

# Neodređeni integral – 1. dio

MATEMATIKA 2

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FOI, Varaždin

# Sadržaj

prvi zadatak

drugi zadatak

treći zadatak

četvrti zadatak

peti zadatak

Diferencijal realne funkcije jedne realne varijable

šesti zadatak

sedmi zadatak

osmi zadatak

deveti zadatak

deseti zadatak

Napomena za logaritamsku funkciju

jedanaesti zadatak

dvanaesti zadatak

trinaesti zadatak

četрнаesti zadatak

petnaesti zadatak

šesnaesti zadatak

sedamnaesti zadatak

**prvi zadatak**

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## Zadatak 1

Riješite neodređeni integral  $\int \frac{dx}{\sqrt[4]{x^3}}$ .

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## Rješenje

$$\int \frac{dx}{\sqrt[4]{x^3}} =$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

## Zadatak 1

Riješite neodređeni integral  $\int \frac{dx}{\sqrt[4]{x^3}}$ .

## Rješenje

$$\int \frac{dx}{\sqrt[4]{x^3}} = \int x^{-\frac{3}{4}} dx$$

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$$\int \frac{dx}{\sqrt[4]{x^3}} = \int x^{-\frac{3}{4}} dx = \frac{x^{-\frac{3}{4}+1}}{-\frac{3}{4}+1}$$

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**drugi zadatak**

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## Zadatak 2

Riješite neodređeni integral  $\int \frac{(x - 3)^2}{x^5} dx$ .

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## Rješenje

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## **treći zadatak**

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### Zadatak 3

Riješite neodređeni integral  $\int (5e^x - 3 \sin x) dx$ .

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### Rješenje

$$\int (5e^x - 3 \sin x) dx =$$

$$\int e^x dx = e^x + C$$

$$\int \sin x dx = -\cos x + C$$

### Zadatak 3

Riješite neodređeni integral  $\int (5e^x - 3 \sin x) dx$ .

### Rješenje

$$\int (5e^x - 3 \sin x) dx = 5 \int e^x dx$$

$$\int e^x dx = e^x + C$$

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### Zadatak 3

Riješite neodređeni integral  $\int (5e^x - 3 \sin x) dx$ .

### Rješenje

$$\begin{aligned}\int (5e^x - 3 \sin x) dx &= 5 \int e^x dx - 3 \int \sin x dx = \\ &= 5\end{aligned}$$

$$\int e^x dx = e^x + C$$

$$\int \sin x dx = -\cos x + C$$

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$$\begin{aligned}\int (5e^x - 3 \sin x) dx &= 5 \int e^x dx - 3 \int \sin x dx = \\ &= 5e^x - 3 \cdot\end{aligned}$$

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### Rješenje

$$\begin{aligned}\int (5e^x - 3 \sin x) dx &= 5 \int e^x dx - 3 \int \sin x dx = \\ &= 5e^x - 3 \cdot (-\cos x)\end{aligned}$$

$$\int e^x dx = e^x + C$$

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$$\begin{aligned}\int (5e^x - 3 \sin x) dx &= 5 \int e^x dx - 3 \int \sin x dx = \\ &= 5e^x - 3 \cdot (-\cos x) + C = \\ &= 5e^x + 3 \cos x + C\end{aligned}$$

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$$\int e^x dx = e^x + C$$

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## čtvrti zadatak

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## Zadatak 4

Riješite neodređeni integral  $\int 3^x e^x dx$ .

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Riješite neodređeni integral  $\int 3^x e^x dx$ .

## Rješenje

$$\int 3^x e^x dx =$$

$$(ab)^n = a^n b^n$$

## Zadatak 4

Riješite neodređeni integral  $\int 3^x e^x dx$ .

## Rješenje

$$\int 3^x e^x dx = \int (3e)^x dx$$

$$(ab)^n = a^n b^n$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 4

Riješite neodređeni integral  $\int 3^x e^x dx$ .

## Rješenje

$$\int 3^x e^x dx = \int (3e)^x dx = \frac{(3e)^x}{\ln(3e)}$$

$$(ab)^n = a^n b^n$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 4

Riješite neodređeni integral  $\int 3^x e^x dx$ .

## Rješenje

$$\int 3^x e^x dx = \int (3e)^x dx = \frac{(3e)^x}{\ln(3e)} + C$$

$$(ab)^n = a^n b^n$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 4

Riješite neodređeni integral  $\int 3^x e^x dx$ .

## Rješenje

$$\int 3^x e^x dx = \int (3e)^x dx = \frac{(3e)^x}{\ln(3e)} + C, \quad C \in \mathbb{R}$$

$$(ab)^n = a^n b^n$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$



**peti zadatak**

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## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx =$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx = \int \text{_____} dx$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx = \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx = \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx = \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \quad \quad \quad \right) dx \end{aligned}$$



## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} \right) dx \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \right) dx \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} \end{aligned}$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} = \\ &= \end{aligned}$$

$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$



## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} = \\ &= -\operatorname{ctg} x \end{aligned}$$

$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} = \\ &= -\operatorname{ctg} x - \end{aligned}$$

$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} = \\ &= -\operatorname{ctg} x - \operatorname{tg} x \end{aligned}$$

$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} = \\ &= -\operatorname{ctg} x - \operatorname{tg} x + C \end{aligned}$$

$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$

## Zadatak 5

Riješite neodređeni integral  $\int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx$ .

## Rješenje

$$\begin{aligned} \int \frac{\cos 2x}{\cos^2 x \sin^2 x} dx &= \int \frac{\cos^2 x - \sin^2 x}{\cos^2 x \sin^2 x} dx = \\ &= \int \left( \frac{1}{\sin^2 x} - \frac{1}{\cos^2 x} \right) dx = \int \frac{dx}{\sin^2 x} - \int \frac{dx}{\cos^2 x} = \\ &= -\operatorname{ctg} x - \operatorname{tg} x + C, \quad C \in \mathbb{R} \end{aligned}$$

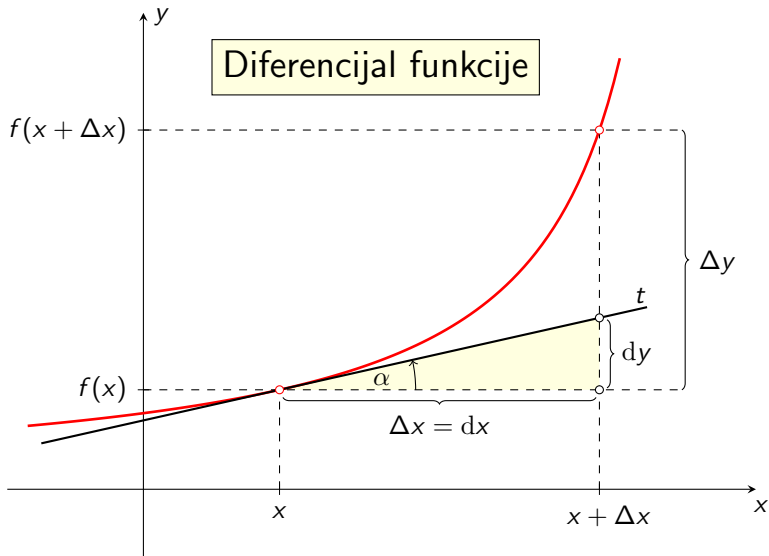
$$\int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C$$

$$\int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C$$

# Diferencijal realne funkcije jedne realne varijable

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## Diferencijal funkcije



$$y = f(x), \quad f'(x) = \operatorname{tg} \alpha = \frac{dy}{dx}, \quad dy = f'(x) dx$$

# šesti zadatak

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## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx =$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \end{array} \right.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ 3 - 2x = t \right]'$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned} t &= f(x) \\ dt &= f'(x) dx \end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 \end{array} \right]'$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx \end{array} \right]$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t /' \\ -2 dx = \end{array} \right.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right]$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$



## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right]$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\int (3 - 2x)^8 dx = \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{array}{l} t = f(x) \\ dt = f'(x) dx \end{array}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned} \int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt \end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned} t &= f(x) \\ dt &= f'(x) dx \end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned} \int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned} t &= f(x) \\ dt &= f'(x) dx \end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned} \int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} \end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned} t &= f(x) \\ dt &= f'(x) dx \end{aligned}$$



## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned} \int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} + C \end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned} t &= f(x) \\ dt &= f'(x) dx \end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned}\int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} + C = -\frac{1}{18} t^9 + C\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}t &= f(x) \\ dt &= f'(x) dx\end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned}\int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} + C = -\frac{1}{18} t^9 + C = \\ &= -\frac{1}{18} (3 - 2x)^9 + C\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}t &= f(x) \\ dt &= f'(x) dx\end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned}\int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} + C = -\frac{1}{18} t^9 + C = \\ &= -\frac{1}{18} (3 - 2x)^9\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}t &= f(x) \\ dt &= f'(x) dx\end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned}\int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} + C = -\frac{1}{18} t^9 + C = \\ &= -\frac{1}{18} (3 - 2x)^9 + C\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}t &= f(x) \\ dt &= f'(x) dx\end{aligned}$$

## Zadatak 6

Riješite neodređeni integral  $\int (3 - 2x)^8 dx$ .

$$dx = \frac{dt}{-2}$$

## Rješenje

$$\begin{aligned}\int (3 - 2x)^8 dx &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int t^8 \cdot \frac{dt}{-2} = \\ &= -\frac{1}{2} \int t^8 dt = -\frac{1}{2} \cdot \frac{t^9}{9} + C = -\frac{1}{18} t^9 + C = \\ &= -\frac{1}{18} (3 - 2x)^9 + C, \quad C \in \mathbb{R}\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}t &= f(x) \\ dt &= f'(x) dx\end{aligned}$$

# sedmi zadatak

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## Zadatak 7

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .



## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .

## Rješenje

$$\int \sqrt[4]{(x-2)^3} dx =$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .

## Rješenje

$$\int \sqrt[4]{(x-2)^3} dx = \int (x-2)^{\frac{3}{4}} dx$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .

## Rješenje

$$\int \sqrt[4]{(x-2)^3} dx = \int (x-2)^{\frac{3}{4}} dx = \left[ \right.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .

## Rješenje

$$\int \sqrt[4]{(x-2)^3} dx = \int (x-2)^{\frac{3}{4}} dx = \left[ x-2 = t \right.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .

## Rješenje

$$\int \sqrt[4]{(x-2)^3} dx = \int (x-2)^{\frac{3}{4}} dx = \left[ x-2 = t \right]'$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Riješite neodređeni integral  $\int \sqrt[4]{(x-2)^3} dx$ .

## Rješenje

$$\int \sqrt[4]{(x-2)^3} dx = \int (x-2)^{\frac{3}{4}} dx = \left[ \begin{array}{l} x-2 = t /' \\ dx \end{array} \right.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 7

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

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$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

# osmi zadatak

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## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

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## Rješenje

$$\int x \cdot 7^{x^2} dx =$$

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## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

## Rješenje

$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t \end{array} \right.$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

## Rješenje

$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t \end{array} \right] /'$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$



## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

## Rješenje

$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t /' \\ 2x \end{array} \right.$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

## Rješenje

$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t \\ 2x dx \end{array} \right]$$

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$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t / ' \\ 2x dx = dt \end{array} \right] = \int$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

## Rješenje

$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t / ' \\ 2x dx = dt \end{array} \right] = \int 7^t$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

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## Rješenje

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$$\int a^x dx = \frac{a^x}{\ln a} + C$$



## Zadatak 8

Riješite neodređeni integral  $\int x \cdot 7^{x^2} dx$ .

$$x dx = \frac{dt}{2}$$

## Rješenje

$$\int x \cdot 7^{x^2} dx = \left[ \begin{array}{l} x^2 = t / ' \\ 2x dx = dt \end{array} \right] = \int 7^t \cdot \frac{dt}{2}$$

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

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$$\int a^x dx = \frac{a^x}{\ln a} + C$$

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$$\int a^x dx = \frac{a^x}{\ln a} + C$$

# deveti zadatak

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## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

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## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} =$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1 - x^2 = t \end{array} \right.$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ 1 - x^2 = t \right]'$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$



## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \end{array} \right]'$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx \end{array} \right]$$

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Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

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$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int \text{---}$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int \frac{1}{\sqrt{t}}$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$



## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

$$x \, dx = -\frac{dt}{2}$$

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int \frac{-\frac{dt}{2}}{\sqrt{t}}$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

$$x \, dx = -\frac{dt}{2}$$

## Rješenje

$$\int \frac{x \, dx}{\sqrt{1-x^2}} = \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int \frac{-\frac{dt}{2}}{\sqrt{t}} = -\frac{1}{2} \int t^{-\frac{1}{2}} \, dt$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

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## Rješenje

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$$= -\frac{1}{2} \cdot$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

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$$x \, dx = -\frac{dt}{2}$$

## Rješenje

$$\begin{aligned} \int \frac{x \, dx}{\sqrt{1-x^2}} &= \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int \frac{-\frac{dt}{2}}{\sqrt{t}} = -\frac{1}{2} \int t^{-\frac{1}{2}} \, dt = \\ &= -\frac{1}{2} \cdot \frac{t^{\frac{1}{2}}}{\frac{1}{2}} \end{aligned}$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$$

## Zadatak 9

Riješite neodređeni integral  $\int \frac{x \, dx}{\sqrt{1-x^2}}$ .

$$x \, dx = -\frac{dt}{2}$$

## Rješenje

$$\begin{aligned} \int \frac{x \, dx}{\sqrt{1-x^2}} &= \left[ \begin{array}{l} 1-x^2 = t \\ -2x \, dx = dt \end{array} \right] = \int \frac{-\frac{dt}{2}}{\sqrt{t}} = -\frac{1}{2} \int t^{-\frac{1}{2}} \, dt = \\ &= -\frac{1}{2} \cdot \frac{t^{\frac{1}{2}}}{\frac{1}{2}} + C \end{aligned}$$

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**deseti zadatak**

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## Zadatak 10

Riješite neodređeni integral  $\int \frac{\sqrt[3]{1 + \ln x}}{x} dx$ .

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## Rješenje

$$\int \frac{\sqrt[3]{1 + \ln x}}{x} dx =$$

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## Zadatak 10

Riješite neodređeni integral  $\int \frac{\sqrt[3]{1 + \ln x}}{x} dx$ .

## Rješenje

$$\int \frac{\sqrt[3]{1 + \ln x}}{x} dx = \left[ \begin{array}{l} 1 + \ln x = t \end{array} \right.$$

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## Zadatak 10

Riješite neodređeni integral  $\int \frac{\sqrt[3]{1 + \ln x}}{x} dx$ .

## Rješenje

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$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$



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Riješite neodređeni integral  $\int \frac{\sqrt[3]{1 + \ln x}}{x} dx$ .

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# Napomena za logaritamsku funkciju

---

# Napomena

$$(\ln |x|)' = \frac{1}{x}, \quad x \neq 0$$

- Ako je  $x > 0$ , tada je  $|x| = x$  pa znamo da vrijedi

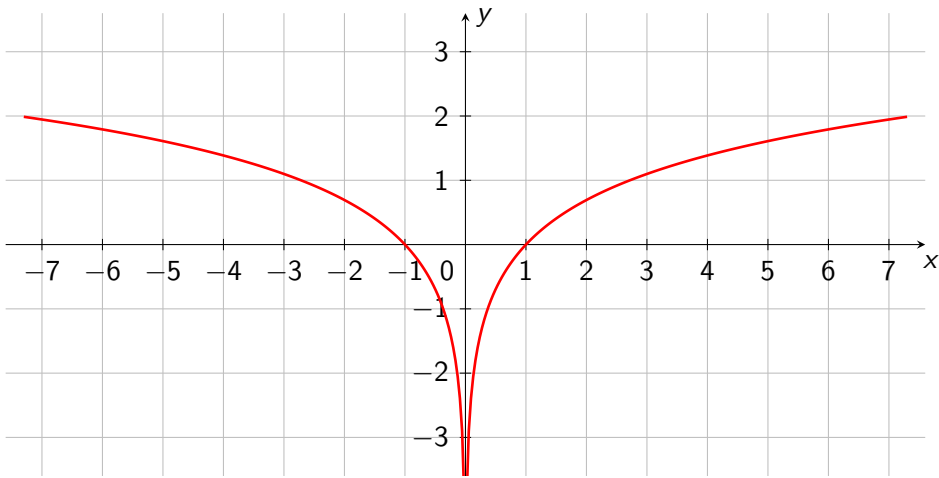
$$(\ln x)' = \frac{1}{x}$$

- Ako je  $x < 0$ , tada je  $|x| = -x$  pa korištenjem pravila za derivaciju složene funkcije ponovo dobivamo

$$(\ln(-x))' = \frac{1}{-x} \cdot (-x)' = \frac{1}{-x} \cdot (-1) = \frac{1}{x}$$



# Graf funkcije $f(x) = \ln |x|$



# **jedanaesti zadatak**

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## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3 - 2x}$ .

## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3 - 2x}$ .

## Rješenje

$$\int \frac{dx}{3 - 2x} =$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln |x| + C$$

## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

## Rješenje

$$\int \frac{dx}{3-2x} = \left[ \begin{array}{l} 3-2x = t \end{array} \right.$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln|x| + C$$

## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

## Rješenje

$$\int \frac{dx}{3-2x} = \left[ 3-2x = t \right]'$$

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## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

## Rješenje

$$\int \frac{dx}{3-2x} = \left[ \begin{array}{l} 3-2x = t \\ -2 \end{array} \right]'$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln|x| + C$$

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Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

## Rješenje

$$\int \frac{dx}{3-2x} = \left[ \begin{array}{l} 3-2x = t \\ -2 dx \end{array} \right]$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

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Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

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$$\int \frac{dx}{3-2x} = \left[ \begin{array}{l} 3-2x = t /' \\ -2 dx = \end{array} \right.$$

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$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

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Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

## Rješenje

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$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

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## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

## Rješenje

$$\int \frac{dx}{3-2x} = \left[ \begin{array}{l} 3-2x = t \\ -2 dx = dt \end{array} \right] = \int \frac{1}{t}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln|x| + C$$

## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

### Rješenje

$$dx = \frac{dt}{-2}$$

$$\int \frac{dx}{3-2x} = \left[ \begin{array}{l} 3-2x = t \\ -2 dx = dt \end{array} \right] = \int \frac{\frac{dt}{-2}}{t}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln|x| + C$$

## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

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## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

### Rješenje

$$\boxed{dx = \frac{dt}{-2}}$$

$$\begin{aligned} \int \frac{dx}{3-2x} &= \left[ \begin{array}{l} 3-2x = t \\ -2 dx = dt \end{array} \right] = \int \frac{\frac{dt}{-2}}{t} = -\frac{1}{2} \int \frac{dt}{t} = \\ &= -\frac{1}{2} \end{aligned}$$

$$\boxed{\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1}$$

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## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

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$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

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$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln |x| + C$$

## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

### Rješenje

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## Zadatak 11

Riješite neodređeni integral  $\int \frac{dx}{3-2x}$ .

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$$\boxed{\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1}$$

$$\boxed{\int \frac{dx}{x} = \ln |x| + C}$$

## Zadatak 11

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

Riješite neodređeni integral  $\int \frac{dx}{3 - 2x}$ .

## Rješenje

$$dx = \frac{dt}{-2}$$

$$\begin{aligned} \int \frac{dx}{3 - 2x} &= \left[ \begin{array}{l} 3 - 2x = t \\ -2 dx = dt \end{array} \right] = \int \frac{\frac{dt}{-2}}{t} = -\frac{1}{2} \int \frac{dt}{t} = \\ &= -\frac{1}{2} \ln |t| + C = -\frac{1}{2} \ln |3 - 2x| + C, \quad C \in \mathbb{R} \end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{dx}{x} = \ln |x| + C$$

# **dvanaesti zadatak**

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## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx =$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx = \int \frac{-3x + 1}{2x + 3} dx =$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx = \int \frac{-3x + 1}{2x + 3} dx =$$

$$(-3x + 1) : (2x + 3) =$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx = \int \frac{-3x + 1}{2x + 3} dx =$$

$$(-3x + 1) : (2x + 3) = -\frac{3}{2}$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx = \int \frac{-3x + 1}{2x + 3} dx =$$

$$\begin{aligned} (-3x + 1) : (2x + 3) &= -\frac{3}{2} \\ &+ \frac{9}{2} \end{aligned}$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx = \int \frac{-3x + 1}{2x + 3} dx =$$

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$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

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$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \end{array}$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$



## Zadatak 12

Riješite neodređeni integral  $\int \frac{1 - 3x}{3 + 2x} dx$ .

## Rješenje

$$\int \frac{1 - 3x}{3 + 2x} dx = \int \frac{-3x + 1}{2x + 3} dx =$$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ 3x + \frac{9}{2} \\ \hline \frac{11}{2} \end{array}$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx =$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx =$$

$$\begin{array}{r} (-3x+1) : (2x+3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

**Rješenje**  $P_1(x) = P_2(x)Q(x) + R(x)$

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx =$$

$$\begin{array}{r} (-3x+1) : (2x+3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (pointing to  $-\frac{3}{2}$ )  
 $R(x)$  (pointing to  $\frac{11}{2}$ )

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje  $P_1(x) = P_2(x)Q(x) + R(x)$

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx =$$

$$(-3x+1) : (2x+3) = -\frac{3}{2}$$
$$\frac{3x + \frac{9}{2}}{2x+3} = Q(x)$$
$$\frac{11}{2} = R(x)$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje  $P_1(x) = P_2(x)Q(x) + R(x)$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (indicated by a blue arrow pointing to the quotient  $-\frac{3}{2}$ )  
 $R(x)$  (indicated by a blue arrow pointing to the remainder  $\frac{11}{2}$ )

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left($$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

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$Q(x)$  (indicated by a blue arrow pointing to  $-\frac{3}{2}$ )  
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$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

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## Zadatak 12

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Rješenje  $P_1(x) = P_2(x)Q(x) + R(x)$

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$Q(x)$  (indicated by a blue arrow pointing to  $-\frac{3}{2}$ )  
 $R(x)$  (indicated by a blue arrow pointing to  $\frac{11}{2}$ )

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\quad}{2x+3} \right) dx$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

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 $R(x)$  (indicated by a blue arrow pointing to  $\frac{11}{2}$ )

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx$$

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$Q(x)$  (pointing to  $-\frac{3}{2}$ )  
 $R(x)$  (pointing to  $\frac{11}{2}$ )

$$\begin{aligned} \int \frac{1-3x}{3+2x} dx &= \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx = \\ &= -\frac{3}{2} \int dx \end{aligned}$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

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## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje  $P_1(x) = P_2(x)Q(x) + R(x)$

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$Q(x)$  (indicated by a blue arrow pointing to  $-\frac{3}{2}$ )  
 $R(x)$  (indicated by a blue arrow pointing to  $\frac{11}{2}$ )

$$\begin{aligned} \int \frac{1-3x}{3+2x} dx &= \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx = \\ &= -\frac{3}{2} \int dx + \end{aligned}$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje  $P_1(x) = P_2(x)Q(x) + R(x)$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (indicated by a blue arrow pointing to the quotient)

$R(x)$  (indicated by a blue arrow pointing to the remainder)

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx =$$

$$= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3}$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$



## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (indicated by a blue arrow pointing to  $-\frac{3}{2}$ )  
 $R(x)$  (indicated by a blue arrow pointing to  $\frac{11}{2}$ )

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx =$$

$$= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3} = -\frac{3}{2}x$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

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$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (pointing to  $-\frac{3}{2}$ )  
 $R(x)$  (pointing to  $\frac{11}{2}$ )

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx =$$

$$= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3} = -\frac{3}{2}x + \frac{11}{2} \cdot$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje  $P_1(x) = P_2(x)Q(x) + R(x)$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (indicated by a blue arrow pointing to the quotient)

$R(x)$  (indicated by a blue arrow pointing to the remainder)

$$\begin{aligned} \int \frac{1-3x}{3+2x} dx &= \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx = \\ &= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3} = -\frac{3}{2}x + \frac{11}{2} \cdot \frac{1}{2} \ln |2x+3| \end{aligned}$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln |ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (pointed to by a blue arrow from the  $-\frac{3}{2}$  result)  
 $R(x)$  (pointed to by a blue arrow from the  $\frac{11}{2}$  remainder)

$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx =$$

$$= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3} = -\frac{3}{2}x + \frac{11}{2} \cdot \frac{1}{2} \ln|2x+3| + C$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln|ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

$$P_1(x) = P_2(x)Q(x) + R(x)$$

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$Q(x)$  (indicated by a blue arrow pointing to the quotient)

$R(x)$  (indicated by a blue arrow pointing to the remainder)

$$\begin{aligned} \int \frac{1-3x}{3+2x} dx &= \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx = \\ &= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3} = -\frac{3}{2}x + \frac{11}{2} \cdot \frac{1}{2} \ln|2x+3| + C = \\ &= -\frac{3}{2}x + \frac{11}{4} \ln|2x+3| + C \end{aligned}$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln|ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

## Zadatak 12

Riješite neodređeni integral  $\int \frac{1-3x}{3+2x} dx$ .

Rješenje

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\begin{array}{r} (-3x + 1) : (2x + 3) = -\frac{3}{2} \\ \underline{3x + \frac{9}{2}} \\ \frac{11}{2} \end{array}$$

$Q(x)$  (indicated by a blue arrow pointing to  $-\frac{3}{2}$ )  
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$$\int \frac{1-3x}{3+2x} dx = \int \frac{-3x+1}{2x+3} dx = \int \left( -\frac{3}{2} + \frac{\frac{11}{2}}{2x+3} \right) dx =$$

$$= -\frac{3}{2} \int dx + \frac{11}{2} \int \frac{dx}{2x+3} = -\frac{3}{2}x + \frac{11}{2} \cdot \frac{1}{2} \ln|2x+3| + C =$$

$$= -\frac{3}{2}x + \frac{11}{4} \ln|2x+3| + C, \quad C \in \mathbb{R}$$

$$\int \frac{dx}{ax+b} = \frac{1}{a} \ln|ax+b| + C$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

# **trinaesti zadatak**

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## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .



## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) =$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x$$

$$-x^2$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x$$
$$-x^2 - \frac{3}{5}x$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x$$

$$-x^2 - \frac{3}{5}x$$

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## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x$$

$$-x^2 - \frac{3}{5}x$$

---

$$\frac{22}{5}x$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x$$
$$\begin{array}{r} -x^2 - \frac{3}{5}x \\ \hline \frac{22}{5}x - 4 \end{array}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25}$$
$$\begin{array}{r} -x^2 - \frac{3}{5}x \\ \hline \frac{22}{5}x - 4 \end{array}$$



## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$\begin{array}{r} (x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \\ -x^2 - \frac{3}{5}x \\ \hline \frac{22}{5}x - 4 \\ -\frac{22}{5}x \end{array}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$\begin{array}{r} (x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \\ -x^2 - \frac{3}{5}x \\ \hline \frac{22}{5}x - 4 \\ -\frac{22}{5}x - \frac{66}{25} \end{array}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$\begin{array}{r} (x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \\ -x^2 - \frac{3}{5}x \\ \hline \frac{22}{5}x - 4 \\ -\frac{22}{5}x - \frac{66}{25} \\ \hline \end{array}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$\begin{array}{r} (x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \\ -x^2 - \frac{3}{5}x \\ \hline \frac{22}{5}x - 4 \\ -\frac{22}{5}x - \frac{66}{25} \\ \hline -\frac{166}{25} \end{array}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \boxed{\frac{1}{5}x + \frac{22}{25}} \leftarrow \boxed{Q(x)}$$

$$-x^2 - \frac{3}{5}x$$

---

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

---

$$-\frac{166}{25}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

---

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

---

$$R(x) \rightarrow -\frac{166}{25}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

$$\begin{array}{r} \frac{22}{5}x - 4 \\ -\frac{22}{5}x - \frac{66}{25} \\ \hline \end{array}$$

$$R(x) \rightarrow -\frac{166}{25}$$

$$\frac{x^2 + 5x - 4}{5x + 3} =$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

$$R(x) \rightarrow -\frac{166}{25}$$

$$\frac{x^2 + 5x - 4}{5x + 3} = \frac{1}{5}x + \frac{22}{25}$$



## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

$$R(x) \rightarrow -\frac{166}{25}$$

$$\frac{x^2 + 5x - 4}{5x + 3} = \frac{1}{5}x + \frac{22}{25} +$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

$$R(x) \rightarrow -\frac{166}{25}$$

$$\frac{x^2 + 5x - 4}{5x + 3} = \frac{1}{5}x + \frac{22}{25} + \frac{\quad}{5x + 3}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

$$R(x) \rightarrow -\frac{166}{25}$$

$$\frac{x^2 + 5x - 4}{5x + 3} = \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3}$$

## Zadatak 13

Riješite neodređeni integral  $\int \frac{x^2 + 5x - 4}{5x + 3} dx$ .

## Rješenje

$$(x^2 + 5x - 4) : (5x + 3) = \frac{1}{5}x + \frac{22}{25} \leftarrow Q(x)$$

$$-x^2 - \frac{3}{5}x$$

$$P_1(x) = P_2(x)Q(x) + R(x)$$

$$\frac{P_1(x)}{P_2(x)} = Q(x) + \frac{R(x)}{P_2(x)}$$

$$\frac{22}{5}x - 4$$

$$-\frac{22}{5}x - \frac{66}{25}$$

$$R(x) \rightarrow -\frac{166}{25}$$

$$\frac{x^2 + 5x - 4}{5x + 3} = \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3}$$

$$\int \frac{x^2 + 5x - 4}{5x + 3} dx =$$

$$\int \frac{x^2 + 5x - 4}{5x + 3} dx = \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx$$

$$\int \frac{x^2 + 5x - 4}{5x + 3} dx = \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx =$$
$$= \frac{1}{5} \int x dx$$

$$\int \frac{x^2 + 5x - 4}{5x + 3} dx = \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx =$$

$$= \frac{1}{5} \int x dx +$$



$$\int \frac{x^2 + 5x - 4}{5x + 3} dx = \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx =$$
$$= \frac{1}{5} \int x dx + \frac{22}{25} \int dx$$

$$\int \frac{x^2 + 5x - 4}{5x + 3} dx = \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx =$$
$$= \frac{1}{5} \int x dx + \frac{22}{25} \int dx -$$

$$\int \frac{x^2 + 5x - 4}{5x + 3} dx = \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx =$$
$$= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3}$$

$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot \frac{x^2}{2}\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot \frac{x^2}{2} +\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot \frac{x^2}{2} + \frac{22}{25}x\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot \frac{x^2}{2} + \frac{22}{25}x - \frac{166}{25} \cdot\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$



$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot \frac{x^2}{2} + \frac{22}{25}x - \frac{166}{25} \cdot \frac{1}{5} \ln |5x + 3|\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

$$\begin{aligned}\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\ &= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\ &= \frac{1}{5} \cdot \frac{x^2}{2} + \frac{22}{25}x - \frac{166}{25} \cdot \frac{1}{5} \ln |5x + 3| + C\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

$$\begin{aligned}
\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\
&= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\
&= \frac{1}{5} \cdot \frac{x^2}{2} + \frac{22}{25}x - \frac{166}{25} \cdot \frac{1}{5} \ln |5x + 3| + C = \\
&= \frac{1}{10}x^2 + \frac{22}{25}x - \frac{166}{125} \ln |5x + 3| + C
\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

$$\begin{aligned}
\int \frac{x^2 + 5x - 4}{5x + 3} dx &= \int \left( \frac{1}{5}x + \frac{22}{25} + \frac{-\frac{166}{25}}{5x + 3} \right) dx = \\
&= \frac{1}{5} \int x dx + \frac{22}{25} \int dx - \frac{166}{25} \int \frac{dx}{5x + 3} = \\
&= \frac{1}{5} \cdot \frac{x^2}{2} + \frac{22}{25}x - \frac{166}{25} \cdot \frac{1}{5} \ln |5x + 3| + C = \\
&= \frac{1}{10}x^2 + \frac{22}{25}x - \frac{166}{125} \ln |5x + 3| + C, \quad C \in \mathbb{R}
\end{aligned}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

# četrnaesti zadatak

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## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx =$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \text{—————}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$



## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{\quad}{x + \cos x}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{(x + \cos x)'}{x + \cos x}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{(x + \cos x)'}{x + \cos x} dx$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{(x + \cos x)'}{x + \cos x} dx = \ln |x + \cos x|$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{(x + \cos x)'}{x + \cos x} dx = \ln |x + \cos x| + C$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 14

Riješite neodređeni integral  $\int \frac{1 - \sin x}{x + \cos x} dx$ .

## Rješenje

$$\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{(x + \cos x)'}{x + \cos x} dx = \ln |x + \cos x| + C, \quad C \in \mathbb{R}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

# **petnaesti zadatak**

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## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .



## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} =$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \int \text{—————}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \int \frac{1}{e^x + 2}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \int \frac{(e^x + 2) - e^x}{e^x + 2}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left( 1 \right.$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$



## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left( 1 - \right.$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left( 1 - \frac{e^x}{e^x + 2} \right)$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\int \frac{dx}{e^x + 2} = \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left( 1 - \frac{e^x}{e^x + 2} \right) dx$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \quad \quad \quad \right)\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx \right)\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

## Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \right)\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right)\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2} x\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$



## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2} x -\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \text{————}\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

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Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{1}{e^x + 2}\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2}\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

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$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2} dx\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

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Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

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$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2} dx = \\ &= \frac{1}{2}x\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2} dx = \\ &= \frac{1}{2}x -\end{aligned}$$

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Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

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$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2} dx = \\ &= \frac{1}{2}x - \frac{1}{2}\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$



## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2} dx = \\ &= \frac{1}{2}x - \frac{1}{2} \ln(e^x + 2)\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

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$$\begin{aligned}\int \frac{dx}{e^x + 2} &= \frac{1}{2} \int \frac{(e^x + 2) - e^x}{e^x + 2} dx = \frac{1}{2} \int \left(1 - \frac{e^x}{e^x + 2}\right) dx = \\ &= \frac{1}{2} \cdot \left( \int dx - \int \frac{e^x}{e^x + 2} dx \right) = \frac{1}{2}x - \frac{1}{2} \int \frac{(e^x + 2)'}{e^x + 2} dx = \\ &= \frac{1}{2}x - \frac{1}{2} \ln(e^x + 2) + C\end{aligned}$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

## Zadatak 15

Riješite neodređeni integral  $\int \frac{dx}{e^x + 2}$ .

### Rješenje

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$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

# šesnaesti zadatak

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## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

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## Rješenje

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## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx$$

## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \cos x = t \right.$$



## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \quad \quad \quad \cos x = t \quad \right]'$$

## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t /' \\ - \sin x \end{array} \right.$$

## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

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$$= \int \text{---}$$

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Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ - \sin x \, dx = dt \end{array} \right] =$$
$$= \int \frac{1}{t}$$

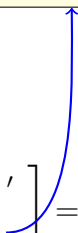


## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ - \sin x \, dx = dt \end{array} \right] =$$
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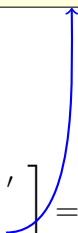
$$\sin x \, dx = -dt$$


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Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ - \sin x \, dx = dt \end{array} \right] =$$
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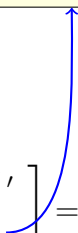
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$$\begin{aligned} \int \operatorname{tg} x \, dx &= \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ -\sin x \, dx = dt \end{array} \right] = \\ &= \int \frac{-dt}{t} = - \int \frac{dt}{t} = -\ln |t| \end{aligned}$$

$$\sin x \, dx = -dt$$

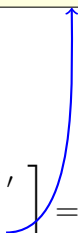
$$\int \frac{dx}{x} = \ln |x| + C$$

## Zadatak 16

Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

## Rješenje

$$\int \operatorname{tg} x \, dx = \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ -\sin x \, dx = dt \end{array} \right] =$$
$$= \int \frac{-dt}{t} = - \int \frac{dt}{t} = -\ln |t| + C$$

$$\sin x \, dx = -dt$$


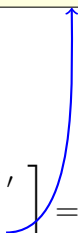
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Riješite neodređeni integral  $\int \operatorname{tg} x \, dx$ .

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$$\begin{aligned} \int \operatorname{tg} x \, dx &= \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ -\sin x \, dx = dt \end{array} \right] = \\ &= \int \frac{-dt}{t} = - \int \frac{dt}{t} = -\ln |t| + C = -\ln |\cos x| \end{aligned}$$

$$\sin x \, dx = -dt$$



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$$\sin x \, dx = -dt$$


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$$\begin{aligned} \int \operatorname{tg} x \, dx &= \int \frac{\sin x}{\cos x} \, dx = \left[ \begin{array}{l} \cos x = t / ' \\ -\sin x \, dx = dt \end{array} \right] = \\ &= \int \frac{-dt}{t} = - \int \frac{dt}{t} = -\ln |t| + C = -\ln |\cos x| + C, \quad C \in \mathbb{R} \end{aligned}$$

$$\sin x \, dx = -dt$$

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**sedamnaesti zadatak**

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## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Rješenje

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} dx =$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Rješenje

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} dx = \left[ \begin{array}{l} 1 + 2 \cos x = t \end{array} \right.$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Rješenje

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} dx = \left[ 1 + 2 \cos x = t \right]'$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Rješenje

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} dx = \left[ \begin{array}{l} 1 + 2 \cos x = t /' \\ - 2 \sin x \end{array} \right.$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Rješenje

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} dx = \left[ \begin{array}{l} 1 + 2 \cos x = t /' \\ - 2 \sin x dx \end{array} \right.$$

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## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

## Rješenje

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} dx = \left[ \begin{array}{l} 1 + 2 \cos x = t /' \\ - 2 \sin x dx = dt \end{array} \right] = \int \frac{1}{\sqrt{t}}$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

### Rješenje

$$\sin x \, dx = -\frac{dt}{2}$$

$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} \, dx = \left[ \begin{array}{l} 1 + 2 \cos x = t \\ -2 \sin x \, dx = dt \end{array} \right] = \int \frac{-\frac{dt}{2}}{\sqrt{t}}$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

### Rješenje

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$$\int \frac{\sin x}{\sqrt{1 + 2 \cos x}} \, dx = \left[ \begin{array}{l} 1 + 2 \cos x = t \\ -2 \sin x \, dx = dt \end{array} \right] = \int \frac{-\frac{dt}{2}}{\sqrt{t}} =$$

$$= -\frac{1}{2} \int \frac{dt}{\sqrt{t}}$$

## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

### Rješenje

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## Zadatak 17

Odredite primitivnu funkciju  $g$  funkcije  $f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$  za koju je  $g(0) = 1$ .

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$$= -\sqrt{1 + 2 \cos x} + C, \quad C \in \mathbb{R}$$

$$f(x) = \frac{\sin x}{\sqrt{1 + 2 \cos x}}$$

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$$g(x) = -\sqrt{1 + 2 \cos x} + \sqrt{3} + 1$$



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