

# Derivacija funkcije – 1. dio

MATEMATIKA 2

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# Sadržaj

prvi zadatak

drugi zadatak

treći zadatak

četvrti zadatak

peti zadatak

šesti zadatak

sedmi zadatak

osmi zadatak

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deseti zadatak

jedanaesti zadatak

dvanaesti zadatak

trinaesti zadatak

četрнаesti zadatak

petnaesti zadatak

**prvi zadatak**

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## Zadatak 1

Odredite derivacije funkcija  $f(x) = \sqrt[5]{x^2}$  i  $g(x) = \left(\frac{2}{5}\right)^x$ .

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$$g(x) = \left(\frac{2}{5}\right)^x \quad g'(x) = \left(\frac{2}{5}\right)^x \ln \frac{2}{5}$$

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**drugi zadatak**

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## Zadatak 2

Odredite derivaciju funkcije  $f(x) = \frac{3}{5}x^3 - \frac{7}{5}x^2 + \frac{9}{5}x + \frac{4}{5}$ .

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$$f'(x) = \left( \frac{3}{5}x^3 - \frac{7}{5}x^2 + \frac{9}{5}x + \frac{4}{5} \right)'$$

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## treći zadatak

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### Zadatak 3

Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

### Zadatak 3

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

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### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}}$$

### Zadatak 3

Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}}$$

$$\frac{x^n}{x^m} = x^{n-m}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$



### Zadatak 3

$$\frac{x^n}{x^m} = x^{n-m}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

### Zadatak 3

$$\frac{x^n}{x^m} = x^{n-m}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

$$y = \frac{4}{3}x^{\frac{10}{7}}$$

### Zadatak 3

$$\frac{x^n}{x^m} = x^{n-m}$$

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Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

$$(cu)'(x) = c \cdot u'(x)$$

### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

$$y = \frac{4}{3}x^{\frac{10}{7}}$$

$$y' =$$

### Zadatak 3

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$$y = \frac{4}{3}x^{\frac{10}{7}}$$

$$y' = \frac{4}{3} \cdot$$

### Zadatak 3

Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

$$y = \frac{4}{3}x^{\frac{10}{7}}$$

$$y' = \frac{4}{3} \cdot \left(x^{\frac{10}{7}}\right)'$$

$$\frac{x^n}{x^m} = x^{n-m}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(x^n)' = nx^{n-1}$$

### Zadatak 3

Odredite derivaciju funkcije  $y = \frac{4x^2}{3\sqrt[7]{x^4}}$ .

### Rješenje

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

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$$y' = \frac{4}{3} \cdot \left(x^{\frac{10}{7}}\right)' = \frac{4}{3} \cdot$$

$$\frac{x^n}{x^m} = x^{n-m}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

$$(cu)'(x) = c \cdot u'(x)$$

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$$\frac{x^n}{x^m} = x^{n-m}$$

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### Rješenje

$$(x^n)' = nx^{n-1}$$

$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

$$y = \frac{4}{3}x^{\frac{10}{7}}$$

$$y' = \frac{4}{3} \cdot \left(x^{\frac{10}{7}}\right)' = \frac{4}{3} \cdot \frac{10}{7}x^{\frac{10}{7}-1}$$

### Zadatak 3

$$\frac{x^n}{x^m} = x^{n-m}$$

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$$y = \frac{4}{3}x^{\frac{10}{7}}$$

$$y' = \frac{4}{3} \cdot \left(x^{\frac{10}{7}}\right)' = \frac{4}{3} \cdot \frac{10}{7}x^{\frac{10}{7}-1}$$

$$y' = \frac{40}{21}x^{\frac{3}{7}}$$



### Zadatak 3

$$\frac{x^n}{x^m} = x^{n-m}$$

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$$y = \frac{4x^2}{3\sqrt[7]{x^4}} = \frac{4x^2}{3x^{\frac{4}{7}}} = \frac{4}{3}x^{2-\frac{4}{7}}$$

$$y = \frac{4}{3}x^{\frac{10}{7}}$$

$$y' = \frac{4}{3} \cdot \left(x^{\frac{10}{7}}\right)' = \frac{4}{3} \cdot \frac{10}{7}x^{\frac{10}{7}-1}$$

$$y' = \frac{40}{21}x^{\frac{3}{7}} = \frac{40}{21}\sqrt[7]{x^3}$$

# čtvrti zadatak

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## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' =$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)'$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)' \cdot e^x$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)' \cdot e^x +$$



$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)' \cdot e^x + x$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)' \cdot e^x + x \cdot$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

### Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

### Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1 \cdot e^x$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

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$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1 \cdot e^x + x$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

$$(e^x)' = e^x$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1 \cdot e^x + x \cdot e^x$$



$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

$$(e^x)' = e^x$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1 \cdot e^x + x \cdot e^x$$

$$y' = (1 + x)e^x$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

$$(e^x)' = e^x$$

## Zadatak 4

Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1 \cdot e^x + x \cdot e^x$$

$$y' = (1 + x)e^x$$

$$y'(0) = (1 + 0) \cdot e^0$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

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$$y'(0) = (1 + 0) \cdot e^0$$

$$y'(0) = 1 \cdot 1$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$(x^n)' = nx^{n-1}$$

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Odredite derivaciju funkcije  $y = xe^x$  u točki 0.

## Rješenje

$$y' = (x)' \cdot e^x + x \cdot (e^x)'$$

$$y' = 1 \cdot e^x + x \cdot e^x$$

$$y' = (1 + x)e^x$$

$$y'(0) = (1 + 0) \cdot e^0$$

$$y'(0) = 1 \cdot 1$$

$$y'(0) = 1$$

**peti zadatak**

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## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \underline{\hspace{15cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \frac{\quad}{(x^3 + 5)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \frac{(x^3 - 5)'}{(x^3 + 5)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \frac{(x^3 - 5)' \cdot (x^3 + 5)}{(x^3 + 5)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$y' = \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5)}{(x^3 + 5)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 5

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## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

### Rješenje

$$y' = \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} =$$
  
$$= \underline{\hspace{10cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



$$(u - v)'(x) = u'(x) - v'(x)$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned} y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\ &= \frac{\quad}{(x^3 + 5)^2} \end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned} y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\ &= \frac{3x^2}{(x^3 + 5)^2} \end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

$$(c)' = 0$$

$$(u - v)'(x) = u'(x) - v'(x)$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned} y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\ &= \frac{3x^2 \cdot (x^3 + 5)}{(x^3 + 5)^2} \end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

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$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

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$$(u - v)'(x) = u'(x) - v'(x)$$

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$$\begin{aligned} y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\ &= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5)}{(x^3 + 5)^2} \end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

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## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\ &= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2}\end{aligned}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

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## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\ &= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2}\end{aligned}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

$$(c)' = 0$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \underline{\hspace{10em}}\end{aligned}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

$$(c)' = 0$$



## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \frac{\quad}{(x^3 + 5)^2}\end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

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$$(x^n)' = nx^{n-1}$$

$$(c)' = 0$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \frac{3x^5}{(x^3 + 5)^2}\end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(x^n)' = nx^{n-1}$$

$$(c)' = 0$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \frac{3x^5 + 15x^2}{(x^3 + 5)^2}\end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(u - v)'(x) = u'(x) - v'(x)$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(x^n)' = nx^{n-1}$$

$$(c)' = 0$$

## Zadatak 5

Odredite derivaciju funkcije  $y = \frac{x^3 - 5}{x^3 + 5}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \frac{3x^5 + 15x^2 - 3x^5}{(x^3 + 5)^2}\end{aligned}$$

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$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \frac{3x^5 + 15x^2 - 3x^5 + 15x^2}{(x^3 + 5)^2}\end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$\begin{aligned}y' &= \frac{(x^3 - 5)' \cdot (x^3 + 5) - (x^3 - 5) \cdot (x^3 + 5)'}{(x^3 + 5)^2} = \\&= \frac{3x^2 \cdot (x^3 + 5) - (x^3 - 5) \cdot 3x^2}{(x^3 + 5)^2} = \\&= \frac{3x^5 + 15x^2 - 3x^5 + 15x^2}{(x^3 + 5)^2} = \frac{30x^2}{(x^3 + 5)^2}\end{aligned}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(x^n)' = nx^{n-1}$$

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# šesti zadatak

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## Zadatak 6

Odredite derivaciju funkcije  $y = \sqrt[3]{x} \log_2 x$ .



## Zadatak 6

Odredite derivaciju funkcije  $y = \sqrt[3]{x} \log_2 x$ .

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

## Rješenje

$$y' = (\sqrt[3]{x} \log_2 x)'$$

## Zadatak 6

Odredite derivaciju funkcije  $y = \sqrt[3]{x} \log_2 x$ .

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

## Rješenje

$$y' = (\sqrt[3]{x} \log_2 x)' = \left(x^{\frac{1}{3}} \log_2 x\right)'$$

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$$\frac{x^m}{x^n} = x^{m-n}$$

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# sedmi zadatak

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## Zadatak 7

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

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## Rješenje

$$y' = \text{_____}$$

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## Zadatak 7

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{\quad}{(\ln x - 1)^2}$$

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## Zadatak 7

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)'}{(\ln x - 1)^2}$$

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= \_\_\_\_\_

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$$= \frac{\frac{1}{x}}{(\ln x - 1)^2}$$

$$(c)' = 0$$

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Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot 0}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1)}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot 0}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

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$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$= \frac{\quad}{(\ln x - 1)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \ln x}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \ln x - \frac{1}{x}}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \ln x - \frac{1}{x} - \frac{1}{x} \ln x}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \ln x - \frac{1}{x} - \frac{1}{x} \ln x - \frac{1}{x}}{(\ln x - 1)^2}$$

$$(c)' = 0$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$(c)' = 0$$

$$= \frac{\frac{1}{x} \ln x - \frac{1}{x} - \frac{1}{x} \ln x - \frac{1}{x}}{(\ln x - 1)^2} = \frac{-\frac{2}{x}}{(\ln x - 1)^2}$$

$$(\ln x)' = \frac{1}{x}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



## Zadatak 7

$$(u + v)'(x) = u'(x) + v'(x)$$

Odredite derivaciju funkcije  $y = \frac{\ln x + 1}{\ln x - 1}$ .

## Rješenje

$$y' = \frac{(\ln x + 1)' \cdot (\ln x - 1) - (\ln x + 1) \cdot (\ln x - 1)'}{(\ln x - 1)^2} =$$

$$= \frac{\frac{1}{x} \cdot (\ln x - 1) - (\ln x + 1) \cdot \frac{1}{x}}{(\ln x - 1)^2} =$$

$$(c)' = 0$$

$$= \frac{\frac{1}{x} \ln x - \frac{1}{x} - \frac{1}{x} \ln x - \frac{1}{x}}{(\ln x - 1)^2} = \frac{-\frac{2}{x}}{(\ln x - 1)^2} =$$

$$(\ln x)' = \frac{1}{x}$$

$$= \frac{-2}{x(\ln x - 1)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

# osmi zadatak

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## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$y' = (10^x \log x + \ln 10)'$$

$$(u + v)'(x) = u'(x) + v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$y' = (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)'$$

$$(u + v)'(x) = u'(x) + v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)'\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot \log x\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$



## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot \log x +\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot \log x + 10^x\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot \log x + 10^x \cdot\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot \log x + 10^x \cdot (\log x)'\end{aligned}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\ &= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0\end{aligned}$$

$$(c)' = 0$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10 \cdot \log x\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10 \cdot \log x +\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$



## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10 \cdot \log x + 10^x\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10 \cdot \log x + 10^x \cdot\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

## Rješenje

$$y' = (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' =$$

$$= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 =$$

$$= 10^x \ln 10 \cdot \log x + 10^x \cdot \frac{1}{x \ln 10}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

### Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10 \cdot \log x + 10^x \cdot \frac{1}{x \ln 10} = \\&= \left( \phantom{10^x \ln 10 \cdot \log x + 10^x \cdot \frac{1}{x \ln 10}} \right) 10^x\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

### Rješenje

$$y' = (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' =$$

$$= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 =$$

$$= 10^x \ln 10 \cdot \log x + 10^x \cdot \frac{1}{x \ln 10} =$$

$$= \left( \ln 10 \log x \quad \right) 10^x$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

### Rješenje

$$y' = (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' =$$

$$= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 =$$

$$= 10^x \ln 10 \cdot \log x + 10^x \cdot \frac{1}{x \ln 10} =$$

$$= \left( \ln 10 \log x + \frac{1}{x} \right) 10^x$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

## Zadatak 8

Odredite derivaciju funkcije  $y = 10^x \log x + \ln 10$ .

### Rješenje

$$\begin{aligned}y' &= (10^x \log x + \ln 10)' = (10^x \log x)' + (\ln 10)' = \\&= (10^x)' \cdot \log x + 10^x \cdot (\log x)' + 0 = \\&= 10^x \ln 10 \cdot \log x + 10^x \cdot \frac{1}{x \ln 10} = \\&= \left( \ln 10 \log x + \frac{1}{x \ln 10} \right) 10^x\end{aligned}$$

$$(c)' = 0$$

$$(a^x)' = a^x \ln a$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(u + v)'(x) = u'(x) + v'(x)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

# deveti zadatak

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## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' =$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' = e^{\sqrt{x}}$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' = e^{\sqrt{x}} \cdot \frac{1}{2\sqrt{x}}.$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' = e^{\sqrt{x}} \cdot (\sqrt{x})'$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' = e^{\sqrt{x}} \cdot (\sqrt{x})' = e^{\sqrt{x}}$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' = e^{\sqrt{x}} \cdot (\sqrt{x})' = e^{\sqrt{x}} \cdot \frac{1}{2\sqrt{x}}$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Zadatak 9

Odredite derivaciju funkcije  $y = e^{\sqrt{x}}$ .

## Rješenje

$$y' = e^{\sqrt{x}} \cdot (\sqrt{x})' = e^{\sqrt{x}} \cdot \frac{1}{2\sqrt{x}}$$

$$y' = \frac{e^{\sqrt{x}}}{2\sqrt{x}}$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$



**deseti zadatak**

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## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$y' =$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$y' = 20(x^2 + 3x - 5)^{19}$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$y' = 20 (x^2 + 3x - 5)^{19} .$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$y' = 20 (x^2 + 3x - 5)^{19} \cdot (x^2 + 3x - 5)'$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$\begin{aligned}y' &= 20 (x^2 + 3x - 5)^{19} \cdot (x^2 + 3x - 5)' = \\ &= 20 (x^2 + 3x - 5)^{19}\end{aligned}$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$\begin{aligned}y' &= 20 (x^2 + 3x - 5)^{19} \cdot (x^2 + 3x - 5)' = \\ &= 20 (x^2 + 3x - 5)^{19} (2x\end{aligned}$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$



## Zadatak 10

Odredite derivaciju funkcije  $y = (x^2 + 3x - 5)^{20}$ .

## Rješenje

$$\begin{aligned}y' &= 20 (x^2 + 3x - 5)^{19} \cdot (x^2 + 3x - 5)' = \\ &= 20 (x^2 + 3x - 5)^{19} (2x + 3)\end{aligned}$$

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

# **jedanaesti zadatak**

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## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' =$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5}$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

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## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5} \cdot (5^x - x^5)'$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5} \cdot (5^x - x^5)' = \text{—————}$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$



$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5} \cdot (5^x - x^5)' = \frac{1}{(5^x - x^5) \ln 5}$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5} \cdot (5^x - x^5)' = \frac{5^x \ln 5}{(5^x - x^5) \ln 5}$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(a^x)' = a^x \ln a$$

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## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5} \cdot (5^x - x^5)' = \frac{5^x \ln 5 - x^4}{(5^x - x^5) \ln 5}$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

## Zadatak 11

Odredite derivaciju funkcije  $y = \log_5 (5^x - x^5)$ .

## Rješenje

$$y' = \frac{1}{(5^x - x^5) \ln 5} \cdot (5^x - x^5)' = \frac{5^x \ln 5 - 5x^4}{(5^x - x^5) \ln 5}$$

$$(\log_a (\text{nešto}))' = \frac{1}{\text{nešto} \cdot \ln a} \cdot (\text{nešto})'$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

# **dvanaesti zadatak**

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## Zadatak 12

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$



## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot (5x)'$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot (5x)'$$

$$f'(x) = \frac{1}{5x}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot (5x)'$$

$$f'(x) = \frac{1}{5x} \cdot 5$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

## Zadatak 12

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$$(\ln x)' = \frac{1}{x}$$

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$$g'(x) =$$

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$$(\ln x)' = \frac{1}{x}$$



## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

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$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

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$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

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$$g(x) = \ln x^5$$

$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

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$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

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$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

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$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$h(x) = (\ln x)^5$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$

## Zadatak 12

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## Rješenje

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$$f'(x) = \frac{1}{x}$$

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$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$h(x) = (\ln x)^5$$

$$h'(x) =$$

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## Zadatak 12

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## Rješenje

$$f(x) = \ln 5x$$

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$$g(x) = \ln x^5$$

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$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

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$$h(x) = (\ln x)^5$$

$$h'(x) = 5(\ln x)^4$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$



## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

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$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

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Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot (5x)'$$

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$$f'(x) = \frac{1}{x}$$

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$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$h(x) = (\ln x)^5$$

$$h'(x) = 5(\ln x)^4 \cdot (\ln x)'$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

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$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$h(x) = (\ln x)^5$$

$$h'(x) = 5(\ln x)^4 \cdot (\ln x)'$$

$$h'(x) = 5(\ln x)^4$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

$$(x^n)' = nx^{n-1}$$

Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot (5x)'$$

$$f'(x) = \frac{1}{5x} \cdot 5$$

$$f'(x) = \frac{1}{x}$$

$$g(x) = \ln x^5$$

$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$h(x) = (\ln x)^5$$

$$h'(x) = 5(\ln x)^4 \cdot (\ln x)'$$

$$h'(x) = 5(\ln x)^4 \cdot \frac{1}{x}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$

## Zadatak 12

$$((\text{nešto})^n)' = n(\text{nešto})^{n-1} \cdot (\text{nešto})'$$

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Odredite derivacije funkcija  $f(x) = \ln 5x$ ,  $g(x) = \ln x^5$  i  $h(x) = \ln^5 x$ .

## Rješenje

$$f(x) = \ln 5x$$

$$f'(x) = \frac{1}{5x} \cdot (5x)'$$

$$f'(x) = \frac{1}{5x} \cdot 5$$

$$f'(x) = \frac{1}{x}$$

$$g(x) = \ln x^5$$

$$g'(x) = \frac{1}{x^5} \cdot (x^5)'$$

$$g'(x) = \frac{1}{x^5} \cdot 5x^4$$

$$g'(x) = \frac{5}{x}$$

$$h(x) = \ln^5 x$$

$$h(x) = (\ln x)^5$$

$$h'(x) = 5(\ln x)^4 \cdot (\ln x)'$$

$$h'(x) = 5(\ln x)^4 \cdot \frac{1}{x}$$

$$h'(x) = \frac{5}{x} \ln^4 x$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$\ln^k x = (\ln x)^k$$

# **trinaesti zadatak**

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## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' =$$

$$(\ln (\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$



## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)'$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)'$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$\begin{aligned} y' &= \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' = \\ &= \frac{x+1}{x-1} \end{aligned}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$\begin{aligned} y' &= \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' = \\ &= \frac{x+1}{x-1} \cdot \end{aligned}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \text{_____}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{\quad}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)'}{(x+1)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1)}{(x+1)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{\quad}{(x+1)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot 1 - 1 \cdot 1}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1)}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1)}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$



## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left( \frac{x-1}{x+1} \right)' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2} = \underline{\hspace{2cm}}$$

$$\left( \frac{u}{v} \right)' (x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

### Rješenje

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2} = \frac{1}{(x-1)(x+1)}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2} = \frac{2}{(x-1)(x+1)}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

## Zadatak 13

Odredite derivaciju funkcije  $y = \ln \frac{x-1}{x+1}$ .

$$(\ln x)' = \frac{1}{x}$$

## Rješenje

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$y' = \frac{1}{\frac{x-1}{x+1}} \cdot \left(\frac{x-1}{x+1}\right)' =$$

$$= \frac{x+1}{x-1} \cdot \frac{(x-1)' \cdot (x+1) - (x-1) \cdot (x+1)'}{(x+1)^2} =$$

$$= \frac{x+1}{x-1} \cdot \frac{1 \cdot (x+1) - (x-1) \cdot 1}{(x+1)^2} = \frac{2}{(x-1)(x+1)} = \frac{2}{x^2-1}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

# četrnaesti zadatak

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## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$y' =$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$



## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$y' = \frac{1}{2\sqrt{\sin(x^2 - 1)}}$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$y' = \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$y' = \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))'$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Rješenje

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\ &= \frac{1}{2\sqrt{\sin(x^2 - 1)}}\end{aligned}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\ &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \end{aligned}$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sin x)' = \cos x$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \left(\sin(x^2 - 1)\right)' = \\ &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1)\end{aligned}$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sin x)' = \cos x$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

## Rješenje

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\ &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1) \cdot (x^2 - 1)'\end{aligned}$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$(\sin x)' = \cos x$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

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## Rješenje

$$(\sin x)' = \cos x$$

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\ &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1) \cdot (x^2 - 1)'\end{aligned}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$



## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Rješenje

$$(\sin x)' = \cos x$$

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\&= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1) \cdot (x^2 - 1)' = \\&= \underline{\hspace{2cm}}\end{aligned}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Rješenje

$$(\sin x)' = \cos x$$

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\&= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1) \cdot (x^2 - 1)' = \\&= \frac{1}{2\sqrt{\sin(x^2 - 1)}}\end{aligned}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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## Zadatak 14

Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Rješenje

$$(\sin x)' = \cos x$$

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\&= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1) \cdot (x^2 - 1)' = \\&= \frac{2x \cos(x^2 - 1)}{2\sqrt{\sin(x^2 - 1)}}\end{aligned}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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Odredite derivaciju funkcije  $y = \sqrt{\sin(x^2 - 1)}$ .

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

## Rješenje

$$(\sin x)' = \cos x$$

$$\begin{aligned}y' &= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot (\sin(x^2 - 1))' = \\&= \frac{1}{2\sqrt{\sin(x^2 - 1)}} \cdot \cos(x^2 - 1) \cdot (x^2 - 1)' = \\&= \frac{2x \cos(x^2 - 1)}{2\sqrt{\sin(x^2 - 1)}} = \frac{x \cos(x^2 - 1)}{\sqrt{\sin(x^2 - 1)}}\end{aligned}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

# **petnaesti zadatak**

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## Zadatak 15

*Odredite jednadžbu tangente na graf funkcije  $y = \ln(5 - 4x)$  u točki s apscisom 1. Odredite duljinu odsječka dobivene tangente između koordinatnih osi.*

## Zadatak 15

Odredite jednadžbu tangente na graf funkcije  $y = \ln(5 - 4x)$  u točki s apscisom 1. Odredite duljinu odsječka dobivene tangente između koordinatnih osi.

## Rješenje

- Jednadžba tangente na graf funkcije  $y = f(x)$  u točki  $T_0(x_0, y_0)$

$$t \dots y - y_0 = k_t \cdot (x - x_0)$$

## Zadatak 15

Odredite jednadžbu tangente na graf funkcije  $y = \ln(5 - 4x)$  u točki s apscisom 1. Odredite duljinu odsječka dobivene tangente između koordinatnih osi.

## Rješenje

- Jednadžba tangente na graf funkcije  $y = f(x)$  u točki  $T_0(x_0, y_0)$

$$t \dots y - y_0 = k_t \cdot (x - x_0)$$

- Pritom je  $y_0 = f(x_0)$  i  $k_t = f'(x_0)$ .



- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1)$$

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$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' =$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)'$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)' = \frac{1}{5 - 4x}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$



- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)' = \frac{1}{5 - 4x} \cdot (-4)$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)' = \frac{1}{5 - 4x} \cdot (-4) = \frac{-4}{5 - 4x}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)' = \frac{1}{5 - 4x} \cdot (-4) = \frac{-4}{5 - 4x}$$

- Koeficijent smjera tangente

$$k_t = y'(1)$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

$$y_0 = \ln(5 - 4 \cdot 1) = \ln 1 = 0$$

Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)' = \frac{1}{5 - 4x} \cdot (-4) = \frac{-4}{5 - 4x}$$

- Koeficijent smjera tangente

$$k_t = y'(1) = \frac{-4}{5 - 4 \cdot 1}$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

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- Znamo da je  $x_0 = 1$ .

$$y = \ln(5 - 4x)$$

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Točka:  $T_0(1, 0)$

- Derivacija funkcije

$$y' = \frac{1}{5 - 4x} \cdot (5 - 4x)' = \frac{1}{5 - 4x} \cdot (-4) = \frac{-4}{5 - 4x}$$

- Koeficijent smjera tangente

$$k_t = y'(1) = \frac{-4}{5 - 4 \cdot 1} = -4$$

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

$$(\ln x)' = \frac{1}{x}$$

$$x_0 = 1$$

$$y_0 = 0$$

$$k_t = -4$$

- Jednadžba tangente

$$y - y_0 = k_t \cdot (x - x_0)$$

$$x_0 = 1$$

$$y_0 = 0$$

$$k_t = -4$$

- Jednadžba tangente

$$y - y_0 = k_t \cdot (x - x_0)$$

$$y - 0 = -4 \cdot (x - 1)$$

$$x_0 = 1$$

$$y_0 = 0$$

$$k_t = -4$$

- Jednadžba tangente

$$y - y_0 = k_t \cdot (x - x_0)$$

$$y - 0 = -4 \cdot (x - 1)$$

$$y = -4x + 4$$



$$x_0 = 1$$

$$y_0 = 0$$

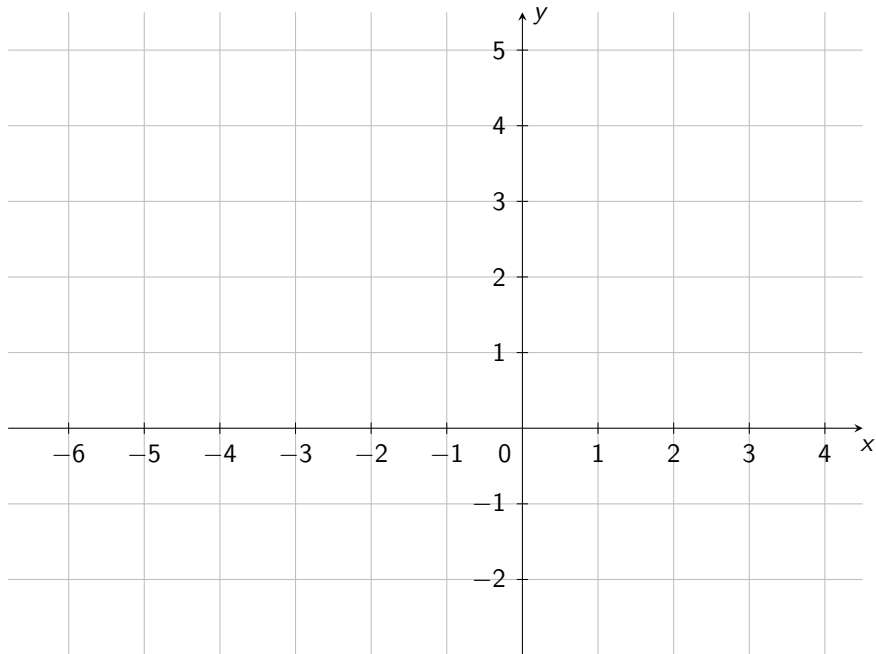
$$k_t = -4$$

- Jednadžba tangente

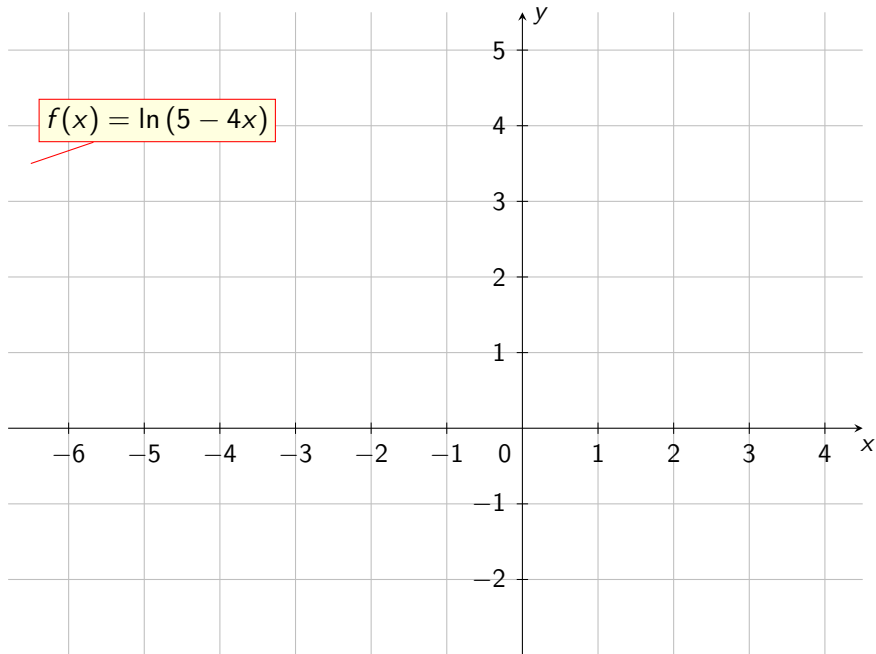
$$y - y_0 = k_t \cdot (x - x_0)$$

$$y - 0 = -4 \cdot (x - 1)$$

$$y = -4x + 4$$



$$f(x) = \ln(5 - 4x)$$



$$f(x) = \ln(5 - 4x)$$

$$5 - 4x > 0$$

$$f(x) = \ln(5 - 4x)$$

$$5 - 4x > 0$$

$$-4x > -5$$

$$f(x) = \ln(5 - 4x)$$

$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

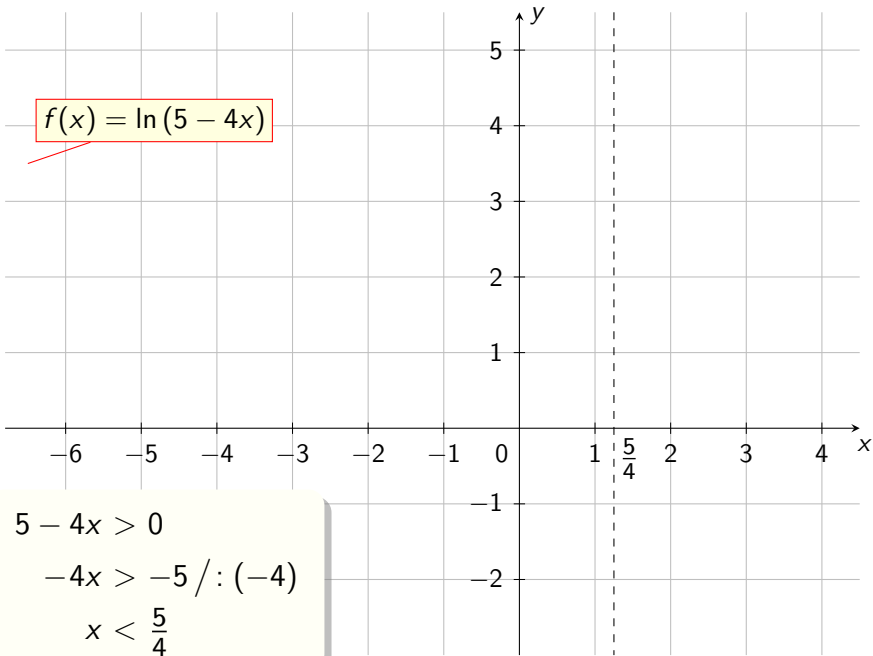
$$f(x) = \ln(5 - 4x)$$

$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$



$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$



$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$

$$5 - 4x > 0$$

$$-4x > -5 \quad / : (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$
1	

$$5 - 4x > 0$$

$$-4x > -5 \quad / : (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$
1	0

$$5 - 4x > 0$$

$$-4x > -5 \quad / : (-4)$$

$$x < \frac{5}{4}$$

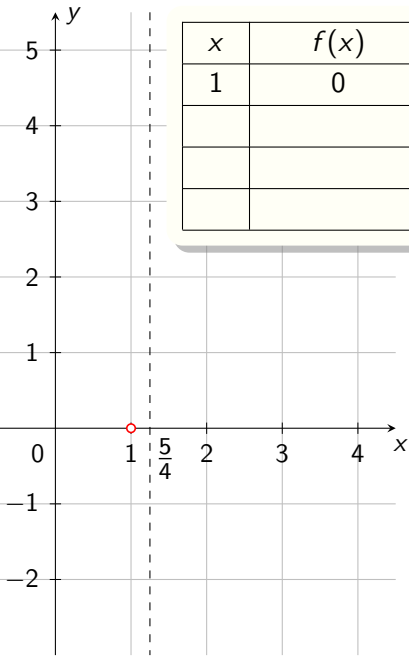
$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$
1	0

$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$



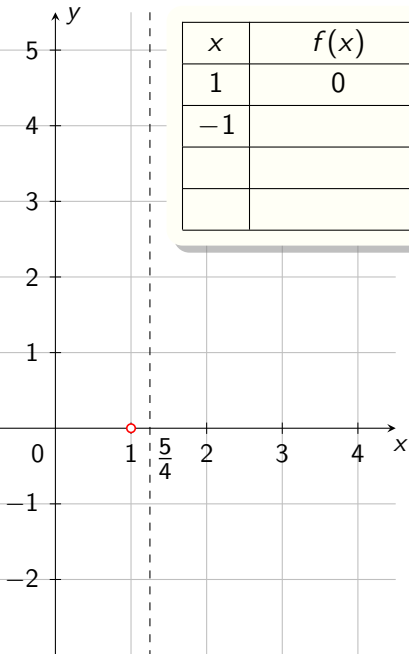
$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$
1	0
-1	

$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$



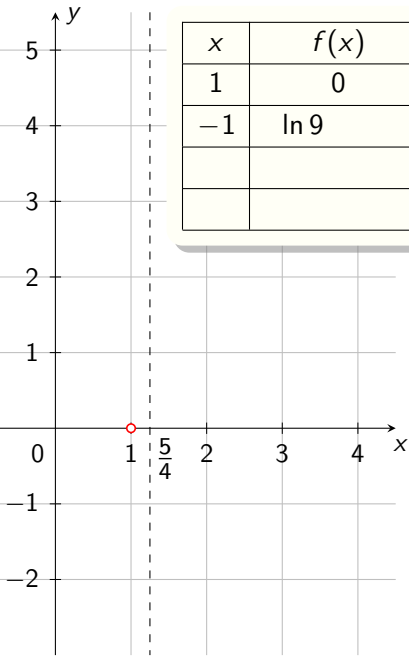
$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$
1	0
-1	$\ln 9$

$$5 - 4x > 0$$

$$-4x > -5 \quad / : (-4)$$

$$x < \frac{5}{4}$$



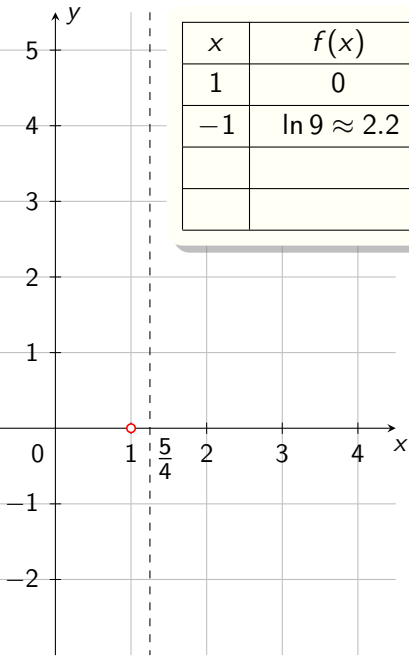
$$f(x) = \ln(5 - 4x)$$

$x$	$f(x)$
1	0
-1	$\ln 9 \approx 2.2$

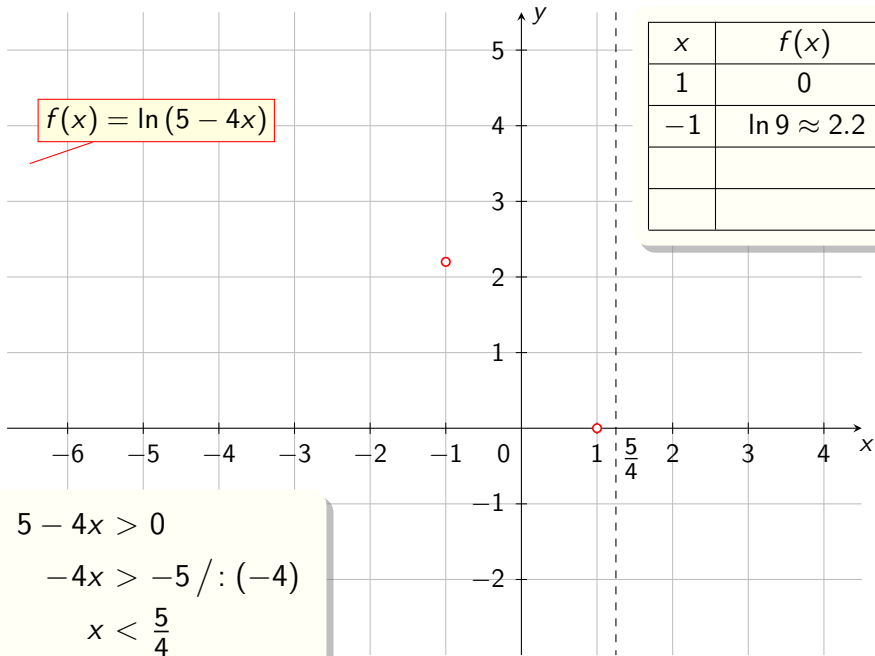
$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$



$$f(x) = \ln(5 - 4x)$$



$x$	$f(x)$
1	0
-1	$\ln 9 \approx 2.2$

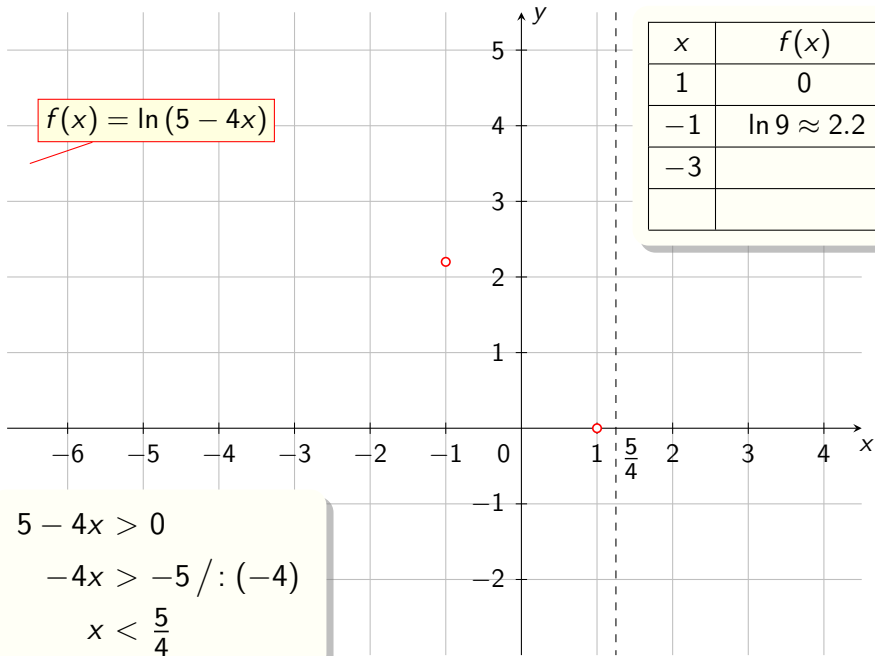
$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$



$$f(x) = \ln(5 - 4x)$$



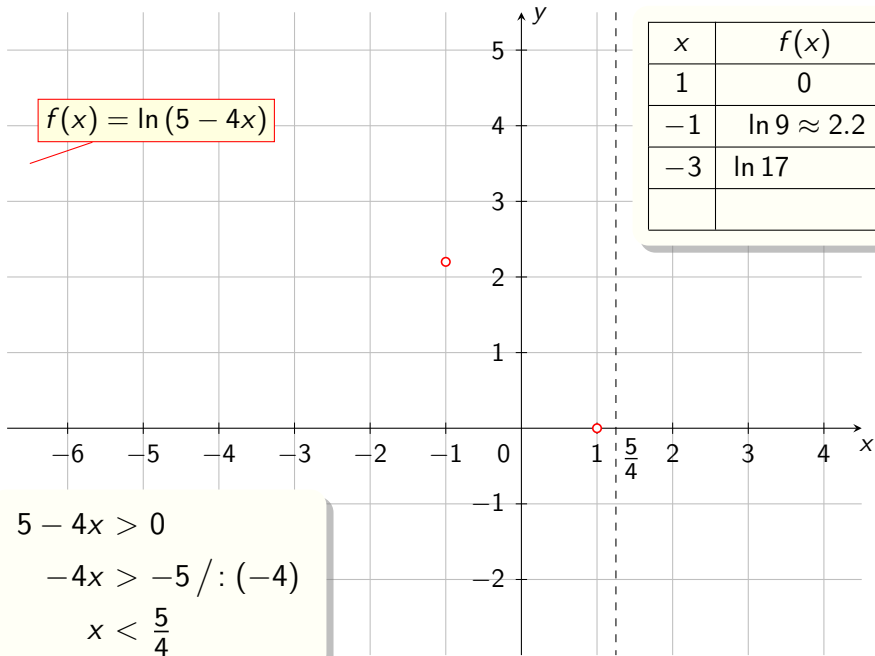
$x$	$f(x)$
1	0
-1	$\ln 9 \approx 2.2$
-3	

$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

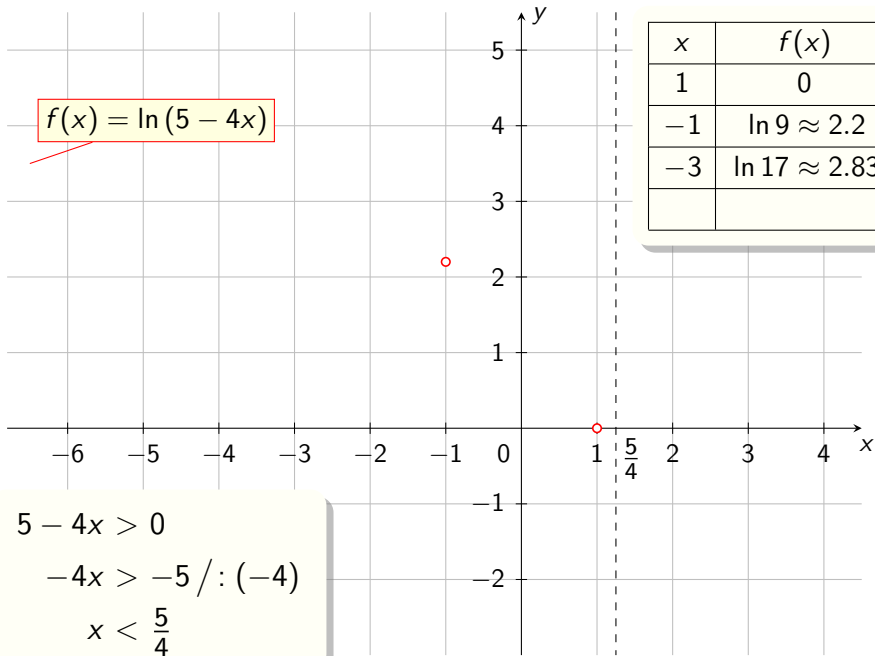


$$5 - 4x > 0$$

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$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

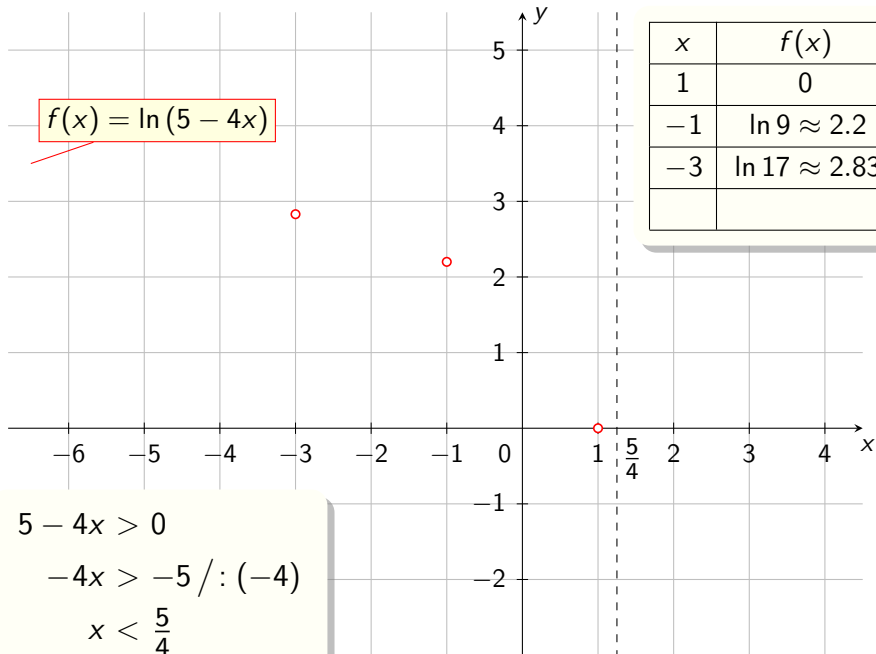


$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

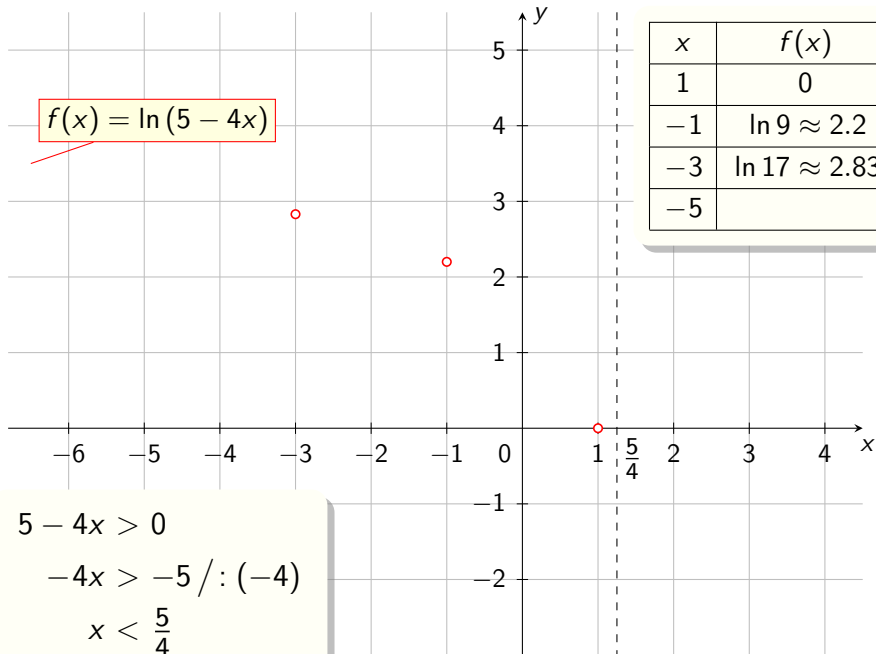


$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

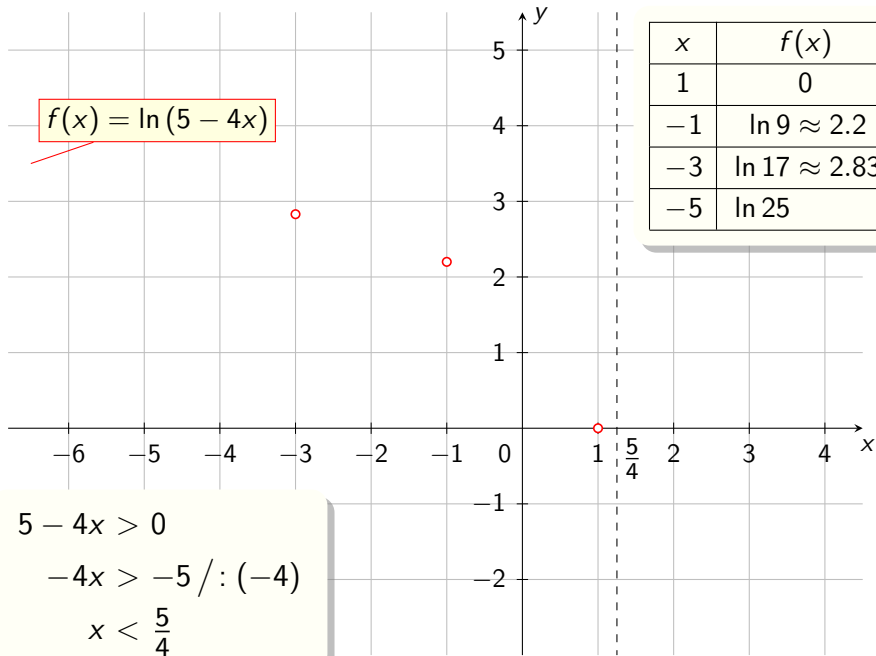


$$5 - 4x > 0$$

$$-4x > -5 \quad /: (-4)$$

$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$

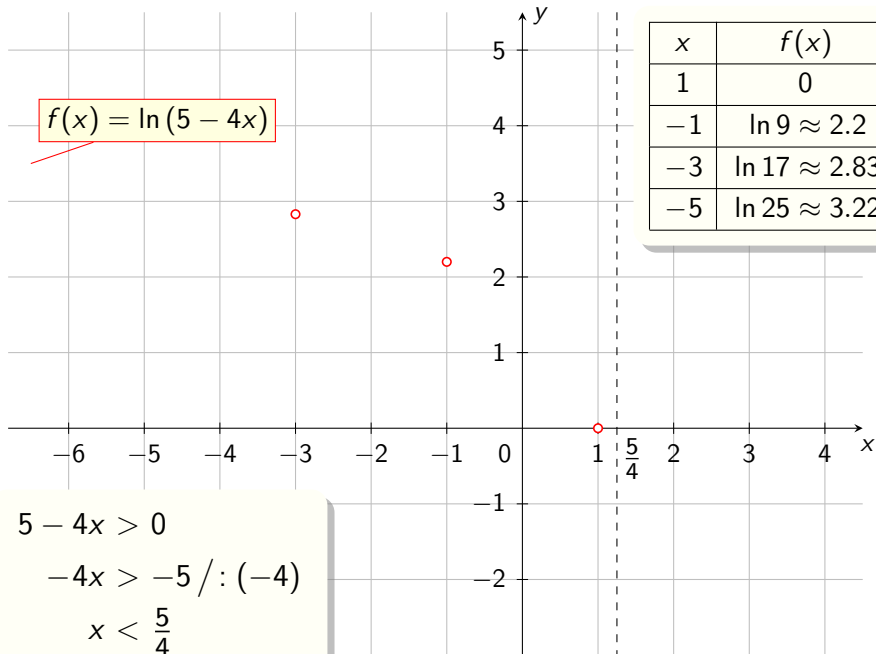


$$5 - 4x > 0$$

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$$x < \frac{5}{4}$$

$$f(x) = \ln(5 - 4x)$$



$$5 - 4x > 0$$

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$$x < \frac{5}{4}$$

