

# The normal distribution

FOUNDATIONS OF PROBABILITY IN R

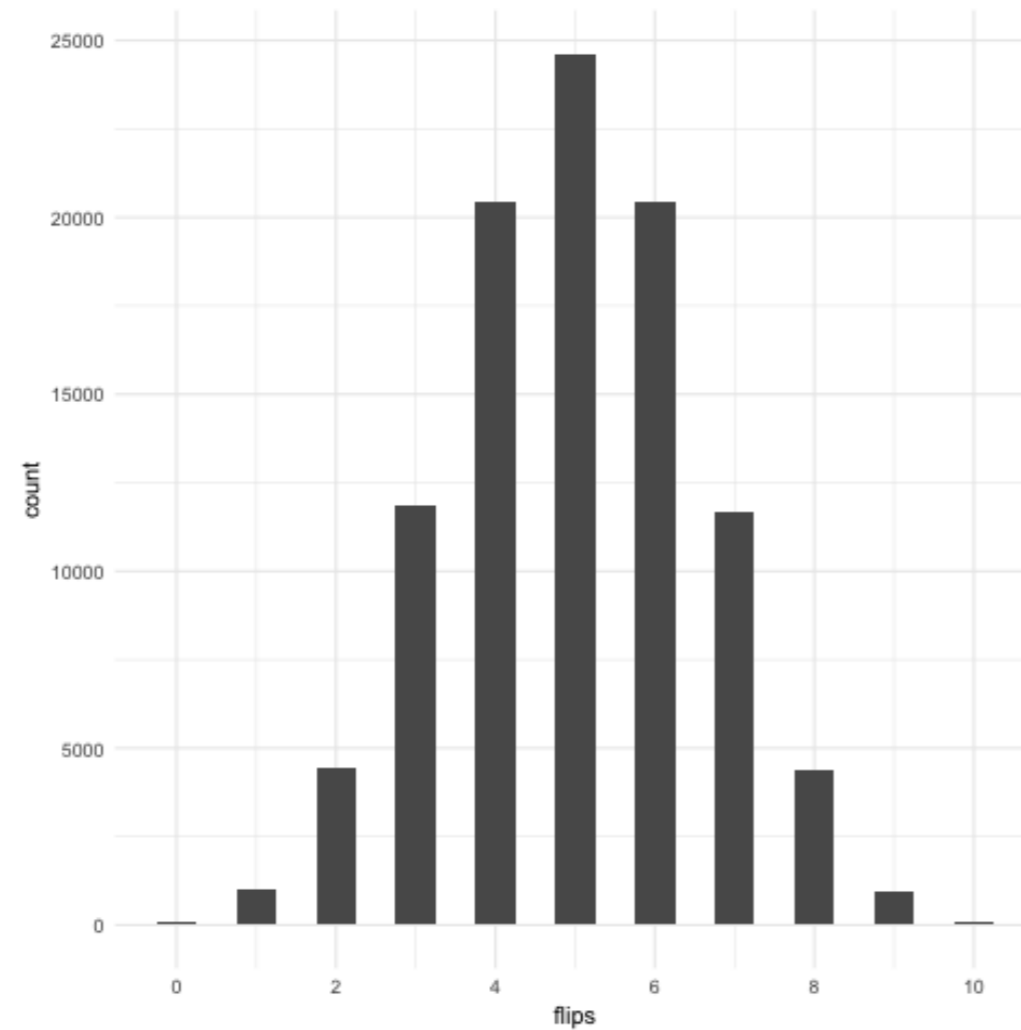


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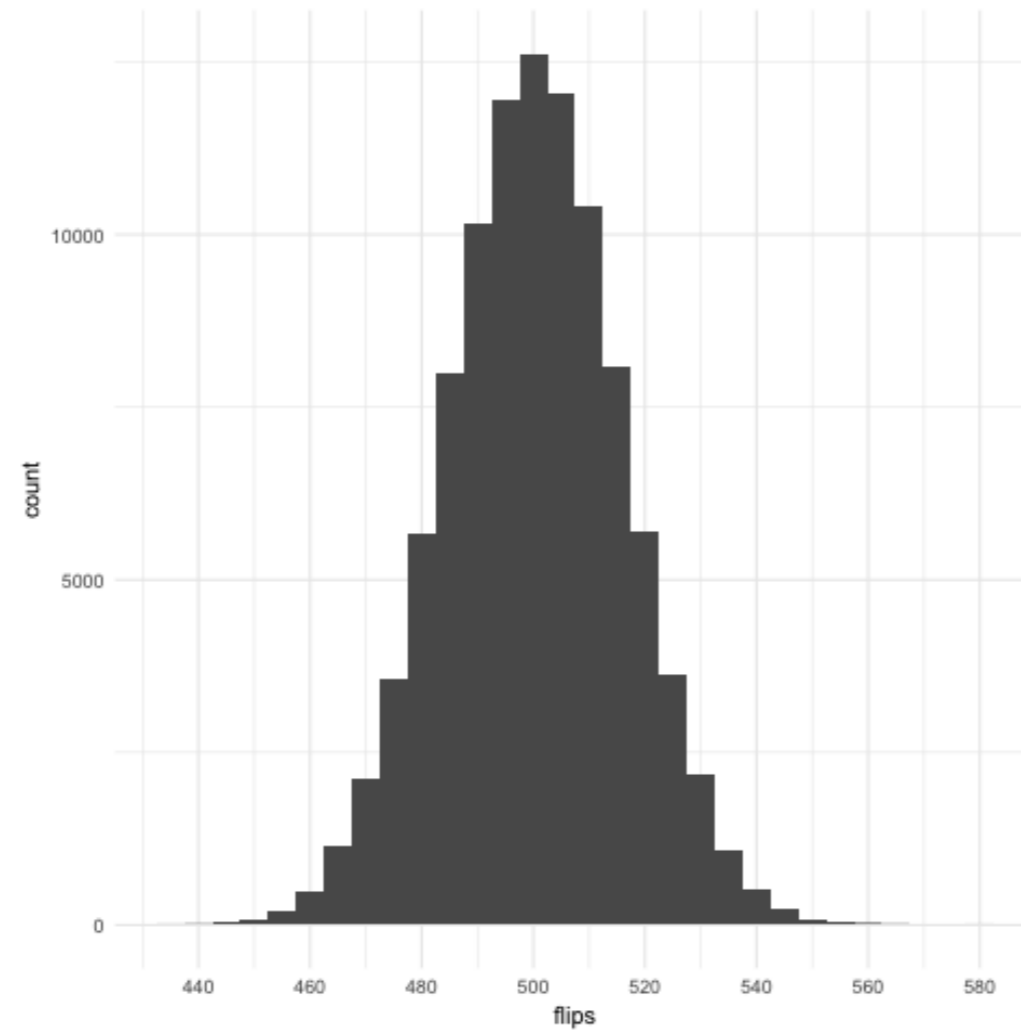
# Flipping 10 coins

```
flips <- rbinom(100000, 10, .5)
```

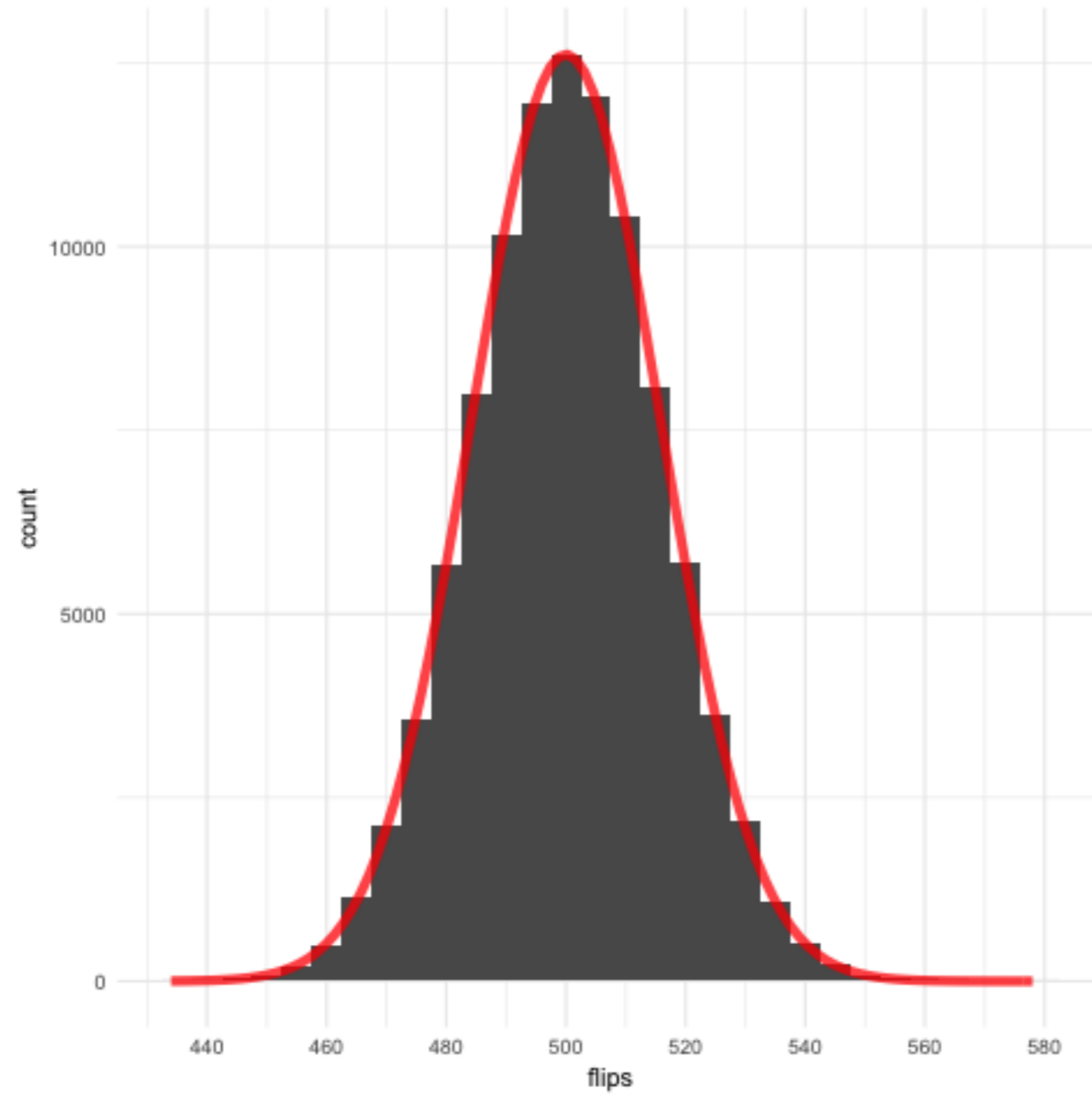


# Flipping 1000 coins

```
flips <- rbinom(100000, 1000, .5)
```



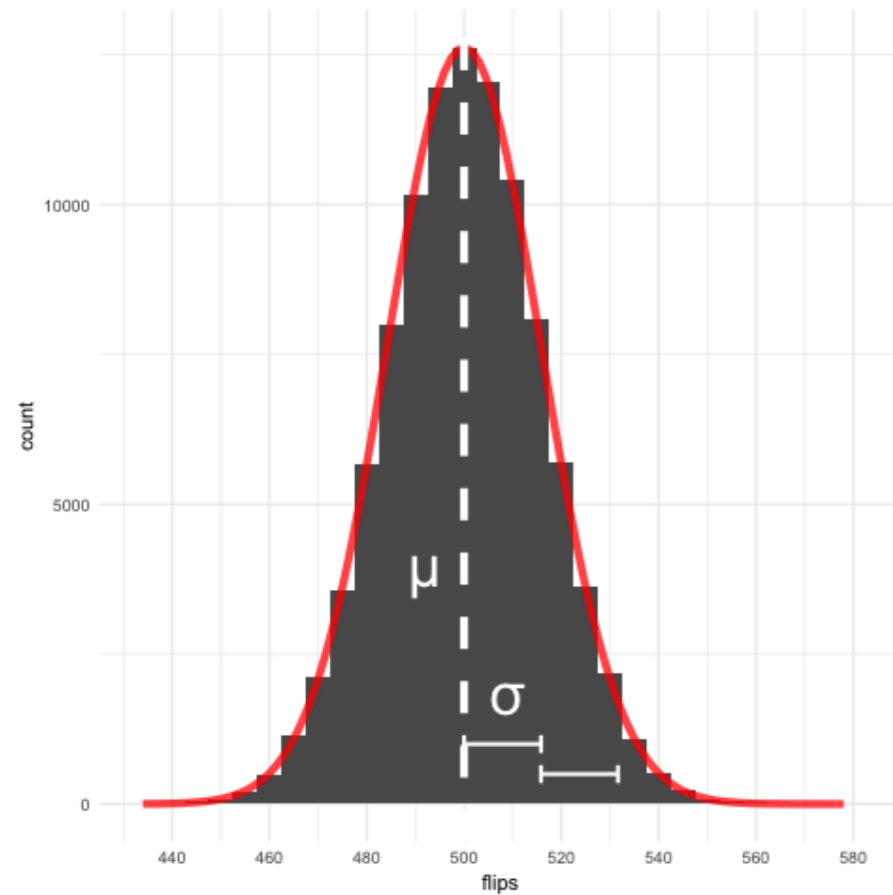
# Flipping 1000 coins



# Normal distribution has mean and standard deviation

$$X \sim \text{Normal}(\mu, \sigma)$$

$$\sigma = \sqrt{\text{Var}(X)}$$



# Normal approximation to the binomial

```
binomial <- rbinom(100000, 1000, .5)
```

$$\mu = \text{size} \cdot p$$

$$\sigma = \sqrt{\text{size} \cdot p \cdot (1 - p)}$$

```
expected_value <- 1000 * .5
```

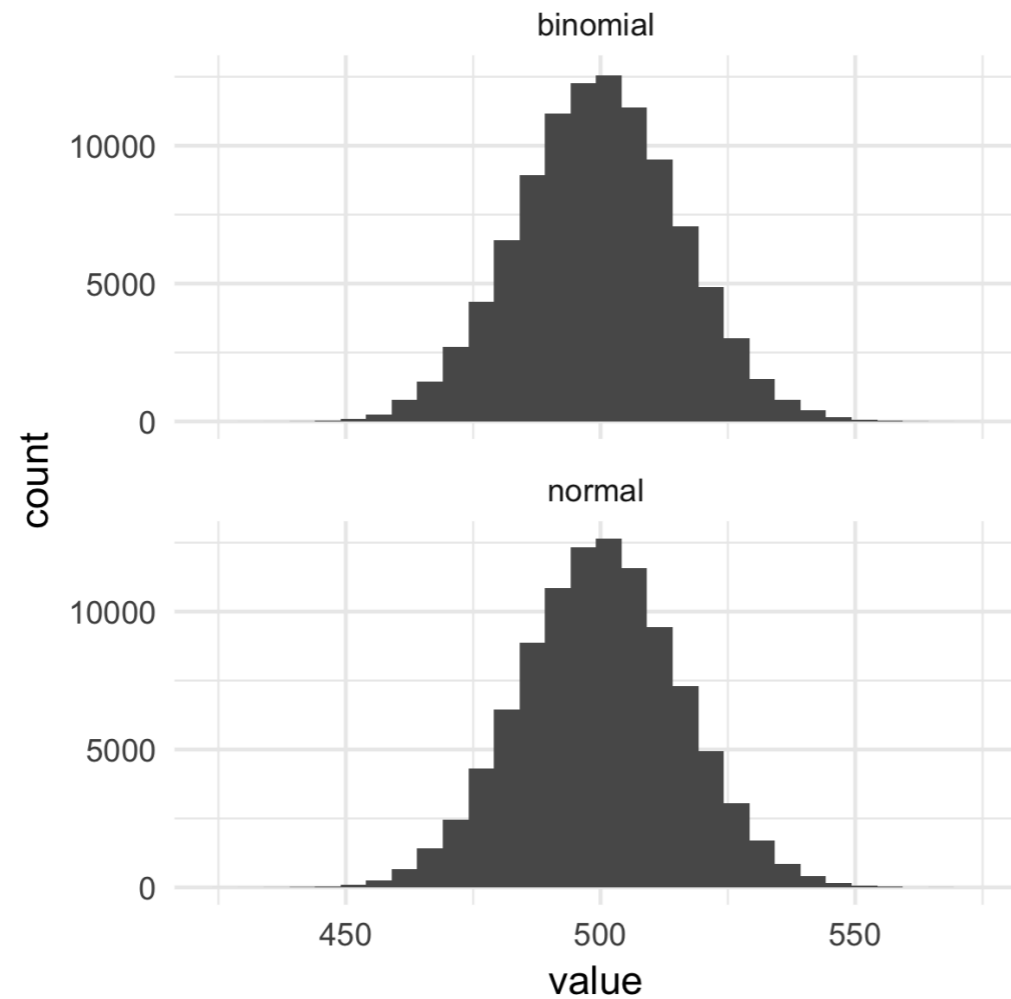
```
variance <- 1000 * .5 * (1 - .5)
```

```
stdev <- sqrt(variance)
```

```
normal <- rnorm(100000, expected_value, stdev)
```

# Comparing histograms

```
compare_histograms(binomial, normal)
```



# Let's practice!

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# The Poisson distribution

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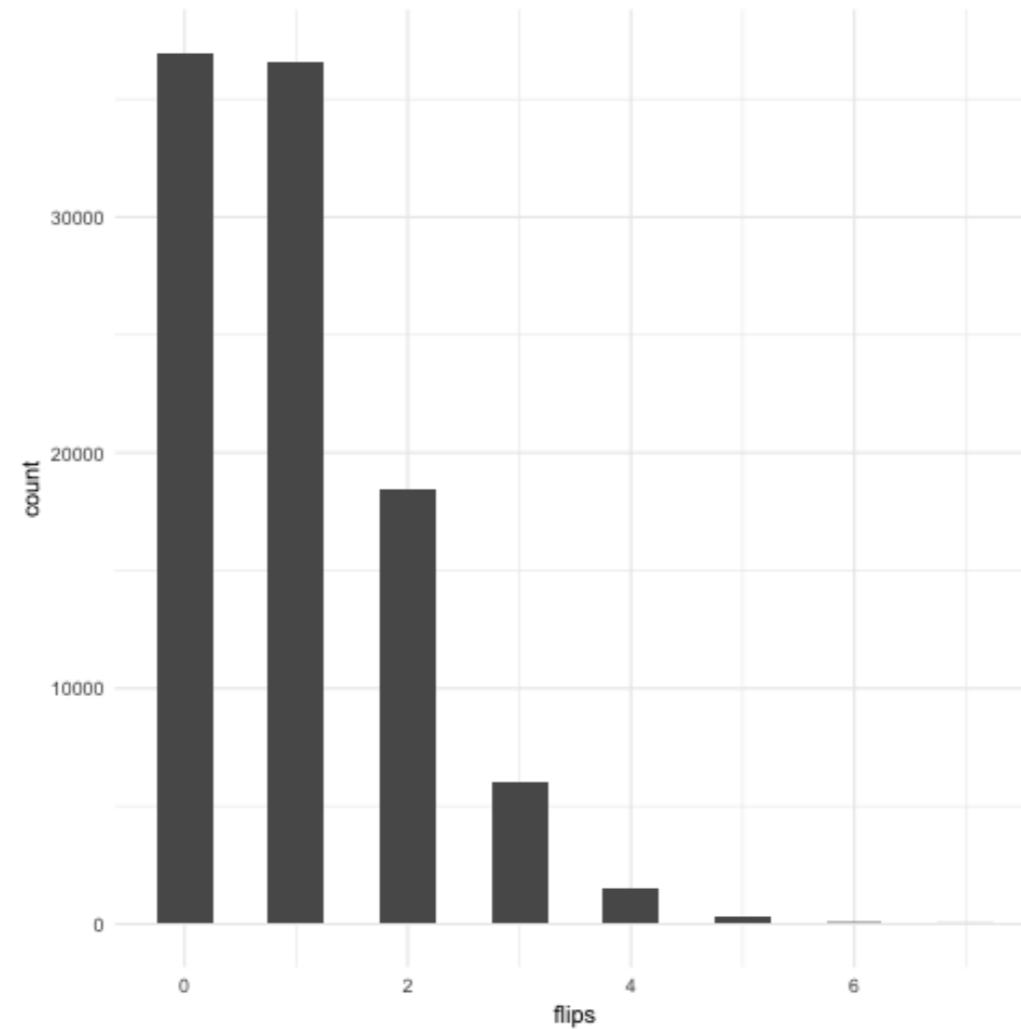


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# Flipping many coins, each with low probability

```
binomial <- rbinom(100000, 1000, 1 / 1000)
```



# Properties of the Poisson distribution

```
binomial <- rbinom(100000, 1000,  
                  1 / 1000)
```

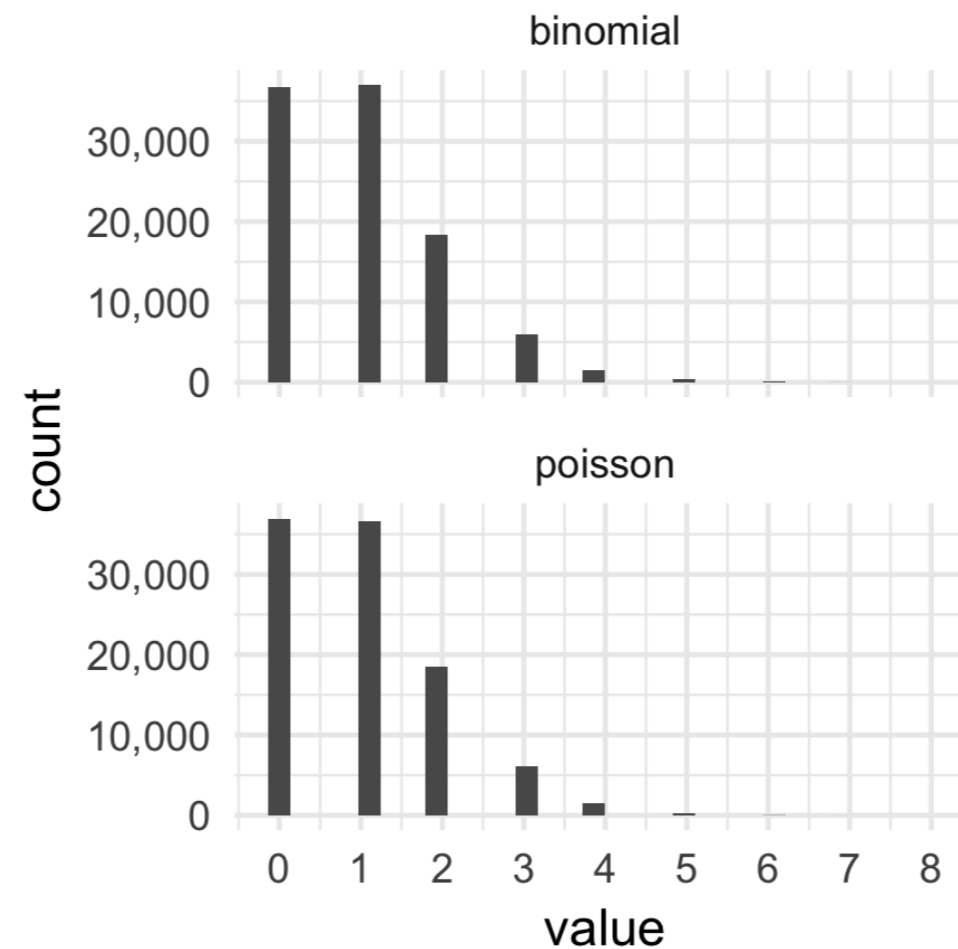
```
poisson <- rpois(100000, 1)
```

```
compare_histograms(binomial,  
                   poisson)
```

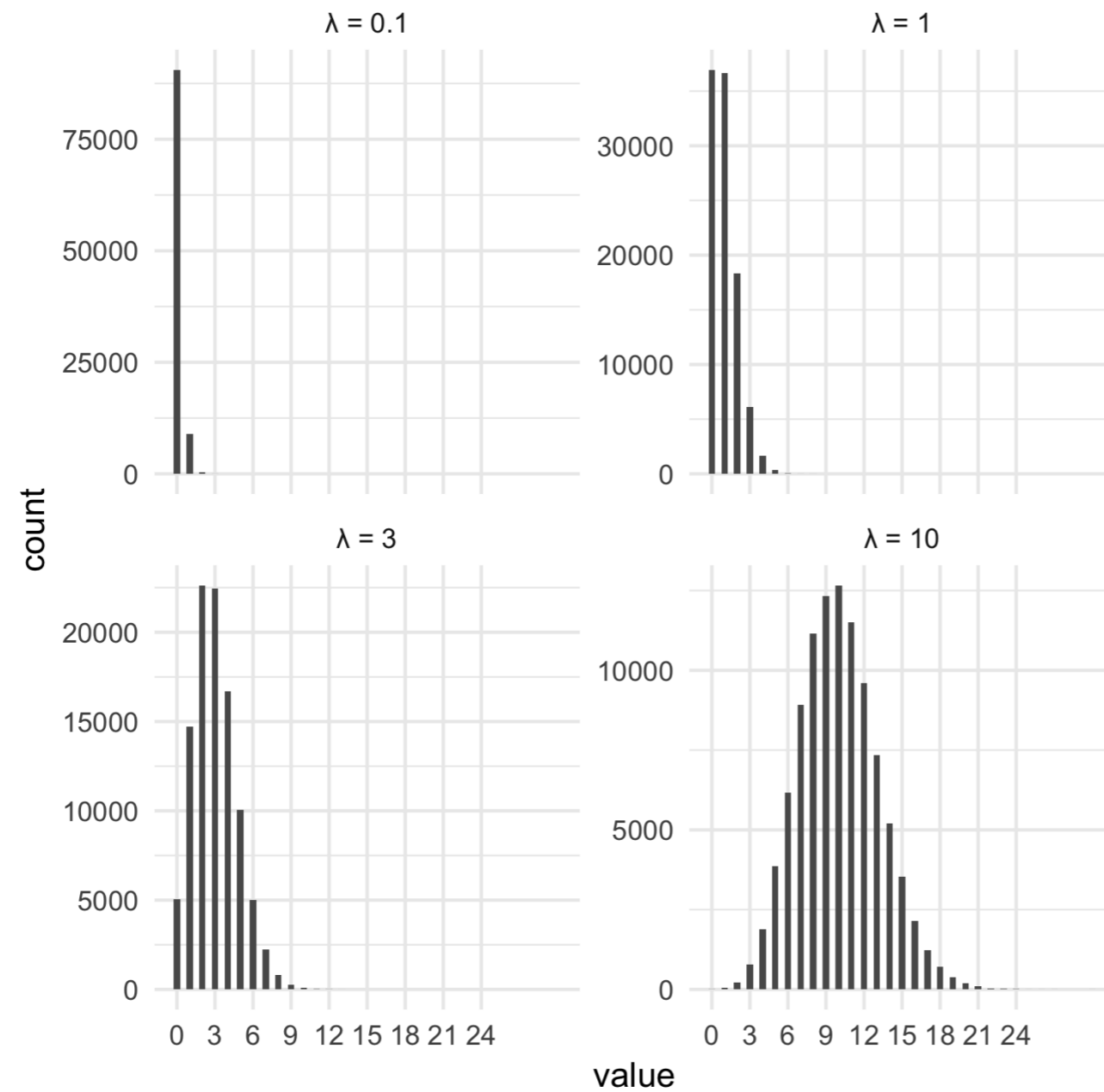
$$X \sim \text{Poisson}(\lambda)$$

$$E[X] = \lambda$$

$$\text{Var}(X) = \lambda$$



# Poisson distribution



# Let's practice!

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# The geometric distribution

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# Simulating waiting for heads

```
flips <- rbinom(100, 1, .1)
flips
# [1] 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0
# [16] 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0
```

```
which(flips == 1)
# [1] 8 27 44 55 82 89
```

```
which(flips == 1)[1]
# [1] 8
```

# Replicating simulations

```
which(rbinom(100, 1, .1) == 1)[1]  
# [1] 28
```

```
which(rbinom(100, 1, .1) == 1)[1]  
# [1] 4
```

```
which(rbinom(100, 1, .1) == 1)[1]  
# [1] 11
```

```
replicate(10, which(rbinom(100, 1, .1) == 1)[1])  
# [1] 22 12 6 7 35 2 4 44 4 2
```



# Simulating with rgeom

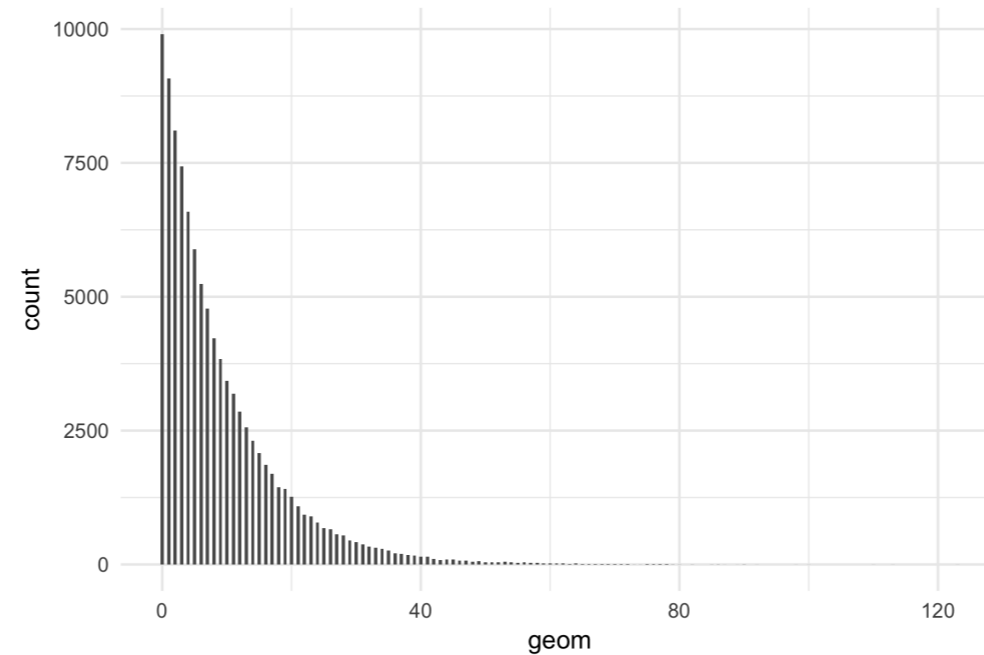
```
geom <- rgeom(100000, .1)
```

```
mean(geom)
```

```
# [1] 9.04376
```

$$X \sim \text{Geom}(p)$$

$$E[X] = \frac{1}{p} - 1$$



# Let's practice!

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