

Seminari 11

MATEMATIČKE METODE ZA INFORMATIČARE

Damir Horvat

FOI, Varaždin

Sadržaj

prvi zadatak

drugi zadatak

treći zadatak

četvrti zadatak

peti zadatak

prvi zadatak

Zadatak 1

Primjenom Euklidovog algoritma ispitajte može li se skratiti razlomak

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

Ukoliko se može, skratite ga.

Rješenje

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2)$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2)$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) =$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ - 2$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ + x - 2$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 + 3x^2 + x - 2$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ - x^3 + 3x^2 + x - 2$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1$$
$$-x^4 - x^3 + 3x^2 + x - 2$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ \underline{-x^4 - x^3 + 3x^2 + x - 2} \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ \underline{-x^4 - x^3 + 3x^2 + x - 2} \\ 2x^2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ \underline{-x^4 - x^3 + 3x^2 + x - 2} \\ 2x^2 + 2x \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \\ \underline{-x^4 - x^3 + 3x^2 + x - 2} \\ 2x^2 + 2x - 4 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
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Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
$$\frac{-x^4 - x^3 + 3x^2 + x - 2}{2x^2 + 2x - 4} \leftarrow R_1$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
$$\frac{-x^4 - x^3 + 3x^2 + x - 2}{2x^2 + 2x - 4} \leftarrow R_1$$

$$(x^4 + x^3 - 3x^2 - x + 2)$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4)$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
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Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

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$$(x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

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$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 \\ \quad + 2x^2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

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$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 \\ -x^3 + 2x^2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

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$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 \\ \hline -x^4 - x^3 + 2x^2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
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Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

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$$(x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2$$
$$\frac{-x^4 - x^3 + 2x^2}{-x^2}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
$$\frac{-x^4 - x^3 + 3x^2 + x - 2}{2x^2 + 2x - 4} \leftarrow R_1$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2$$
$$\frac{-x^4 - x^3 + 2x^2}{-x^2 - x}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
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$$(x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2$$
$$\frac{-x^4 - x^3 + 2x^2}{-x^2 - x + 2}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$(x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1$$
$$\frac{-x^4 - x^3 + 3x^2 + x - 2}{2x^2 + 2x - 4} \leftarrow R_1$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2}$$
$$\frac{-x^4 - x^3 + 2x^2}{-x^2 - x + 2}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline -2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline +x - 2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline x^2 + x - 2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \quad x^2 + x - 2 \\ \hline \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \quad x^2 + x - 2 \\ \hline 0 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline x^2 + x - 2 \\ \hline 0 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline x^2 + x - 2 \\ \hline 0 \leftarrow R_2 \end{array}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ x^2 + x - 2 \\ \hline 0 \leftarrow R_2 \end{array}$$

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Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline x^2 + x - 2 \\ \hline 0 \leftarrow R_2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2,$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ x^2 + x - 2 \\ \hline 0 \leftarrow R_2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2)$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline x^2 + x - 2 \\ \hline 0 \leftarrow R_2 \end{array}$$

$$\begin{aligned} M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) &= \\ &= n(2x^2 + 2x - 4) \end{aligned}$$

Rješenje $\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$

$$\begin{array}{l} (x^4 + x^3 - x^2 + x - 2) : (x^4 + x^3 - 3x^2 - x + 2) = 1 \leftarrow Q_1 \\ \hline -x^4 - x^3 + 3x^2 + x - 2 \\ \hline 2x^2 + 2x - 4 \leftarrow R_1 \end{array}$$

$$\begin{array}{l} (x^4 + x^3 - 3x^2 - x + 2) : (2x^2 + 2x - 4) = \frac{1}{2}x^2 - \frac{1}{2} \leftarrow Q_2 \\ \hline -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ \hline x^2 + x - 2 \\ \hline 0 \leftarrow R_2 \end{array}$$

$$\begin{aligned} M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) &= \\ &= n(2x^2 + 2x - 4) = x^2 + x - 2 \end{aligned}$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2)$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2)$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) =$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 - x^3 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2$$
$$-x^4 - x^3 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2$$

$$-x^4 - x^3 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2$$
$$\frac{-x^4 - x^3 + 2x^2}{x^2}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2$$
$$\frac{-x^4 - x^3 + 2x^2}{x^2 + x}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2$$
$$\frac{-x^4 - x^3 + 2x^2}{x^2 + x - 2}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ + 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x + 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ \hline -x^2 - x + 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \underline{\hspace{10em}}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2)$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2)$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) =$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{x^4 + x^3 - 3x^2 - x + 2}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2$$

$$-x^3 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$(x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1$$

$$\begin{array}{r} -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$(x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2$$

$$-x^4 - x^3 + 2x^2$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 \\ \underline{-x^4 - x^3 + 2x^2} \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x + 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ -2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ -x^4 - x^3 + 2x^2 \\ \hline x^2 + x - 2 \\ -x^2 - x + 2 \\ \hline 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ -x^4 - x^3 + 2x^2 \\ \hline -x^2 - x + 2 \\ +x - 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x + 2 \\ x^2 + x - 2 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x + 2 \\ \underline{x^2 + x - 2} \\ 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 + 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x + 2 \\ \underline{x^2 + x - 2} \\ 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 - 1)}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x + 2 \\ \underline{x^2 + x - 2} \\ 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

$$\frac{x^4 + x^3 - x^2 + x - 2}{x^4 + x^3 - 3x^2 - x + 2} = \frac{(x^2 + x - 2)(x^2 + 1)}{(x^2 + x - 2)(x^2 - 1)} = \frac{x^2 + 1}{x^2 - 1}$$

$$\begin{array}{r} (x^4 + x^3 - x^2 + x - 2) : (x^2 + x - 2) = x^2 + 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ x^2 + x - 2 \\ \underline{-x^2 - x + 2} \\ 0 \end{array}$$

$$\begin{array}{r} (x^4 + x^3 - 3x^2 - x + 2) : (x^2 + x - 2) = x^2 - 1 \\ \underline{-x^4 - x^3 + 2x^2} \\ -x^2 - x + 2 \\ \underline{x^2 + x - 2} \\ 0 \end{array}$$

$$M(x^4 + x^3 - x^2 + x - 2, x^4 + x^3 - 3x^2 - x + 2) = x^2 + x - 2$$

drugi zadatak

Zadatak 2

Zadani su polinomi

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1 \quad i \quad g(x) = 2x^3 - 3x^2 + 2x + 2.$$

Odredite polinome \tilde{f} i \tilde{g} takve da je $f\tilde{f} + g\tilde{g} = M(f, g)$.

Rješenje

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1)$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2)$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) =$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x - 2x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x - 2x^2 - 2x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 3x^3 - 2x^2 - 2x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x - 2x^4 + 3x^3 - 2x^2 - 2x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{l} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x \\ \underline{-2x^4 + 3x^3 - 2x^2 - 2x} \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{l} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{l} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1$$
$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ - 2 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ - 2x - 2 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ + 3x^2 - 2x - 2 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$
$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{l} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1 \\ \hline -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$(2x^3 - 3x^2 + 2x + 2)$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1)$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) =$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$-2x^4 + 3x^3 - 2x^2 - 2x$$

$$2x^3 - x^2 + x + 1$$

$$-2x^3 + 3x^2 - 2x - 2$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x$$
$$+ x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x + x^2 + x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$\begin{array}{r} (2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x \\ -2x^3 + x^2 + x \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$-1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$-x - 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$2x^2 - x - 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1)$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1)$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

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$$2x^2 - x - 1 \leftarrow R_1$$

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$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) =$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

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Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

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$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x$$

$$-x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

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$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$+ 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$2x + 1$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$\begin{array}{r} 2x + 1 \\ \hline \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$
$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$\begin{array}{r} 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$
$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$\begin{array}{r} -2x^2 + 3x + 2 \\ 2x^2 - x - 1 \\ \hline 2x + 1 \leftarrow R_2 \end{array}$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1$$
$$\begin{array}{r} -2x^2 - x \\ \hline -2x - 1 \\ 2x + 1 \\ \hline 0 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1 \leftarrow Q_3$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$\begin{array}{r} 2x + 1 \\ \hline \end{array}$$

$$0$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$\begin{array}{r} (2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1 \\ -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline 2x^3 - x^2 + x + 1 \\ -2x^3 + 3x^2 - 2x - 2 \\ \hline 2x^2 - x - 1 \leftarrow R_1 \end{array}$$

$$\begin{array}{r} (2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2 \\ -2x^3 + x^2 + x \\ \hline -2x^2 + 3x + 2 \\ 2x^2 - x - 1 \\ \hline 2x + 1 \leftarrow R_2 \end{array}$$

$$\begin{array}{r} (2x^2 - x - 1) : (2x + 1) = x - 1 \leftarrow Q_3 \\ -2x^2 - x \\ \hline -2x - 1 \\ 2x + 1 \\ \hline 0 \leftarrow R_3 \end{array}$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$M(f, g) =$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1 \leftarrow Q_3$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$\begin{array}{r} 2x + 1 \\ \hline \end{array}$$

$$0 \leftarrow R_3$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$M(f, g) = n(2x + 1)$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1 \leftarrow Q_3$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$\begin{array}{r} 2x + 1 \\ \hline \end{array}$$

$$0 \leftarrow R_3$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$M(f, g) = n(2x + 1) = x + \frac{1}{2}$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1 \leftarrow Q_3$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$\begin{array}{r} 2x + 1 \\ \hline \end{array}$$

$$0 \leftarrow R_3$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

Rješenje

$$(2x^4 - x^3 + x^2 + 3x + 1) : (2x^3 - 3x^2 + 2x + 2) = x + 1 \leftarrow Q_1$$

$$\begin{array}{r} -2x^4 + 3x^3 - 2x^2 - 2x \\ \hline \end{array}$$

$$2x^3 - x^2 + x + 1$$

$$\begin{array}{r} -2x^3 + 3x^2 - 2x - 2 \\ \hline \end{array}$$

$$2x^2 - x - 1 \leftarrow R_1$$

$$M(f, g) = n(2x + 1) = x + \frac{1}{2}$$

$$\frac{1}{2}R_2$$

$$(2x^3 - 3x^2 + 2x + 2) : (2x^2 - x - 1) = x - 1 \leftarrow Q_2$$

$$\begin{array}{r} -2x^3 + x^2 + x \\ \hline \end{array}$$

$$-2x^2 + 3x + 2$$

$$\begin{array}{r} 2x^2 - x - 1 \\ \hline \end{array}$$

$$2x + 1 \leftarrow R_2$$

$$(2x^2 - x - 1) : (2x + 1) = x - 1$$

$$\begin{array}{r} -2x^2 - x \\ \hline \end{array}$$

$$-2x - 1$$

$$\begin{array}{r} 2x + 1 \\ \hline \end{array}$$

$$0 \leftarrow R_3$$

$$f(x) = 2x^4 - x^3 + x^2 + 3x + 1$$

$$g(x) = 2x^3 - 3x^2 + 2x + 2$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$f = gQ_1 + R_1$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$f = gQ_1 + R_1$$

$$g = R_1Q_2 + R_2$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$f = gQ_1 + R_1$$

$$g = R_1Q_2 + R_2$$

$$R_1 = R_2Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$g = R_1 Q_2 + R_2$$

$$f = gQ_1 + R_1$$

$$g = R_1 Q_2 + R_2$$

$$R_1 = R_2 Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$g = R_1 Q_2 + R_2$$

$$g - R_1 Q_2 = R_2$$

$$f = gQ_1 + R_1$$

$$g = R_1 Q_2 + R_2$$

$$R_1 = R_2 Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$g = R_1 Q_2 + R_2$$

$$g - R_1 Q_2 = R_2$$

$$f = gQ_1 + R_1$$

$$g = R_1 Q_2 + R_2$$

$$R_1 = R_2 Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$M(f, g) = \frac{1}{2}R_2$$

$$g = R_1 Q_2 + R_2$$

$$g - R_1 Q_2 = R_2 \quad / \cdot \frac{1}{2}$$

$$f = gQ_1 + R_1$$

$$g = R_1 Q_2 + R_2$$

$$R_1 = R_2 Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$M(f, g) = \frac{1}{2}R_2$$

$$g = R_1 Q_2 + R_2$$

$$g - R_1 Q_2 = R_2 \quad / \cdot \frac{1}{2}$$

$$\frac{1}{2}g - \frac{1}{2}R_1 Q_2 = \frac{1}{2}R_2$$

$$f = gQ_1 + R_1$$

$$g = R_1 Q_2 + R_2$$

$$R_1 = R_2 Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$M(f, g) = \frac{1}{2}R_2$$

$$g = R_1 Q_2 + R_2$$

$$g - R_1 Q_2 = R_2 \quad / \cdot \frac{1}{2}$$

$$\frac{1}{2}g - \frac{1}{2}R_1 Q_2 = \frac{1}{2}R_2$$

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$$\left(-\frac{1}{2}x + \frac{1}{2}\right) \cdot f(x) + \frac{1}{2}x^2 \cdot g(x) = M(f, g)$$

$$\tilde{f}(x) = -\frac{1}{2}x + \frac{1}{2} \quad \tilde{g}(x) = \frac{1}{2}x^2$$

$$R_1 = f - gQ_1 \quad \leftarrow f = gQ_1 + R_1$$

$$Q_2(x) = x - 1$$

$$Q_1(x) = x + 1$$

$$g = R_1 Q_2 + R_2$$

$$R_1 = R_2 Q_3$$

$$f\tilde{f} + g\tilde{g} = M(f, g)$$

$$M(f, g) = \frac{1}{2}R_2$$

treći zadatak

Zadatak 3

Riješite jednađbu

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

ako je poznato jedno njezino rješenje $x_1 = 2 - i$.

Zadatak 3

Riješite jednadžbu

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

ako je poznato jedno njezino rješenje $x_1 = 2 - i$.

Kompleksne nultočke polinoma

Neka je $P \in \mathbb{R}[x]$. Ako je $z_0 \in \mathbb{C}$ nultočka polinoma P , tada je i \bar{z}_0 također nultočka polinoma P .

Rješenje $x_1 = 2 - i$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

Rješenje $x_1 = 2 - i, \quad x_2 = 2 + i$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

Rješenje

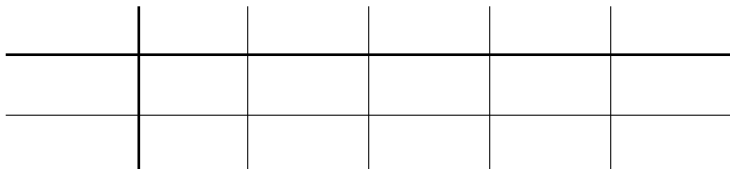
$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$



Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1				

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4			

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6		

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$					

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1				

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$(2 - i)(-2 - i) =$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$(2 - i)(-2 - i) = -4$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$(2 - i)(-2 - i) = -4 - 2i$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$(2 - i)(-2 - i) = -4 - 2i + 2i$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$			

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1		

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$					

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1				

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0			

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1		

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i))$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i)) \cdot (x - (2 + i))$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i)) \cdot (x - (2 + i)) \cdot ($$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1)$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x - (2 - i)) \cdot (x^3 + (-2 - i)x^2 + x - 2 - i) = 0$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1 \quad (x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$(x - (2 - i)) \cdot (x - (2 + i)) =$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned} &(x - (2 - i)) \cdot (x - (2 + i)) = \\ &= x^2 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x + \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x + 4 - i^2 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ & = x^2 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

2. način

$$\begin{aligned}(x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x\end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
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$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x^4 - 4x^3 + 6x^2 - 4x + 5)$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ & = x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

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$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5)$$

2. način

$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ & = x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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$$\begin{aligned} & (x - (2 - i)) \cdot (x - (2 + i)) = \\ & = x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ & = x^2 - 4x + 5 \end{aligned}$$

Rješenje

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$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

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$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5) = x^2 - 5x^2$$

2. način

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

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$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

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$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5) = x^2 + 4x^3 - 5x^2$$

2. način

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

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$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

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2. način

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

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$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

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$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

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2. način

$$\frac{-x^4 + 4x^3 - 5x^2}{}$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

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$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5) = x^2$$

2. način

$$\frac{-x^4 + 4x^3 - 5x^2}{x^2}$$

$$\begin{aligned}(x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5\end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

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	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
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$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

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$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5) = x^2$$

2. način

$$\frac{-x^4 + 4x^3 - 5x^2}{x^2 - 4x + 5}$$

$$\begin{aligned}
 (x - (2 - i)) \cdot (x - (2 + i)) &= \\
 &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\
 &= x^2 - 4x + 5
 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
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$$x^2 - 4x + 5$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

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	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
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2. način

$$\begin{array}{r} -x^4 + 4x^3 - 5x^2 \\ \hline \end{array}$$

$$\begin{array}{r} x^2 - 4x + 5 \\ -5 \end{array}$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

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2. način

$$\begin{array}{r} -x^4 + 4x^3 - 5x^2 \\ \hline \end{array}$$

$$\begin{array}{r} x^2 - 4x + 5 \\ + 4x - 5 \\ \hline \end{array}$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

	1	-4	6	-4	5
$2 - i$	1	$-2 - i$	1	$-2 - i$	0
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$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

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2. način

$$\begin{array}{r} -x^4 + 4x^3 - 5x^2 \\ \hline \end{array}$$

$$x^2 - 4x + 5$$

$$-x^2 + 4x - 5$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

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$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5) = x^2 + 1$$

2. način

$$\begin{array}{r} -x^4 + 4x^3 - 5x^2 \\ \hline \end{array}$$

$$x^2 - 4x + 5$$

$$\begin{array}{r} -x^2 + 4x - 5 \\ \hline \end{array}$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$

Rješenje

$$x_1 = 2 - i, \quad x_2 = 2 + i$$

$$x^4 - 4x^3 + 6x^2 - 4x + 5 = 0$$

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$2 - i$	1	$-2 - i$	1	$-2 - i$	0
$2 + i$	1	0	1	0	

$$i^2 = -1$$

$$(x - (2 - i)) \cdot (x - (2 + i)) \cdot (x^2 + 0 \cdot x + 1) = 0$$

$$x^2 + 1 = 0 \rightsquigarrow x^2 = -1 \rightsquigarrow x_3 = i, \quad x_4 = -i$$

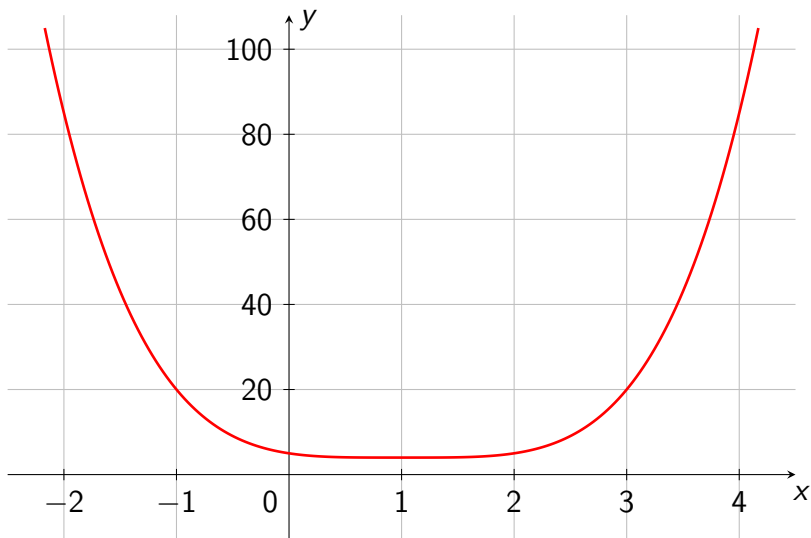
$$(2 - i)(-2 - i) = -4 - 2i + 2i + i^2 = -4 - 1 = -5$$

$$(x^4 - 4x^3 + 6x^2 - 4x + 5) : (x^2 - 4x + 5) = x^2 + 1$$

2. način

$$\begin{array}{r} -x^4 + 4x^3 - 5x^2 \\ \hline x^2 - 4x + 5 \\ -x^2 + 4x - 5 \\ \hline 0 \end{array}$$

$$\begin{aligned} (x - (2 - i)) \cdot (x - (2 + i)) &= \\ &= x^2 - (2 + i)x - (2 - i)x + 4 - i^2 = \\ &= x^2 - 4x + 5 \end{aligned}$$



$$f(x) = x^4 - 4x^3 + 6x^2 - 4x + 5$$

čtvrti zadatak

Zadatak 4

Odredite sva rješenja jednadžbe

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

ako je poznato da ima barem jedno cjelobrojno kompleksno rješenje.

Zadatak 4

Odredite sva rješenja jednadžbe

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

ako je poznato da ima barem jedno cjelobrojno kompleksno rješenje.

Cjelobrojne kompleksne nultočke polinoma

Ako je $\alpha + \beta i$ cjelobrojna kompleksna nultočka polinoma

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

s cjelobrojnim koeficijentima, onda je $\alpha^2 + \beta^2$ djeliteľ slobodnog člana.

Rješenje

pozitivni djelitelji od 25:

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 =$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

i ,

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

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$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$i, -i,$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 =$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$i, -i,$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 = 1^2 + 2^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$i, -i,$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 = 1^2 + 2^2 = 1^2 + (-2)^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$i, -i,$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 = 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$i, -i,$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 = 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2$$

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$i, -i,$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

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$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$i, -i, 1 + 2i,$$

Rješenje

pozitivni djelitelji od 25: 1, 5, 25

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 = 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$i, -i, 1 + 2i, 1 - 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$5 = 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

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$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

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$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 \end{aligned}$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

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$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

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$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

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$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

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$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
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Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

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$$25 =$$

$$\begin{aligned} &i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i, \\ &-2 - i, \end{aligned}$$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

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$$25 = 0^2 + 5^2$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

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Rješenje

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$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

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Rješenje

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Rješenje

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Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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Rješenje

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pozitivni djelitelji od 25: 1, 5, 25

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$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
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Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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 $-2 - i, 5i, -5i, 3 + 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

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 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

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$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 = 4^2 + (-3)^2 = (-4)^2 + 3^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 = 4^2 + (-3)^2 = (-4)^2 + 3^2 = (-4)^2 + (-3)^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

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$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

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$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 = 4^2 + (-3)^2 = (-4)^2 + 3^2 = (-4)^2 + (-3)^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 = 4^2 + (-3)^2 = (-4)^2 + 3^2 = (-4)^2 + (-3)^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 = 4^2 + (-3)^2 = (-4)^2 + 3^2 = (-4)^2 + (-3)^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i,$

Rješenje

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

pozitivni djelitelji od 25: 1, 5, 25

$$\alpha^2 + \beta^2 \rightsquigarrow \alpha + \beta i$$

$$1 = 0^2 + 1^2 = 0^2 + (-1)^2$$

$$\begin{aligned} 5 &= 1^2 + 2^2 = 1^2 + (-2)^2 = (-1)^2 + 2^2 = (-1)^2 + (-2)^2 \\ &= 2^2 + 1^2 = 2^2 + (-1)^2 = (-2)^2 + 1^2 = (-2)^2 + (-1)^2 \end{aligned}$$

$$\begin{aligned} 25 &= 0^2 + 5^2 = 0^2 + (-5)^2 \\ &= 3^2 + 4^2 = 3^2 + (-4)^2 = (-3)^2 + 4^2 = (-3)^2 + (-4)^2 \\ &= 4^2 + 3^2 = 4^2 + (-3)^2 = (-4)^2 + 3^2 = (-4)^2 + (-3)^2 \end{aligned}$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$



$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$



$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6			

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18		

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$					

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1				

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$(1 + 2i)(-5 + 2i) =$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$(1 + 2i)(-5 + 2i) = -5$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$(1 + 2i)(-5 + 2i) = -5 + 2i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$			

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) =$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$
 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) =$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) = -5$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) = -5 + 10i$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) = -5 + 10i - 10i$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) = -5 + 10i - 10i + 20i^2$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) = -5 + 10i - 10i + 20i^2 = -25$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + 2i)(9 - 8i) = 9 - 8i + 18i - 16i^2 = 25 + 10i$$

$$(1 + 2i)(-5 + 10i) = -5 + 10i - 10i + 20i^2 = -25$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

$$-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$$

$$4 - 3i, -4 + 3i, -4 - 3i$$

$$x_1 = 1 + 2i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

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$$x_1 = 1 + 2i, \quad x_2 = 1 - 2i \quad x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0

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	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
$1 - 2i$					

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + (x - (1 + 2i))) \cdot (x^3 + (-5 + 2i)x^2 + (9 - 8i)x - 5 + 10i) = 0$$

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$$x_1 = 1 + 2i, \quad x_2 = 1 - 2i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
$1 - 2i$	1				

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + (x - (1 + 2i))) \cdot (x^3 + (-5 + 2i)x^2 + (9 - 8i)x - 5 + 10i) = 0$$

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$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
$1 - 2i$	1	-4			

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

$$(1 + (x - (1 + 2i))) \cdot (x^3 + (-5 + 2i)x^2 + (9 - 8i)x - 5 + 10i) = 0$$

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$$x_1 = 1 + 2i, \quad x_2 = 1 - 2i$$

$$x^4 - 6x^3 + 18x^2 - 30x + 25 = 0$$

	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
$1 - 2i$	1	-4	5		

$$i^2 = -1$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

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	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
$1 - 2i$	1	-4	5	0	

$$i^2 = -1$$

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 $-2 - i, 5i, -5i, 3 + 4i, 3 - 4i, -3 + 4i, -3 - 4i, 4 + 3i,$
 $4 - 3i, -4 + 3i, -4 - 3i$

$$x_1 = 1 + 2i, \quad x_2 = 1 - 2i$$

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	1	-6	18	-30	25
$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
$1 - 2i$	1	-4	5	0	

$$i^2 = -1 \quad (x - (1 + 2i))$$

$$(1 + 2i)(-5 + 2i) = -5 + 2i - 10i + 4i^2 = -9 - 8i$$

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$1 + 2i$	1	$-5 + 2i$	$9 - 8i$	$-5 + 10i$	0
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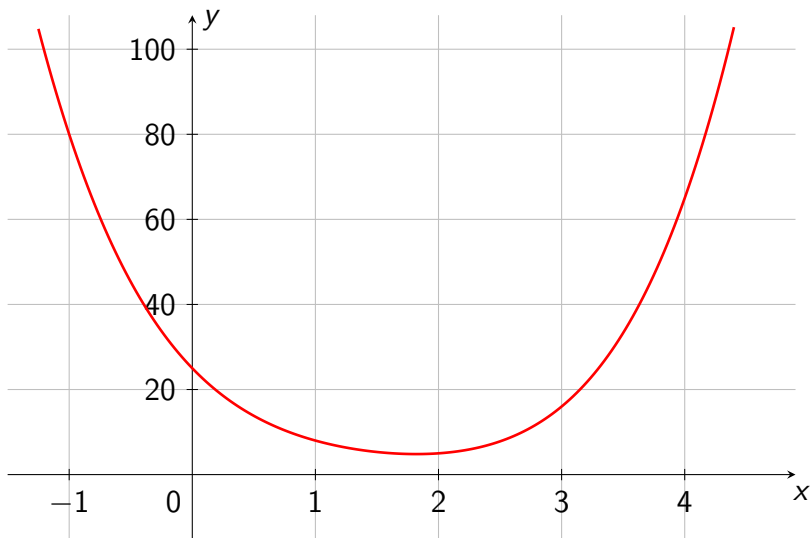
$$x_3 = 2 + i$$

$$x_4 = 2 - i$$

$$i, -i, 1 + 2i, 1 - 2i, -1 + 2i, -1 - 2i, 2 + i, 2 - i, -2 + i,$$

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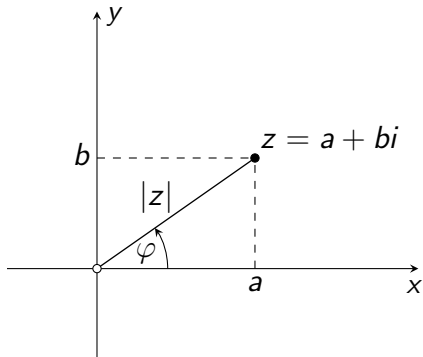
$$4 - 3i, -4 + 3i, -4 - 3i$$



$$f(x) = x^4 - 6x^3 + 18x^2 - 30x + 25$$

peti zadatak

Trigonometrijski zapis kompleksnog broja



$$a = r \cos \varphi$$

$$b = r \sin \varphi$$

$$\arg z = \varphi \in [0, 2\pi)$$

$$\operatorname{tg} \varphi = \frac{b}{a}$$

$$r = |z| = \sqrt{a^2 + b^2}$$

$$z = r(\cos \varphi + i \sin \varphi)$$

$$z^n = r^n (\cos(n\varphi) + i \sin(n\varphi)), \quad n \in \mathbb{N}$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right), \quad k = 0, 1, \dots, n-1$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1,$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$



Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

	1			
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Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

	1	3		

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

	1	3	1	

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

	1	3	1	3

Zadatak 5

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Rješenje

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$$1, -1, 3, -3$$

	1	3	1	3
-3				

Zadatak 5

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Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

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$$1, -1, 3, -3$$

	1	3	1	3
-3	1			

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & & \end{array}$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

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$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & \end{array}$$

Zadatak 5

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$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$(t - (-3))$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$(t - (-3))(t^2 + 0 \cdot t + 1)$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

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$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

$$(t - (-3))(t^2 + 0 \cdot t + 1) = 0$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

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$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

$$(t - (-3))(t^2 + 0 \cdot t + 1) = 0$$

$$(t + 3)(t^2 + 1) = 0$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

$$(t - (-3))(t^2 + 0 \cdot t + 1) = 0$$

$$(t + 3)(t^2 + 1) = 0$$


$$t_1 = -3$$

Zadatak 5

U skupu kompleksnih brojeva riješite jednačbu $z^6 + 3z^4 + z^2 + 3 = 0$.

Rješenje

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t$$

$$t^3 + 3t^2 + t + 3 = 0$$

$$1, -1, 3, -3$$

$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

$$(t - (-3))(t^2 + 0 \cdot t + 1) = 0$$

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$$t_1 = -3$$

$$t^2 + 1 = 0$$

Zadatak 5

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$$\begin{array}{c|c|c|c|c} & 1 & 3 & 1 & 3 \\ \hline -3 & 1 & 0 & 1 & 0 \end{array}$$

$$(t - (-3))(t^2 + 0 \cdot t + 1) = 0$$

$$(t + 3)(t^2 + 1) = 0$$

$$t_1 = -3$$

$$t^2 + 1 = 0$$

$$t_2 = i$$

$$t_3 = -i$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

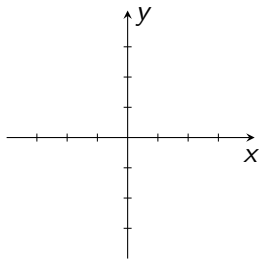
$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



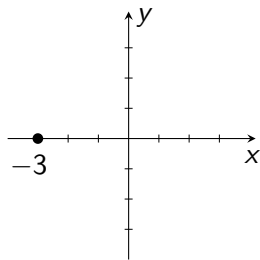
$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



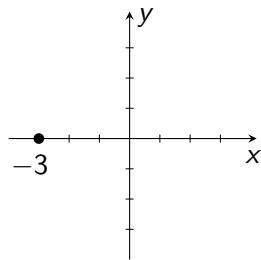
$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3$$

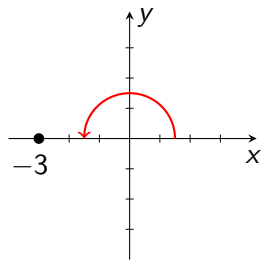
$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3$$

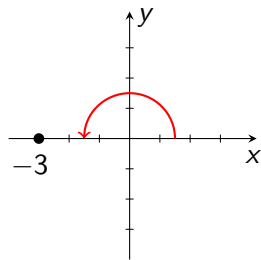
$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

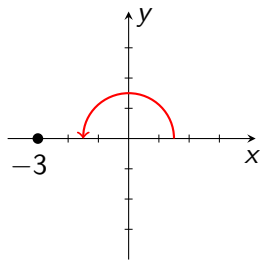
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k =$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

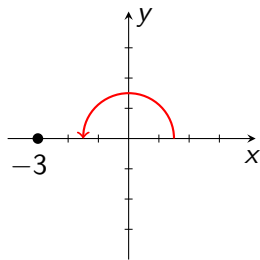
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\right.$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

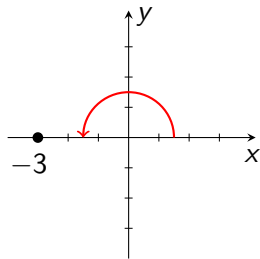
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} \right)$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

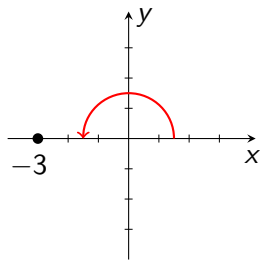
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} + i \sin \frac{\pi + 2k\pi}{2} \right)$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

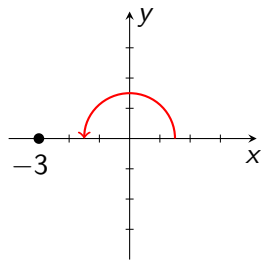
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

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$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} + i \sin \frac{\pi + 2k\pi}{2} \right)$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

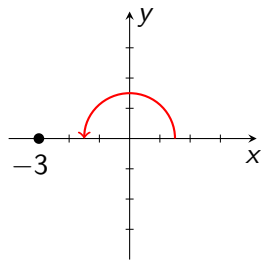
$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} + i \sin \frac{\pi + 2k\pi}{2} \right)$$

$$(\sqrt{-3})_0 =$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

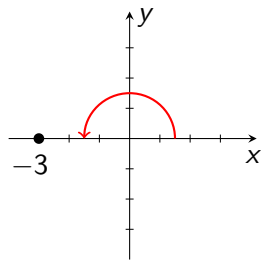
$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} + i \sin \frac{\pi + 2k\pi}{2} \right)$$

$$(\sqrt{-3})_0 = \sqrt{3} \cdot \left(\right)$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

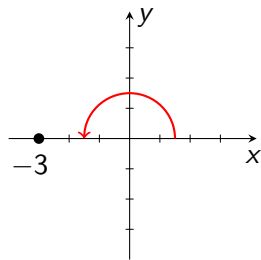
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$$z = \sqrt{-3}$$

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$$(\sqrt{-3})_0 = \sqrt{3} \cdot \left(\cos \frac{\pi}{2} \right)$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

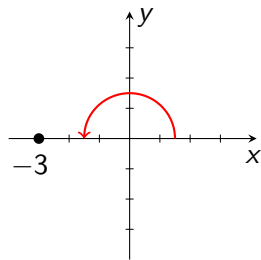
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$$(\sqrt{-3})_0 = \sqrt{3} \cdot \left(\cos \frac{\pi}{2} + \right)$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

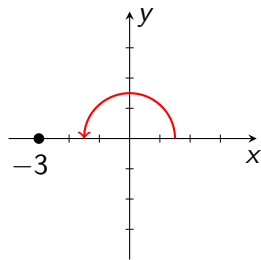
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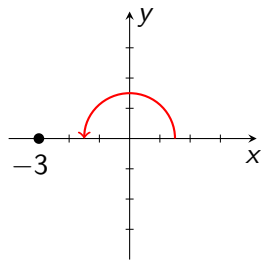
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$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

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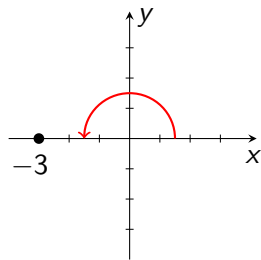
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$$(\sqrt{-3})_0 = \sqrt{3} \cdot \left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2} \right)$$

$$(\sqrt{-3})_0 = \sqrt{3}i$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

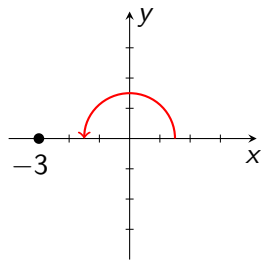
$$z = \sqrt{-3}$$

$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} + i \sin \frac{\pi + 2k\pi}{2} \right)$$

$$(\sqrt{-3})_0 = \sqrt{3} \cdot \left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2} \right)$$

$$(\sqrt{-3})_0 = \sqrt{3}i$$

$$(\sqrt{-3})_1 =$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

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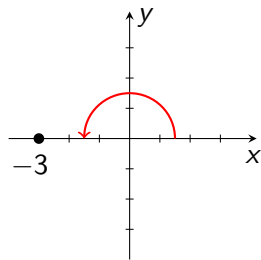
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$$(\sqrt{-3})_0 = \sqrt{3} \cdot \left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2} \right)$$

$$(\sqrt{-3})_0 = \sqrt{3}i$$

$$(\sqrt{-3})_1 = \sqrt{3} \cdot \left(\right)$$



$$r = 3 \quad \varphi = \pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$

$$z^2 = -3$$

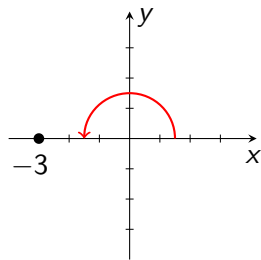
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$$(\sqrt{-3})_k = \sqrt{3} \cdot \left(\cos \frac{\pi + 2k\pi}{2} + i \sin \frac{\pi + 2k\pi}{2} \right)$$

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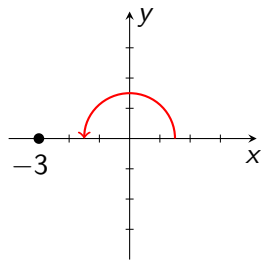
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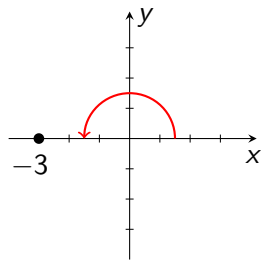
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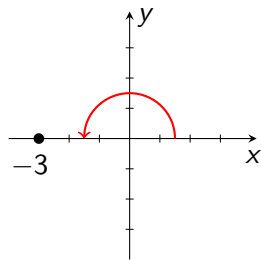
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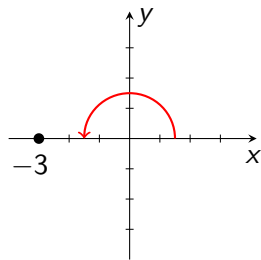
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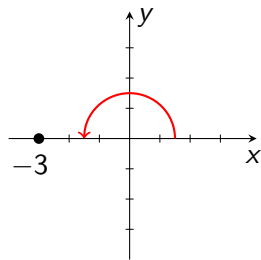
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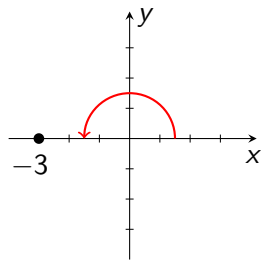
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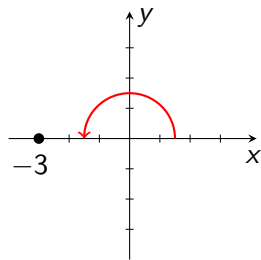
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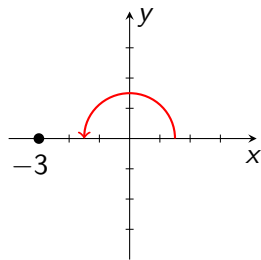
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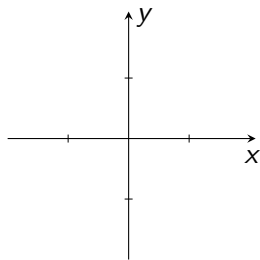
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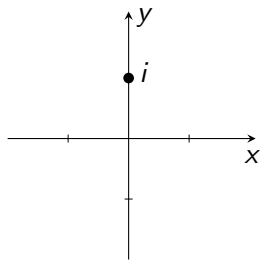
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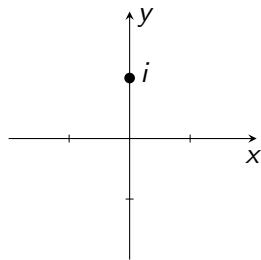
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$$r = 1$$

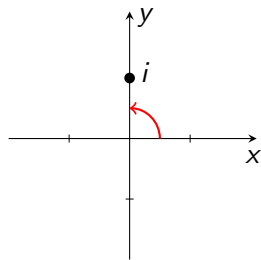
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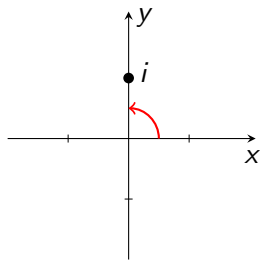
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$$z = \sqrt{i}$$

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$$r = 1$$

$$\varphi = \frac{\pi}{2}$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

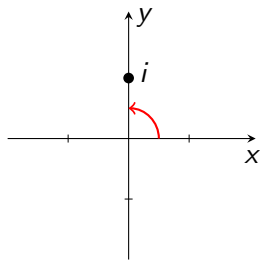
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

$$z^2 = i$$

$$z = \sqrt{i}$$

$$(\sqrt{i})_k =$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 1 \quad \varphi = \frac{\pi}{2}$$

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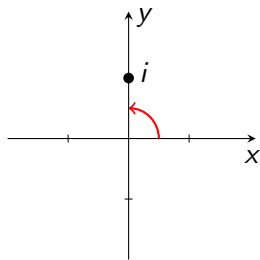
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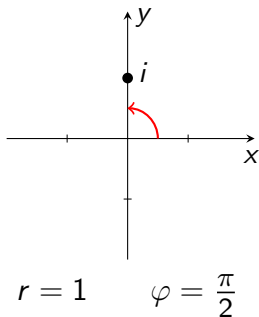
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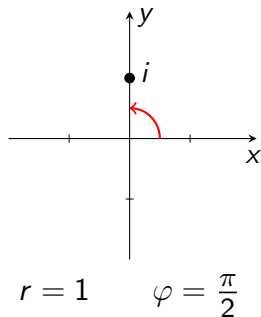
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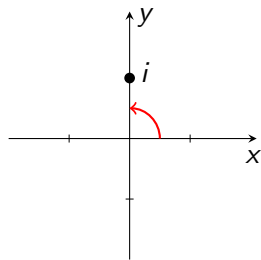
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$$(\sqrt{i})_k = \sqrt{1} \cdot \left(\cos \frac{\frac{\pi}{2} + 2k\pi}{2} + i \sin \frac{\frac{\pi}{2} + 2k\pi}{2} \right)$$



$$r = 1 \quad \varphi = \frac{\pi}{2}$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

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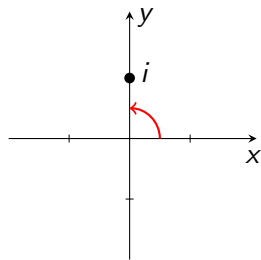
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$$(\sqrt{i})_0 =$$



$$r = 1 \quad \varphi = \frac{\pi}{2}$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

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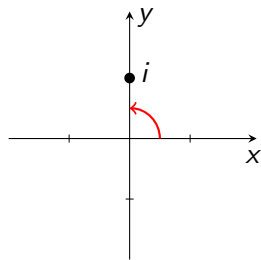
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$$(\sqrt{i})_0 = \cos \frac{\pi}{4}$$



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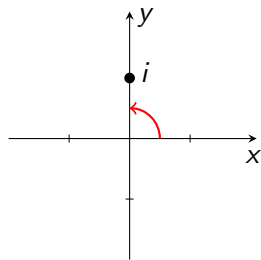
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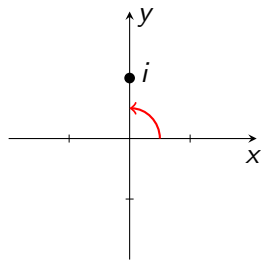
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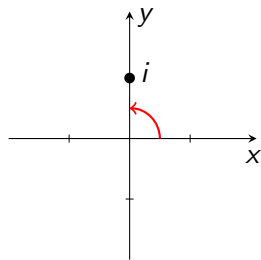
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$$(\sqrt{i})_0 =$$



$$r = 1 \quad \varphi = \frac{\pi}{2}$$

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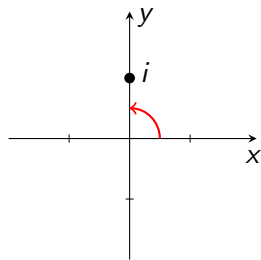
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$$(\sqrt{i})_0 = \cos \frac{\pi}{4} + i \sin \frac{\pi}{4}$$

$$(\sqrt{i})_0 = \frac{\sqrt{2}}{2}$$



$$r = 1 \quad \varphi = \frac{\pi}{2}$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$

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$$z^6 + 3z^4 + z^2 + 3 = 0$$

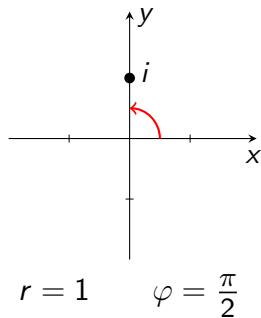
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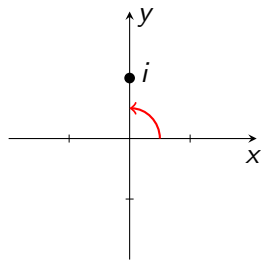
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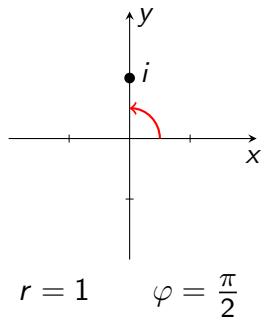
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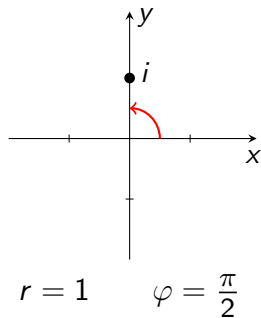
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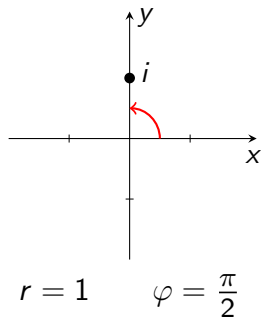
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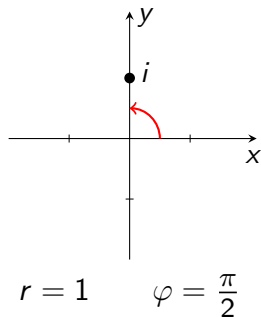
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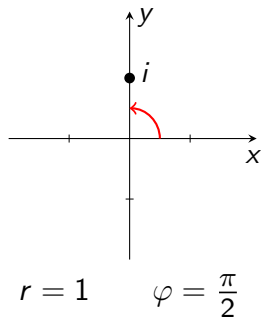
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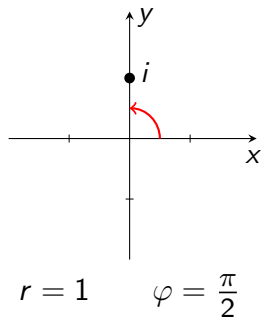
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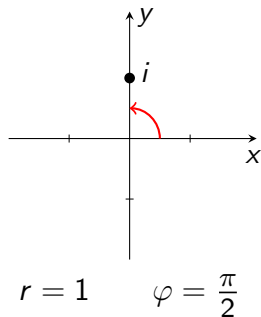
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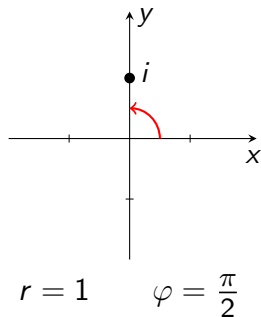
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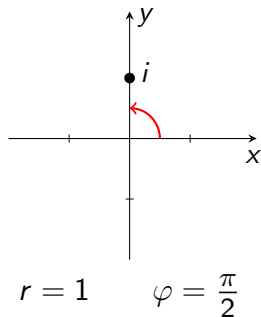
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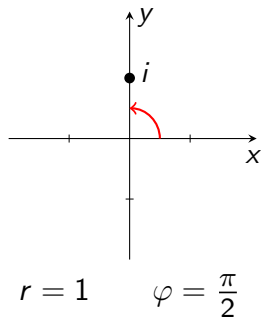
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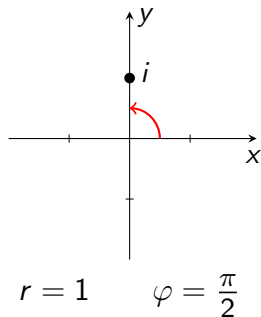
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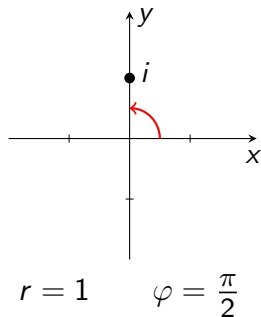
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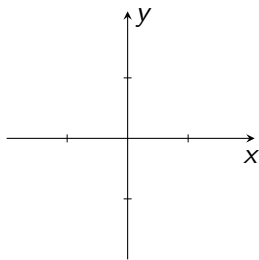
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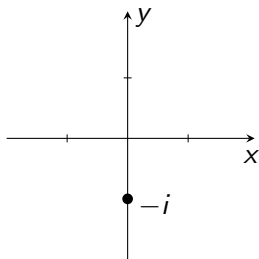
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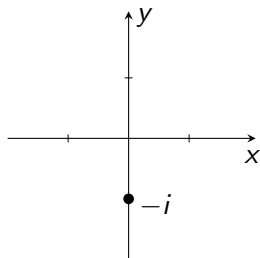
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$$r = 1$$

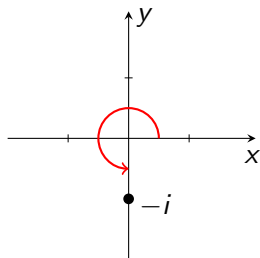
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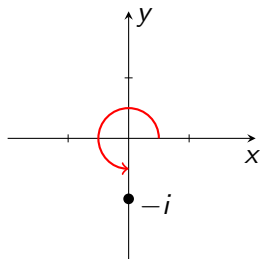
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$$z = \sqrt{-i}$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



$$r = 1 \quad \varphi = \frac{3}{2}\pi$$

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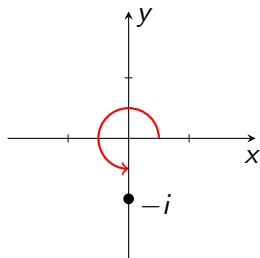
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$$z = \sqrt{-i}$$

$$(\sqrt{-i})_k =$$

$$z^6 + 3z^4 + z^2 + 3 = 0$$



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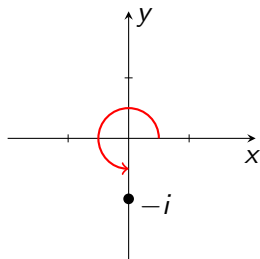
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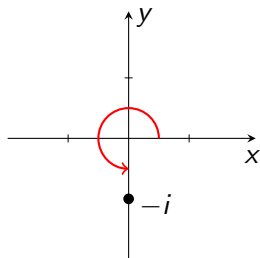
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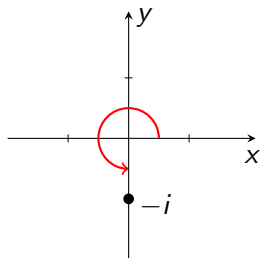
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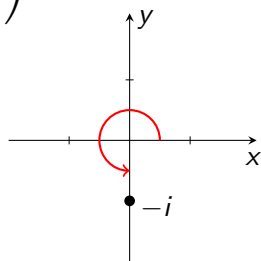
$$z^2 = t, \quad t_1 = -3, \quad t_2 = i, \quad t_3 = -i$$

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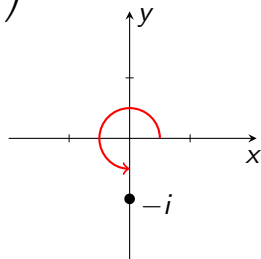
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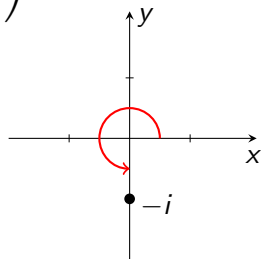
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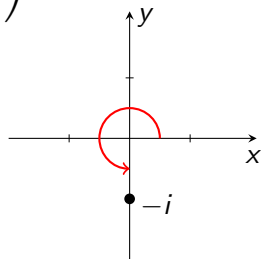
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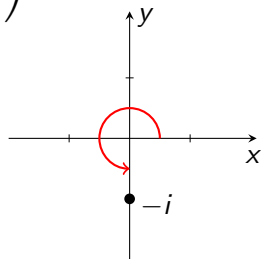
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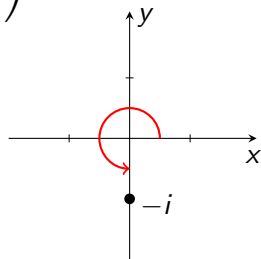
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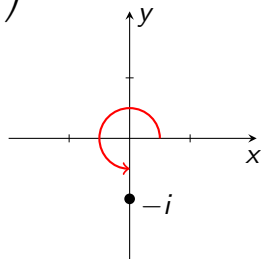
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$$(\sqrt{-i})_0 = -\frac{\sqrt{2}}{2}$$



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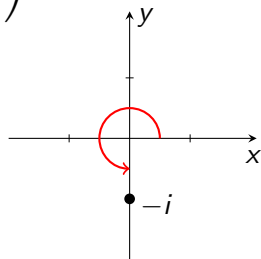
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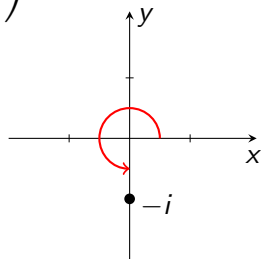
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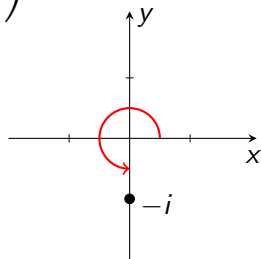
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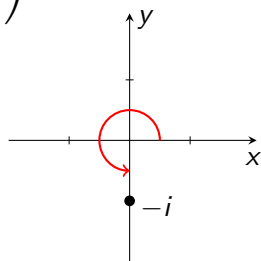
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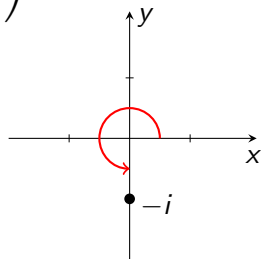
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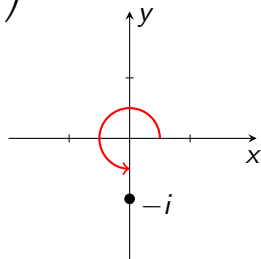
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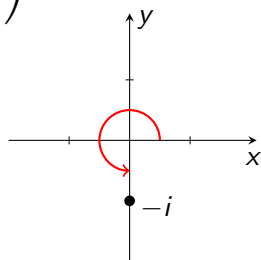
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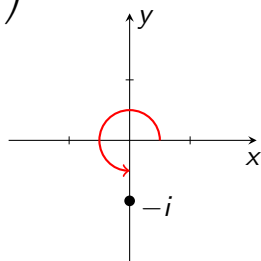
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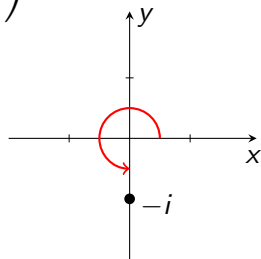
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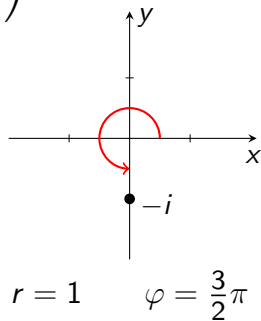
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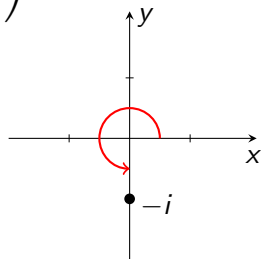
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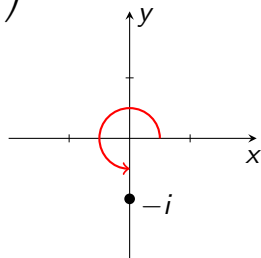
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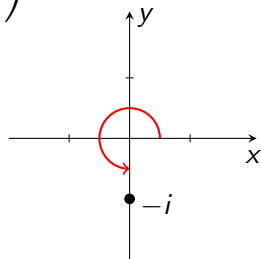
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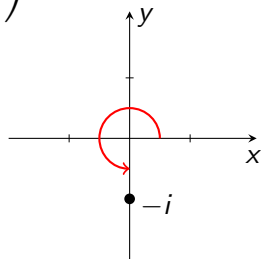
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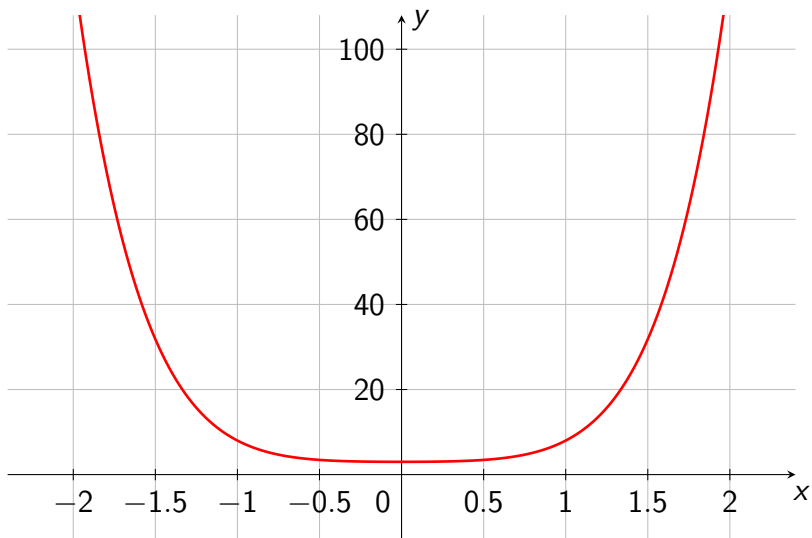
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$$r = 1 \quad \varphi = \frac{3}{2}\pi$$

$$\sqrt[n]{z} = \sqrt[n]{r} \left(\cos \frac{\varphi + 2k\pi}{n} + i \sin \frac{\varphi + 2k\pi}{n} \right)$$



$$f(x) = x^6 + 3x^4 + x^2 + 3$$