9  1
```

# Let's practice!

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