

# Seminari 4

## MATEMATIČKE METODE ZA INFORMATIČARE

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Damir Horvat

FOI, Varaždin

# Sadržaj

prvi zadatak

drugi zadatak

treći zadatak

četvrti zadatak

peti zadatak

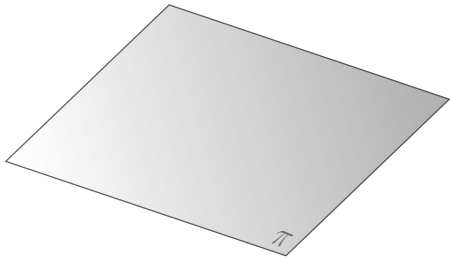
**prvi zadatak**

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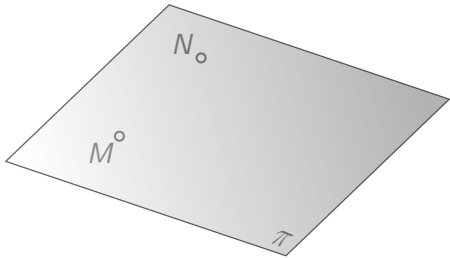
## Zadatak 1

*Odredite jednadžbu ravnine  $\pi$  koja prolazi točkama  $M(3, 4, -1)$ ,  $N(-2, -3, -2)$  i paralelna je s  $y$ -osi. Odredite točke u kojima ravnina  $\pi$  siječe preostale koordinatne osi.*

## Rješenje

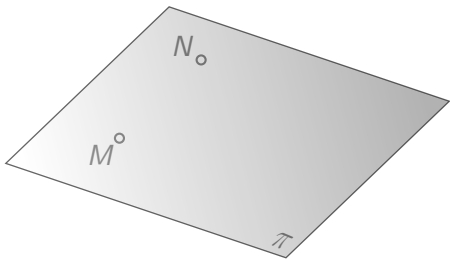


## Rješenje



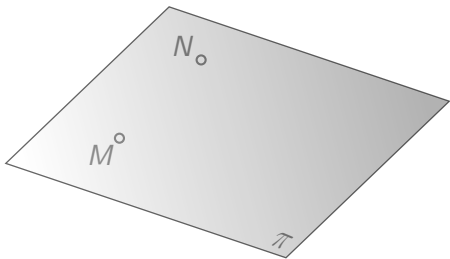
## Rješenje

$$M(3, 4, -1), \quad N(-2, -3, -2)$$



## Rješenje

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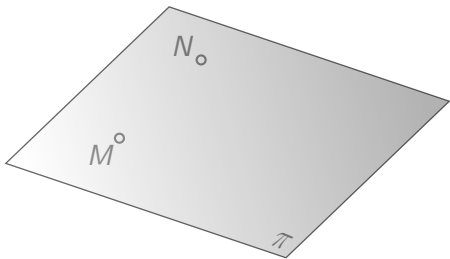


## Rješenje

y-os

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$$M(3, 4, -1), \quad N(-2, -3, -2)$$

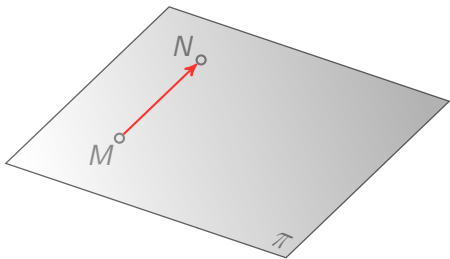


## Rješenje

y-os

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$$M(3, 4, -1), \quad N(-2, -3, -2)$$

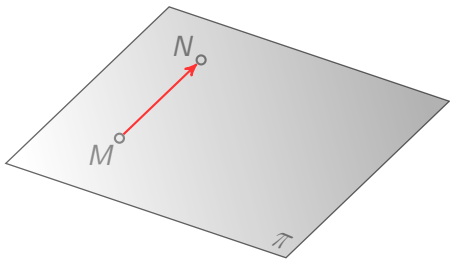


## Rješenje

y-os

$\vec{j}$

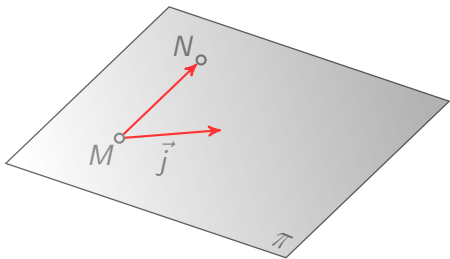
$$M(3, 4, -1), \quad N(-2, -3, -2)$$



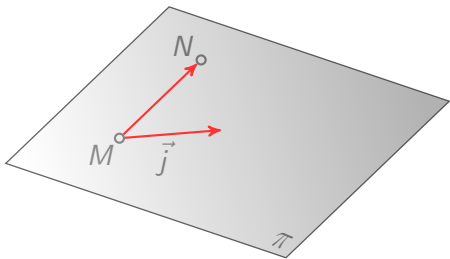
# Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$



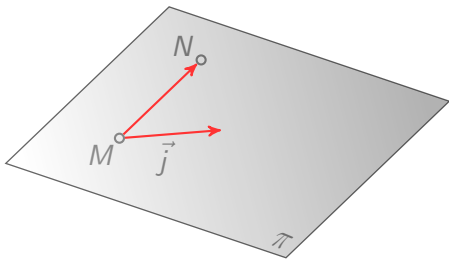
## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

Parametarske jednadžbe

## Rješenje

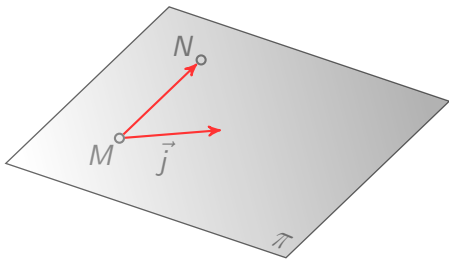


$$M(3, 4, -1), \quad N(-2, -3, -2)$$

Parametarske jednadžbe

$\pi \dots$

## Rješenje

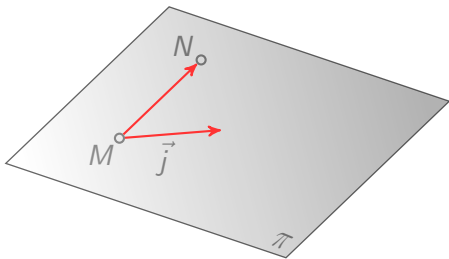


$$M(3, 4, -1), \quad N(-2, -3, -2)$$

Parametarske jednadžbe

$$\pi \dots M,$$

## Rješenje



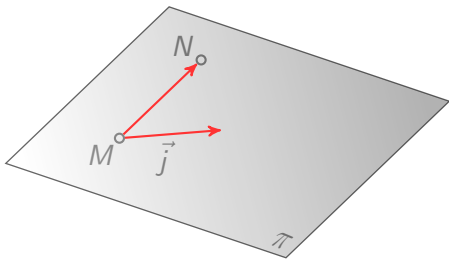
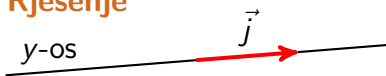
$$M(3, 4, -1), \quad N(-2, -3, -2)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN},$$



## Rješenje

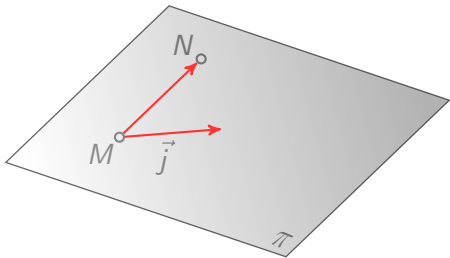
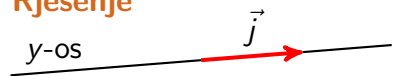


$$M(3, 4, -1), \quad N(-2, -3, -2)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

## Rješenje



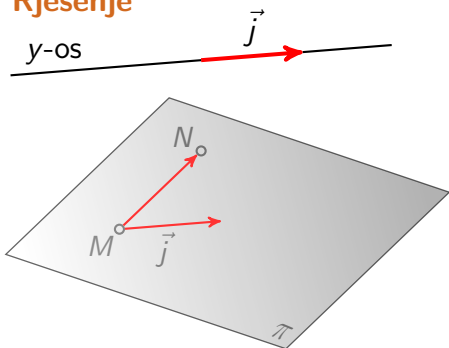
$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} =$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

## Rješenje



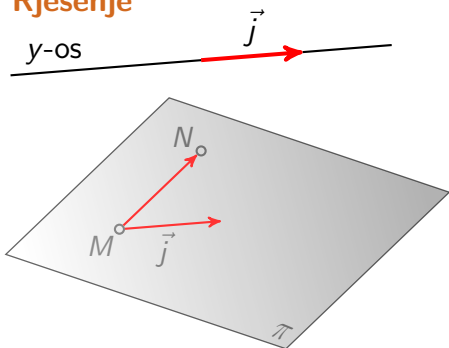
$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

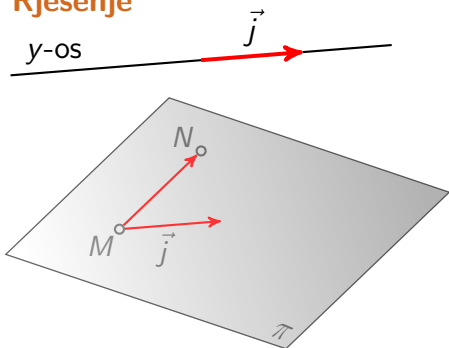
$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} =$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

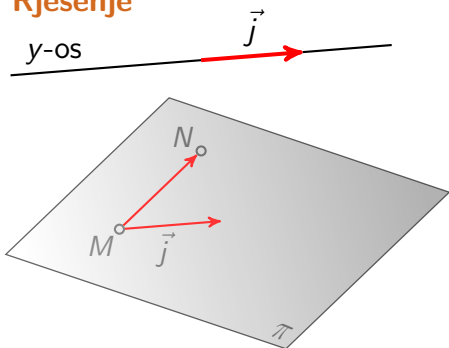
$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

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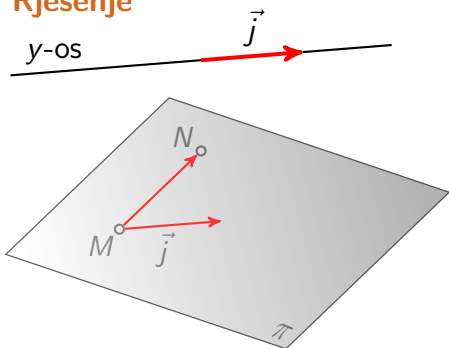
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \left\{ \right.$$

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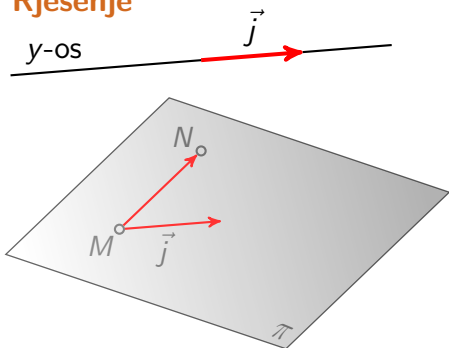
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = \\ y = \\ z = \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} = (0, 1, 0)$$

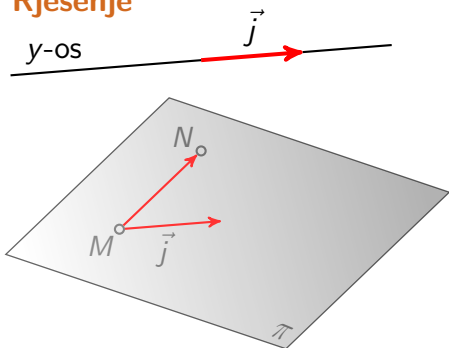
Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 \\ y = 4 \\ z = -1 \end{cases}$$



## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

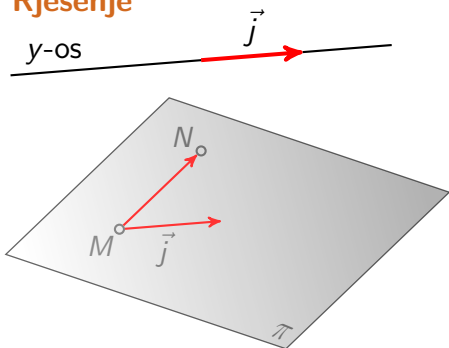
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + \\ y = 4 + \\ z = -1 + \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

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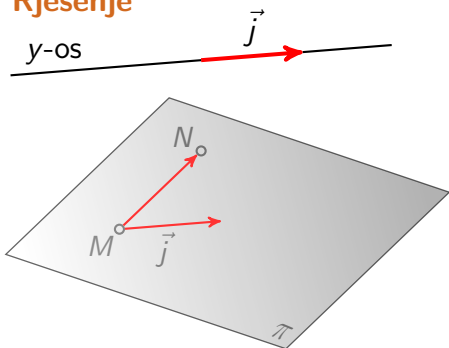
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \\ y = 4 + (-7) \\ z = -1 + (-1) \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

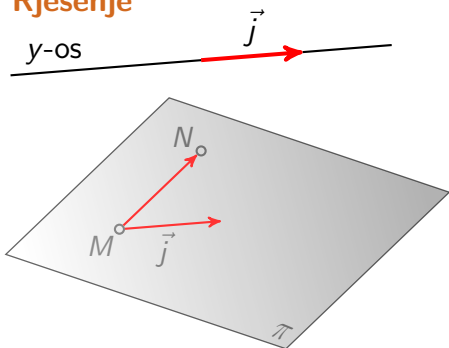
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u \\ y = 4 + (-7) \cdot u \\ z = -1 + (-1) \cdot u \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

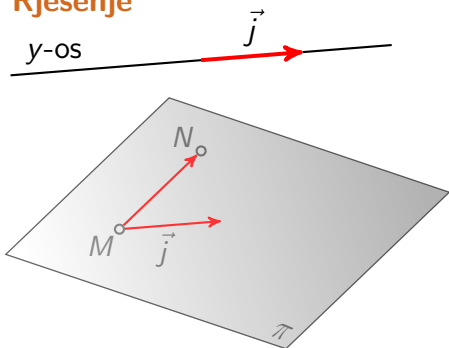
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + \\ y = 4 + (-7) \cdot u + \\ z = -1 + (-1) \cdot u + \end{cases}$$

## Rješenje



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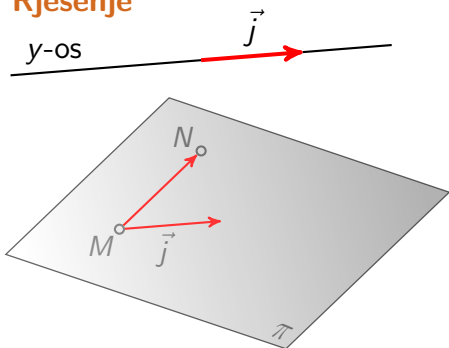
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + 0 \\ y = 4 + (-7) \cdot u + 1 \\ z = -1 + (-1) \cdot u + 0 \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

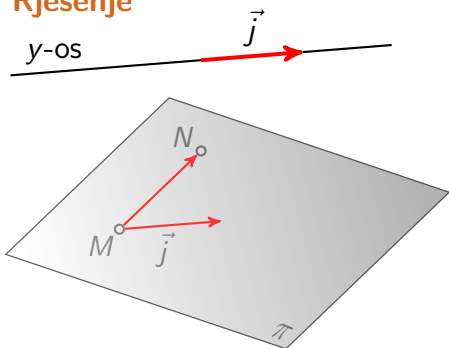
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + 0 \cdot v \\ y = 4 + (-7) \cdot u + 1 \cdot v \\ z = -1 + (-1) \cdot u + 0 \cdot v \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

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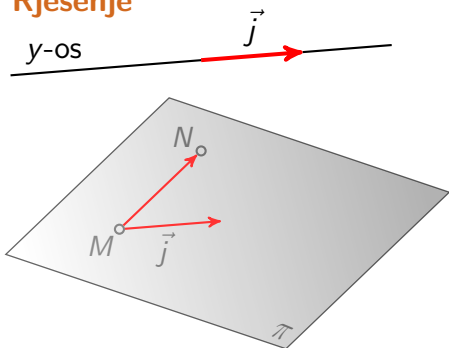
Parametarske jednadžbe

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$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + 0 \cdot v \\ y = 4 + (-7) \cdot u + 1 \cdot v \\ z = -1 + (-1) \cdot u + 0 \cdot v \end{cases}$$

$$\pi \dots \left\{ \right.$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

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Parametarske jednadžbe

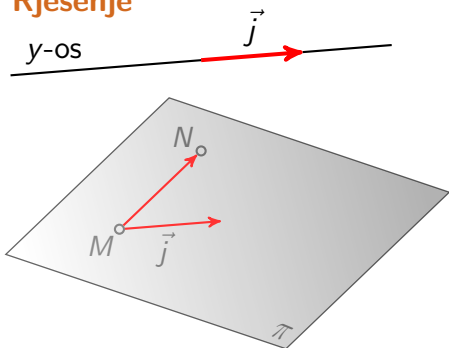
$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + 0 \cdot v \\ y = 4 + (-7) \cdot u + 1 \cdot v \\ z = -1 + (-1) \cdot u + 0 \cdot v \end{cases}$$

$$\pi \dots \begin{cases} x = 3 - 5u \end{cases}$$



## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} = (0, 1, 0)$$

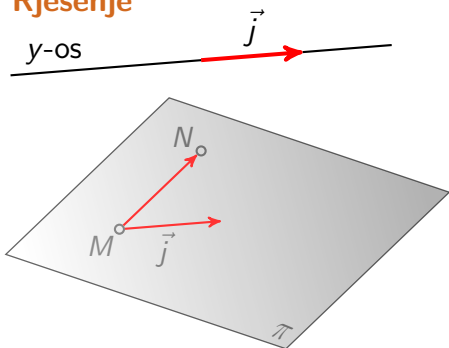
Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + 0 \cdot v \\ y = 4 + (-7) \cdot u + 1 \cdot v \\ z = -1 + (-1) \cdot u + 0 \cdot v \end{cases}$$

$$\pi \dots \begin{cases} x = 3 - 5u \\ y = 4 - 7u + v \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} = (0, 1, 0)$$

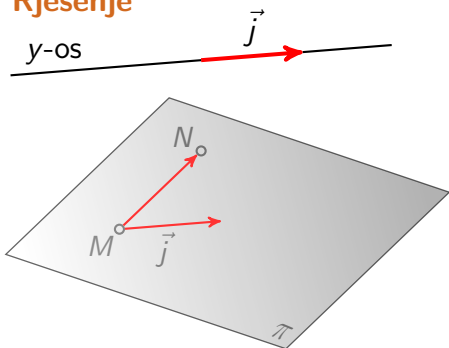
Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

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$$\pi \dots \begin{cases} x = 3 - 5u \\ y = 4 - 7u + v \\ z = -1 - u \end{cases}$$

## Rješenje



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

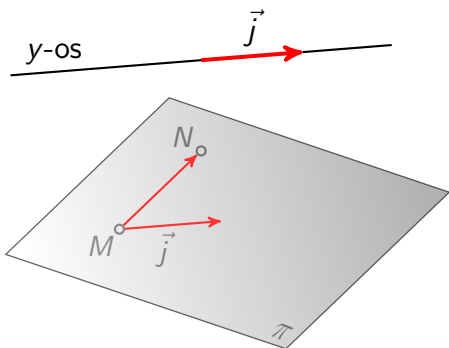
$$\vec{j} = (0, 1, 0)$$

Parametarske jednadžbe

$$\pi \dots M, \overrightarrow{MN}, \vec{j}$$

$$\pi \dots \begin{cases} x = 3 + (-5) \cdot u + 0 \cdot v \\ y = 4 + (-7) \cdot u + 1 \cdot v \\ z = -1 + (-1) \cdot u + 0 \cdot v \end{cases}$$

$$\pi \dots \begin{cases} x = 3 - 5u \\ y = 4 - 7u + v \\ z = -1 - u \end{cases} \quad u, v \in \mathbb{R}$$

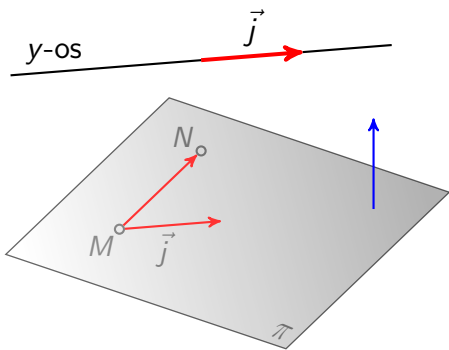


$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} = (0, 1, 0)$$

Opční oblik

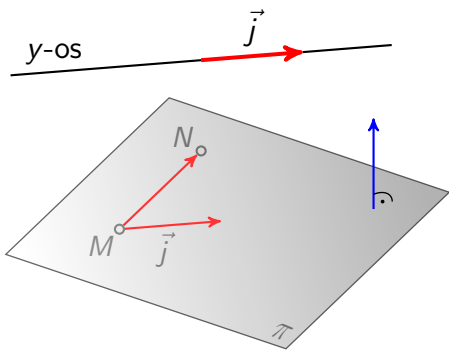


$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

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Opční oblik

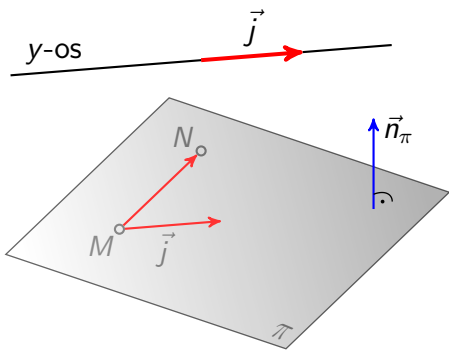


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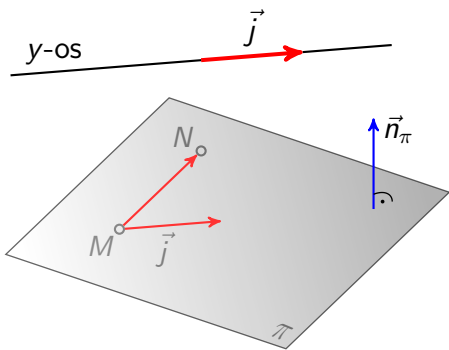


$$M(3, 4, -1), N(-2, -3, -2)$$

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Opční oblik



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

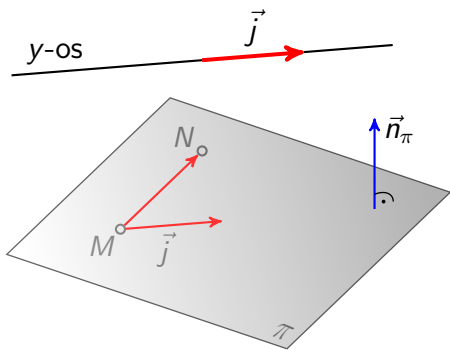
$$\overrightarrow{MN} = (-5, -7, -1)$$

$$\vec{j} = (0, 1, 0)$$

Opční oblik

$\pi \dots$





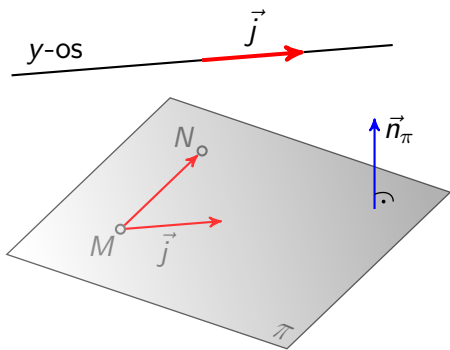
$$M(3, 4, -1), N(-2, -3, -2)$$

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Opční oblik

$\pi \dots M,$



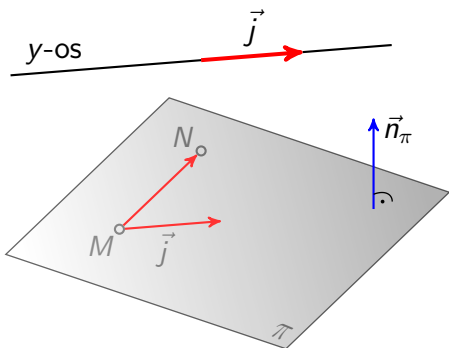
$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

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Opční oblik

$$\pi \dots M, \vec{n}_\pi$$



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

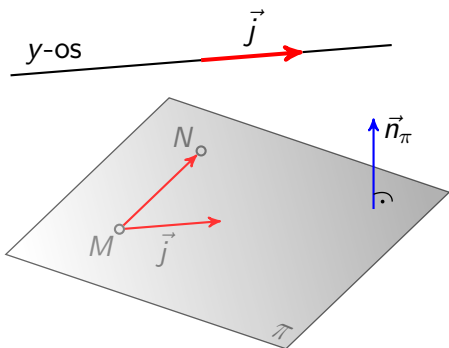
$$\overrightarrow{MN} = (-5, -7, -1)$$

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Opční oblik

$$\pi \dots M, \vec{n}_\pi$$

$$\vec{n}_\pi = \vec{j} \times \overrightarrow{MN}$$



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

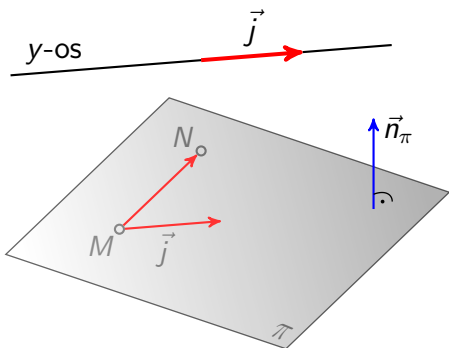
$$\overrightarrow{MN} = (-5, -7, -1)$$

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Opční oblik

$$\pi \dots M, \vec{n}_\pi$$

$$\vec{n}_\pi = \vec{j} \times \overrightarrow{MN} = \left| \begin{array}{ccc} & & \\ & & \\ & & \end{array} \right|$$



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

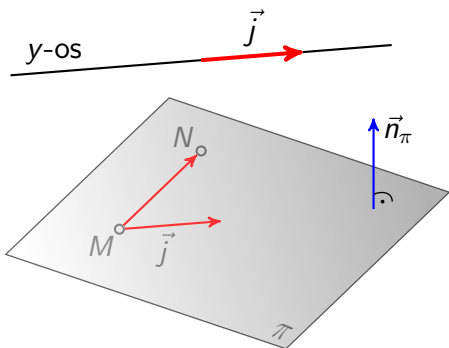
$$\overrightarrow{MN} = (-5, -7, -1)$$

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Opční oblik

$$\pi \dots M, \vec{n}_\pi$$

$$\vec{n}_\pi = \vec{j} \times \overrightarrow{MN} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 1 & 0 \\ -5 & -7 & -1 \end{vmatrix}$$



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

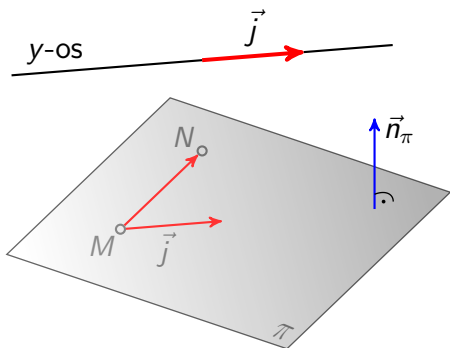
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Opční oblik

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$$\vec{n}_\pi = \vec{j} \times \overrightarrow{MN} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 1 & 0 \end{vmatrix}$$



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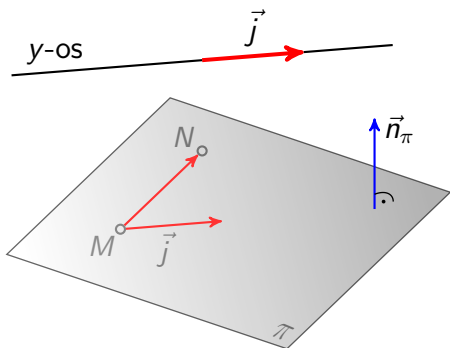
$$\overrightarrow{MN} = (-5, -7, -1)$$

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Opční oblik

$$\pi \dots M, \vec{n}_\pi$$

$$\vec{n}_\pi = \vec{j} \times \overrightarrow{MN} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 1 & 0 \\ -5 & -7 & -1 \end{vmatrix}$$



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

$$\overrightarrow{MN} = (-5, -7, -1)$$

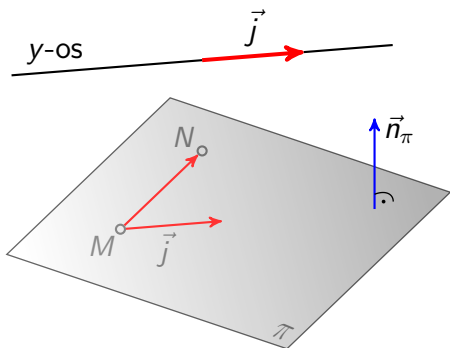
$$\vec{j} = (0, 1, 0)$$

Opční oblik

$$\pi \dots M, \vec{n}_\pi$$

$$\vec{n}_\pi = \vec{j} \times \overrightarrow{MN} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 1 & 0 \\ -5 & -7 & -1 \end{vmatrix} = ($$





$$M(3, 4, -1), \quad N(-2, -3, -2)$$

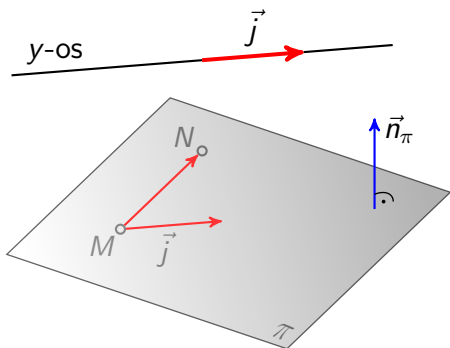
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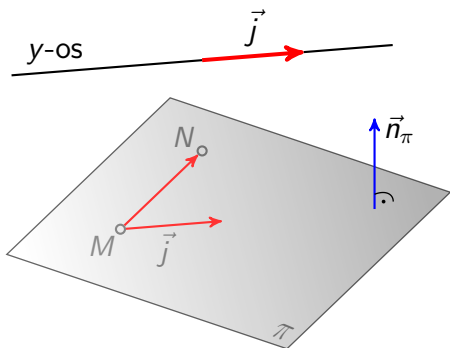
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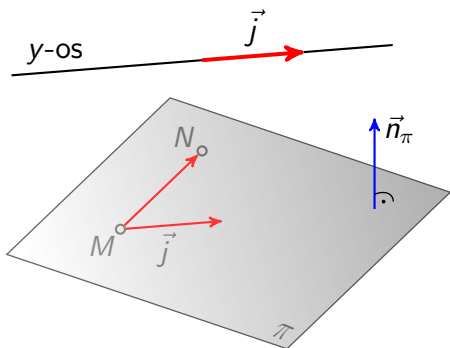
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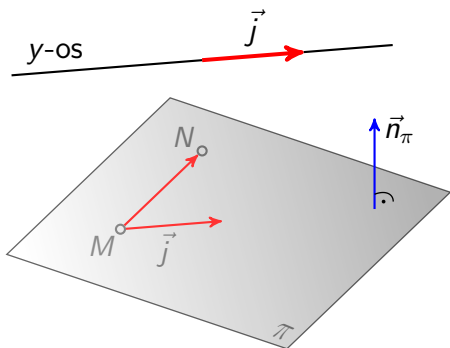
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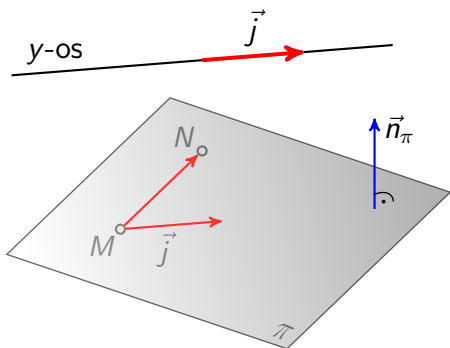
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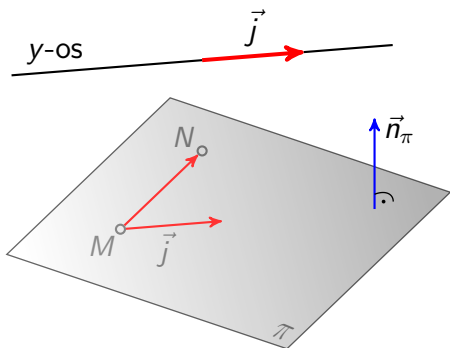
Opční oblik

$$M(x_0, y_0, z_0) \\ M(3, 4, -1)$$

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Opční oblik

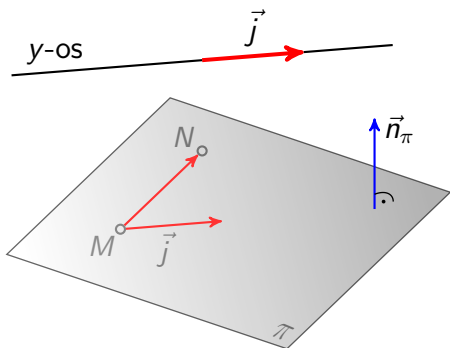
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Opční oblik

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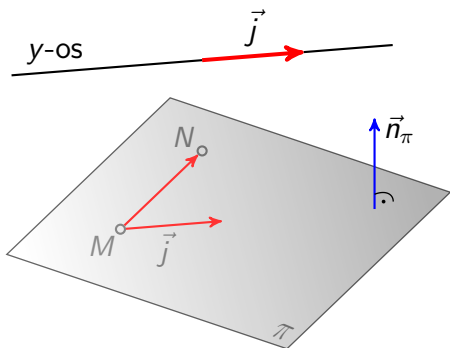
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$$-1 \cdot (x -$$





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Opční oblik

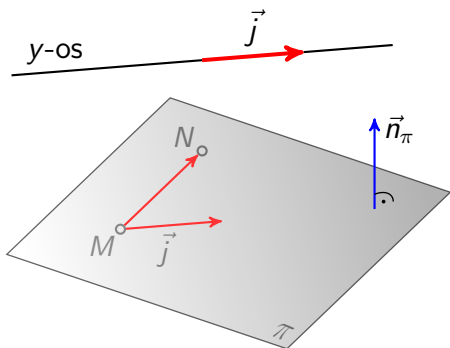
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$$A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$-1 \cdot (x - 3)$$



$$M(3, 4, -1), \quad N(-2, -3, -2)$$

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Opční oblik

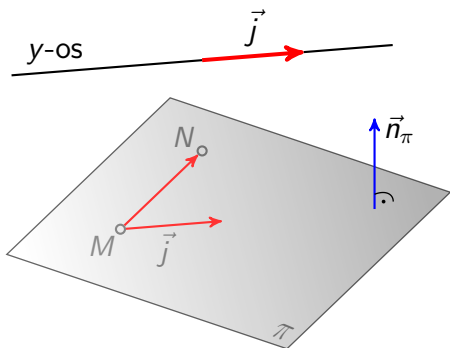
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$$A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$-1 \cdot (x - 3) + 0 \cdot$$



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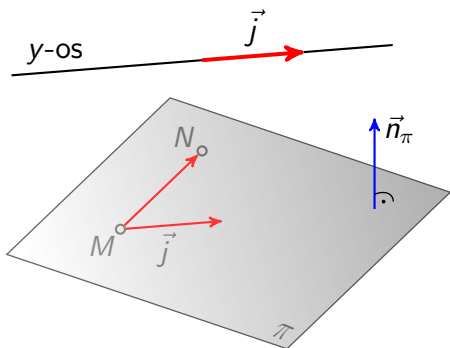
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$$-1 \cdot (x - 3) + 0 \cdot (y -$$



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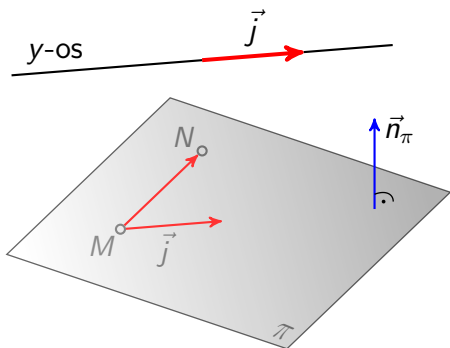
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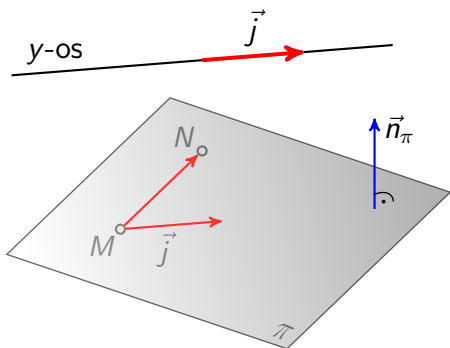
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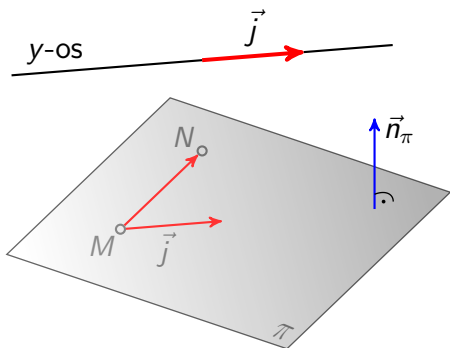
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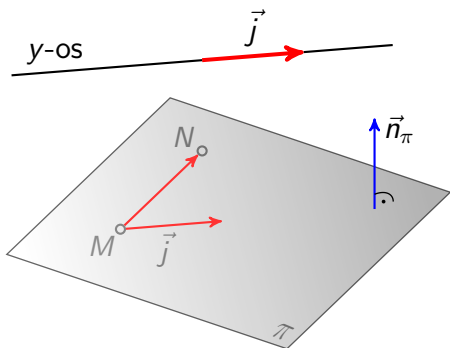
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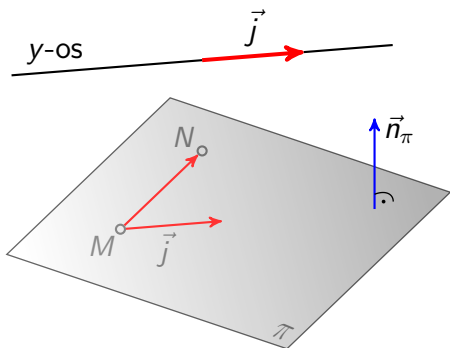
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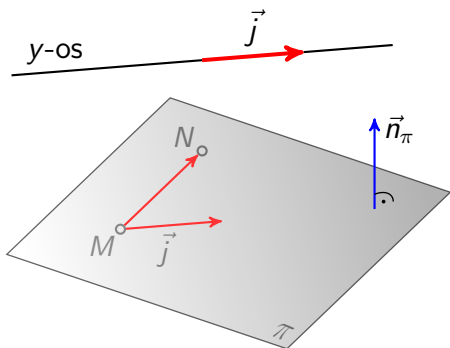
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$$-x + 5z + 8 = 0$$



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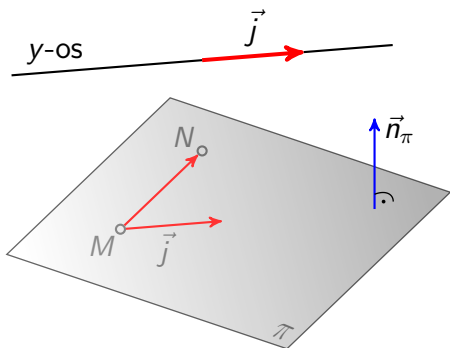
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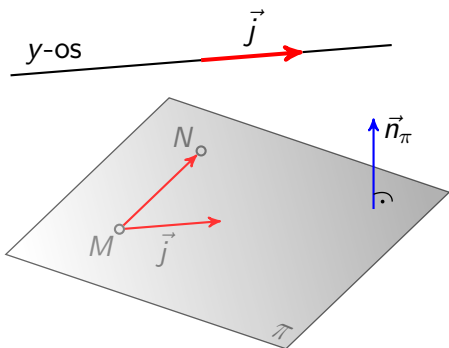
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Ova ravnina nema segmentni oblik

$$A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

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$$\pi \dots -x + 5z + 8 = 0$$

## Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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$$Ax + By + Cz + D = 0$$

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$$\vec{n}_\pi = (\overset{A}{-1}, \overset{B}{0}, \overset{C}{5})$$

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$$Ax + By + Cz + D = 0$$

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$$\vec{n}_\pi = (\overset{A}{-1}, \overset{B}{0}, \overset{C}{5}) \quad D = 8$$

$$\lambda = \frac{1}{-\text{sign } D \cdot \sqrt{A^2 + B^2 + C^2}}$$

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$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

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$$Ax + By + Cz + D = 0$$

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$$\lambda = \frac{1}{-\text{sign } D \cdot \sqrt{A^2 + B^2 + C^2}}$$

$$\lambda = \frac{1}{-8 \cdot \sqrt{1 + 0 + 25}} = \frac{1}{-8 \cdot 5} = -\frac{1}{40}$$

### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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$$\vec{n}_\pi = (\overset{A}{-1}, \overset{B}{0}, \overset{C}{5}) \quad D = 8$$

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$$\lambda = \frac{1}{\phantom{\sqrt{A^2 + B^2 + C^2}}}$$

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$$\lambda = \frac{1}{-\text{sign } 8 \cdot \sqrt{(-1)^2}}$$

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$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

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$$Ax + By + Cz + D = 0$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

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$$Ax + By + Cz + D = 0$$

$$-x + 5z + 8 = 0$$

$$\vec{n}_\pi = (\overset{A}{-1}, \overset{B}{0}, \overset{C}{5}) \quad D = 8$$

$$\lambda = \frac{1}{-\text{sign } D \cdot \sqrt{A^2 + B^2 + C^2}}$$

$$\lambda = \frac{1}{-\text{sign } 8 \cdot \sqrt{(-1)^2 + 0^2 + 5^2}}$$

### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

$$-x + 5z + 8 = 0$$

$$\vec{n}_\pi = (\overset{A}{-1}, \overset{B}{0}, \overset{C}{5}) \quad D = 8$$

$$\lambda = \frac{1}{-\text{sign } D \cdot \sqrt{A^2 + B^2 + C^2}}$$

$$\lambda = \frac{1}{-\text{sign } 8 \cdot \sqrt{(-1)^2 + 0^2 + 5^2}}$$

$$\lambda =$$

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$$\lambda = \frac{1}{-8 \cdot \sqrt{26}}$$

### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

### Opći oblik

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$$\lambda = \frac{1}{-1}$$

### Normalni oblik

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

$$-x + 5z + 8 = 0$$

$$\vec{n}_\pi = \begin{matrix} A & B & C \\ (-1, & 0, & 5) \end{matrix} \quad D = 8$$

$$\lambda = \frac{1}{-\text{sign } D \cdot \sqrt{A^2 + B^2 + C^2}}$$

$$\lambda = \frac{1}{-\text{sign } 8 \cdot \sqrt{(-1)^2 + 0^2 + 5^2}}$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z$$

### Opći oblik

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}}$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

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$$\lambda = \frac{1}{-1 \cdot \sqrt{26}}$$

$$\lambda = \frac{-1}{\sqrt{26}}$$



### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

### Opći oblik

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}}$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}}$$

$$\cos \beta = 0$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}}$$

$$\cos \beta = 0$$

$$\cos \gamma = -\frac{5}{\sqrt{26}}$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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$$\vec{n}_\pi = \begin{matrix} A & B & C \\ (-1, & 0, & 5) \end{matrix} \quad D = 8$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}}$$

$$\cos \beta = 0$$

$$\cos \gamma = -\frac{5}{\sqrt{26}}$$

$$\delta = \frac{8}{\sqrt{26}}$$

### Opći oblik

$$Ax + By + Cz + D = 0$$

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### Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

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$$Ax + By + Cz + D = 0$$

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## Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}}$$

$$\cos \beta = 0$$

$$\cos \gamma = -\frac{5}{\sqrt{26}}$$

$$\delta = \frac{8}{\sqrt{26}}$$

udaljenost ravnine  
od ishodišta

## Opći oblik

$$Ax + By + Cz + D = 0$$

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## Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}}$$

$$\cos \beta = 0$$

$$\cos \gamma = -\frac{5}{\sqrt{26}}$$

$$\delta = \frac{8}{\sqrt{26}}$$

udaljenost ravnine  
od ishodišta

## Opći oblik

$$Ax + By + Cz + D = 0$$

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$$\lambda = \frac{1}{-1 \cdot \sqrt{26}}$$

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## Normalni oblik

$$x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

$$-x + 5z + 8 = 0 \quad / \cdot \frac{-1}{\sqrt{26}}$$

$$\frac{1}{\sqrt{26}}x - \frac{5}{\sqrt{26}}z - \frac{8}{\sqrt{26}} = 0$$

$$\cos \alpha = \frac{1}{\sqrt{26}} \quad \vec{n}_0 = -\frac{1}{\sqrt{26}} \vec{n}_\pi$$

$$\cos \beta = 0$$

kosinusi smjera od  $\vec{n}_0$  i od  $-\vec{n}_\pi$

$$\cos \gamma = -\frac{5}{\sqrt{26}}$$

$$\delta = \frac{8}{\sqrt{26}}$$

udaljenost ravnine od ishodišta

## Opći oblik

$$Ax + By + Cz + D = 0$$

$$-x + 5z + 8 = 0$$

$$\vec{n}_\pi = \begin{matrix} A & B & C \\ (-1, & 0, & 5) \end{matrix} \quad D = 8$$

$$\lambda = \frac{1}{-\text{sign } D \cdot \sqrt{A^2 + B^2 + C^2}}$$

$$\lambda = \frac{1}{-\text{sign } 8 \cdot \sqrt{(-1)^2 + 0^2 + 5^2}}$$

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$$\lambda = \frac{-1}{\sqrt{26}}$$

$\pi \cap X\text{-OS}$

$\pi \cap x\text{-os}$

$$\pi \dots -x + 5z + 8 = 0$$

$$\pi \cap X\text{-OS}$$

$$\pi \dots -x + 5z + 8 = 0$$

$$X\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$\pi \cap X\text{-OS}$

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$\pi \cap X\text{-OS}$

$$\pi \dots -x + 5z + 8 = 0$$

$$X\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$$-x + 5z + 8 = 0$$

$$-t + 5 \cdot 0 + 8 = 0$$

$\pi \cap X\text{-OS}$

$$\pi \dots -x + 5z + 8 = 0$$

$$X\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$$-x + 5z + 8 = 0$$

$$-t + 5 \cdot 0 + 8 = 0$$

$$t = 8$$

$\pi \cap x\text{-OS}$

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$$-x + 5z + 8 = 0$$

$$-t + 5 \cdot 0 + 8 = 0$$

$$t = 8$$

$$T_1(8, 0, 0)$$



$\pi \cap x\text{-OS}$  $\pi \cap z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$x\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$$-x + 5z + 8 = 0$$

$$-t + 5 \cdot 0 + 8 = 0$$

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$$T_1(8, 0, 0)$$

$\pi \cap x\text{-OS}$ 

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$$x\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$$-x + 5z + 8 = 0$$

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$$t = 8$$

$$T_1(8, 0, 0)$$

 $\pi \cap z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$\pi \cap X\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$X\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$$-x + 5z + 8 = 0$$

$$-t + 5 \cdot 0 + 8 = 0$$

$$t = 8$$

$$T_1(8, 0, 0)$$

 $\pi \cap Z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$Z\text{-OS} \dots \begin{cases} x = 0 \\ y = 0 \\ z = t \end{cases}$$

$\pi \cap x\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$x\text{-OS} \dots \begin{cases} x = t \\ y = 0 \\ z = 0 \end{cases}$$

$$-x + 5z + 8 = 0$$

$$-t + 5 \cdot 0 + 8 = 0$$

$$t = 8$$

$$T_1(8, 0, 0)$$

 $\pi \cap z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$z\text{-OS} \dots \begin{cases} x = 0 \\ y = 0 \\ z = t \end{cases}$$

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$$\pi \dots -x + 5z + 8 = 0$$

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$$T_1(8, 0, 0)$$

 $\pi \cap z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

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 $\pi \cap Z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$Z\text{-OS} \dots \begin{cases} x = 0 \\ y = 0 \\ z = t \end{cases}$$

$$-x + 5z + 8 = 0$$

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$$t = -\frac{8}{5}$$

$\pi \cap X\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

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$$t = 8$$

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 $\pi \cap Z\text{-OS}$ 

$$\pi \dots -x + 5z + 8 = 0$$

$$Z\text{-OS} \dots \begin{cases} x = 0 \\ y = 0 \\ z = t \end{cases}$$

$$-x + 5z + 8 = 0$$

$$0 + 5t + 8 = 0$$

$$t = -\frac{8}{5}$$

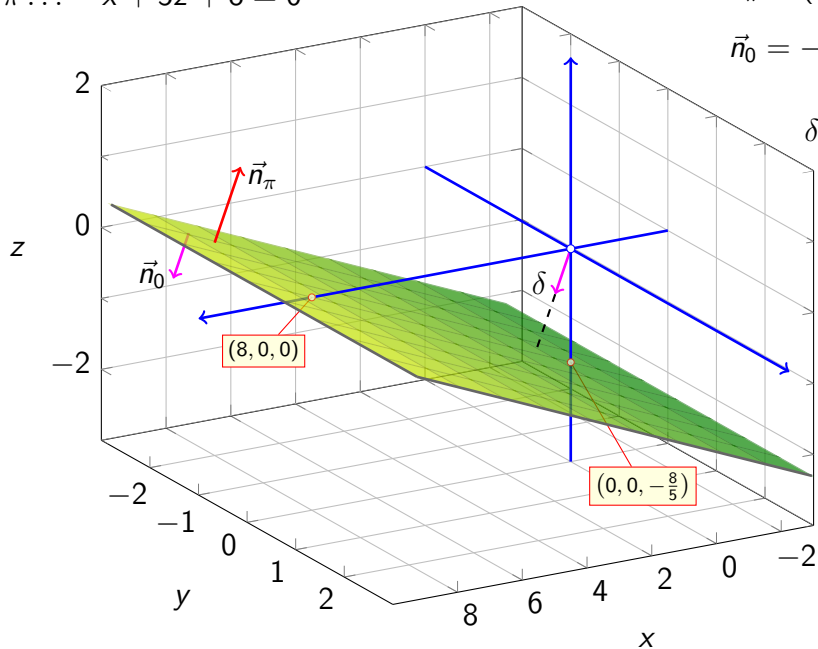
$$T_2\left(0, 0, -\frac{8}{5}\right)$$

$$\pi \dots -x + 5z + 8 = 0$$

$$\vec{n}_\pi = (-1, 0, 5)$$

$$\vec{n}_0 = -\frac{1}{\sqrt{26}} \vec{n}_\pi$$

$$\delta = \frac{8}{\sqrt{26}}$$





# Domaća zadaća

Odredite vrijednosti parametara  $u$  i  $v$  za koje se dobivaju presjeci ravnine  $\pi$  s koordinatnim osima u njezinim parametarskim jednadžbama

$$\pi \dots \begin{cases} x = 3 - 5u \\ y = 4 - 7u + v. \\ z = -1 - u \end{cases}$$

# Domaća zadaća

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$$\pi \dots \begin{cases} x = 3 - 5u \\ y = 4 - 7u + v. \\ z = -1 - u \end{cases}$$

$$T_1(8, 0, 0)$$

## Domaća zadaća

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$$T_1(8, 0, 0) \rightsquigarrow u = -1, v = -11$$

# Domaća zadaća

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$$T_1(8, 0, 0) \rightsquigarrow u = -1, v = -11$$

$$T_2\left(0, 0, -\frac{8}{5}\right)$$

# Domaća zadaća

Odredite vrijednosti parametara  $u$  i  $v$  za koje se dobivaju presjeci ravnine  $\pi$  s koordinatnim osima u njezinim parametarskim jednadžbama

$$\pi \dots \begin{cases} x = 3 - 5u \\ y = 4 - 7u + v. \\ z = -1 - u \end{cases}$$

$$T_1(8, 0, 0) \rightsquigarrow u = -1, v = -11$$

$$T_2\left(0, 0, -\frac{8}{5}\right) \rightsquigarrow u = \frac{3}{5}, v = \frac{1}{5}$$

**drugi zadatak**

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## Zadatak 2

Nađite jednadžbu ravnine čija je normala  $\vec{n} = 8\vec{i} + 9\vec{j} + \vec{k}$ , a udaljenost od ishodišta iznosi 1.

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## Rješenje

1. način



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## Rješenje

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$$\pi \dots x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

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1. način  $\vec{n} = (8, 9, 1)$

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## Rješenje

1. način  $\vec{n} = (8, 9, 1), \delta = 1$

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Podrazumijevamo da se od ishodišta pomičemo u smjeru zadane normale poštujući njezinu orijentaciju jer u protivnom postoje dvije takve ravnine.

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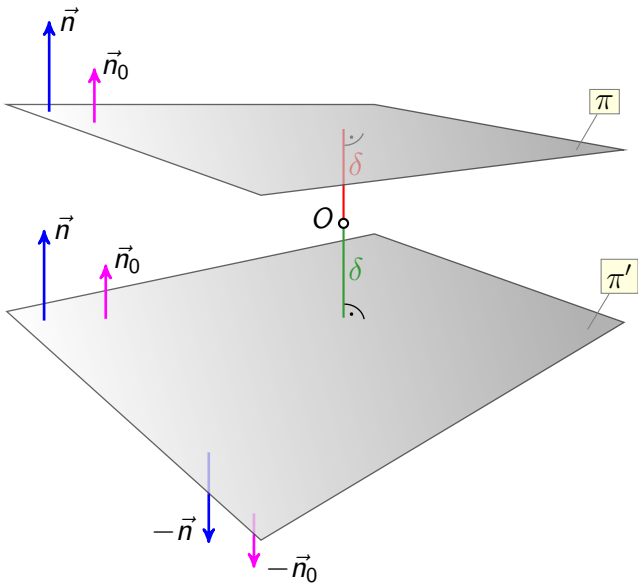
$$|\vec{n}| = \sqrt{8^2 + 9^2 + 1^2}$$

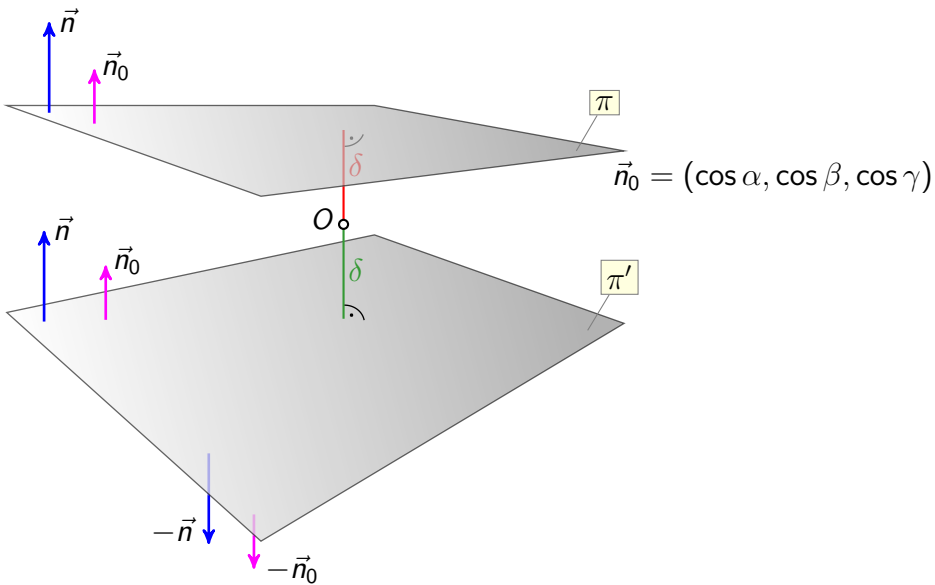
$$\pi \dots x \cos \alpha + y \cos \beta + z \cos \gamma - \delta = 0$$

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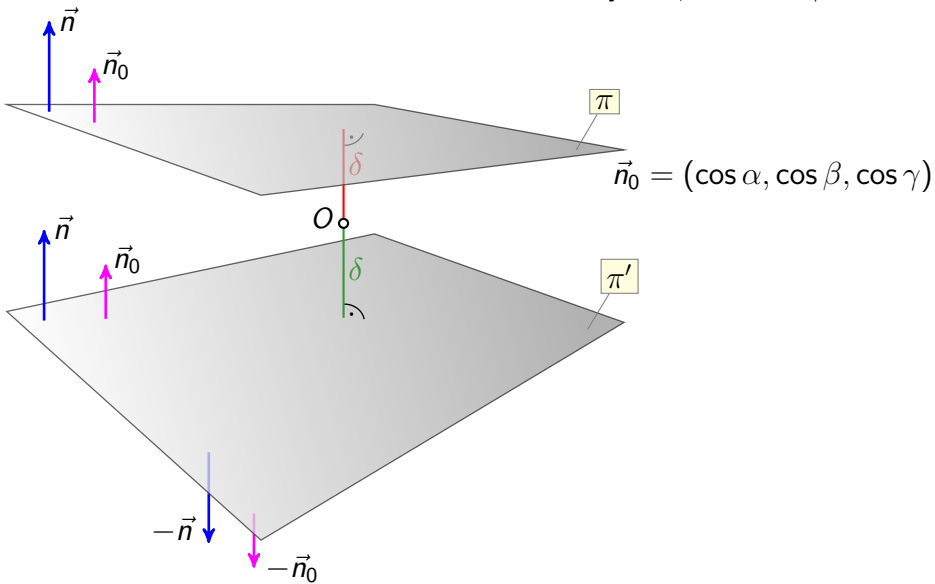
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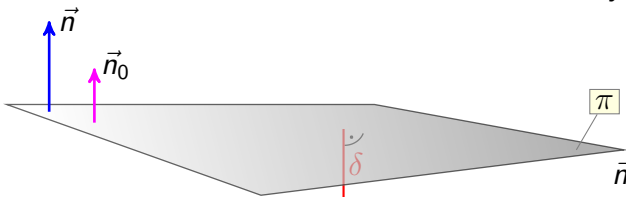


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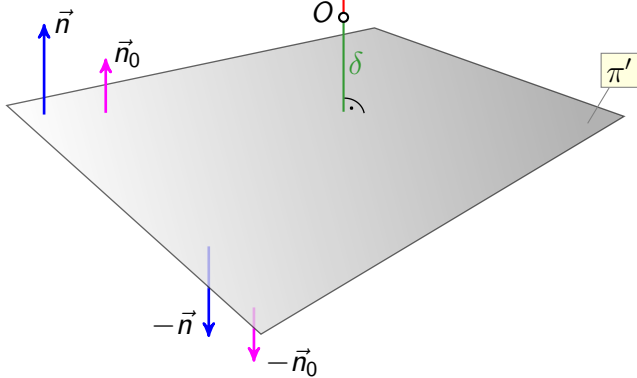


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normalni oblik

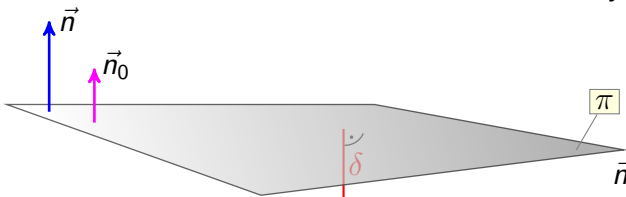


$$\vec{n}_0 = (\cos \alpha, \cos \beta, \cos \gamma)$$

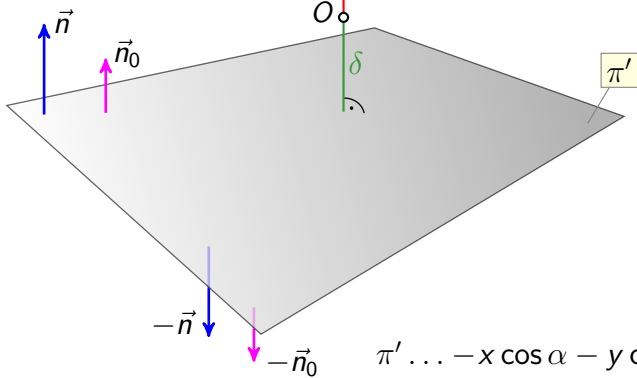


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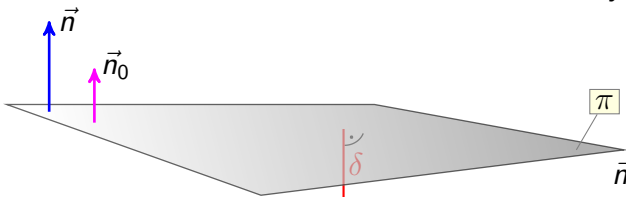
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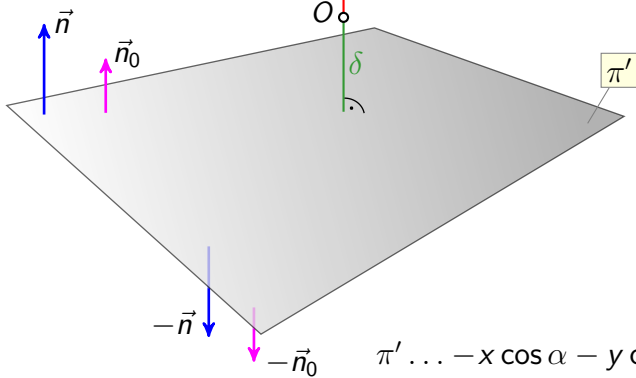
$$\pi' \dots -x \cos \alpha - y \cos \beta - z \cos \gamma - \delta = 0$$

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normalni oblik



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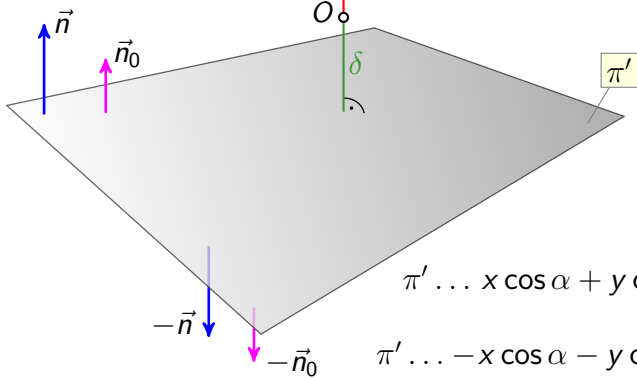
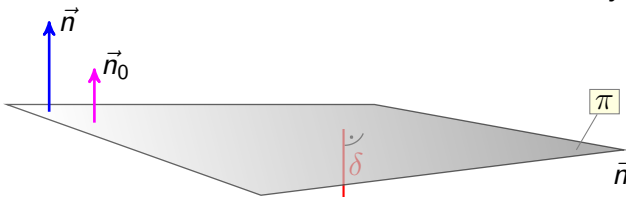
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normalni oblik

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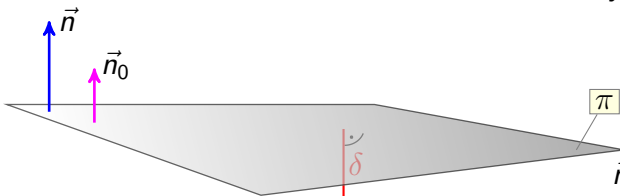
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normalni oblik



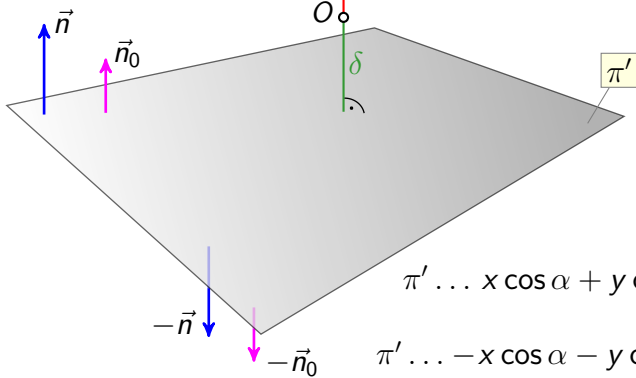
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normalni oblik



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nije normalni oblik



$$\pi' \dots x \cos \alpha + y \cos \beta + z \cos \gamma + \delta = 0$$

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normalni oblik

## 2. način

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$$1 = \frac{|8 \cdot 0 + 9 \cdot 0 + 1 \cdot 0 + D|}{\sqrt{8^2}}$$

2. način  $\vec{n} = (8, 9, 1)$ ,  $T_0(0, 0, 0)$ ,  $d(T_0, \pi) = 1$

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$$1 = \frac{|D|}{\sqrt{146}}$$

2. način  $\vec{n} = (8, 9, 1)$ ,  $T_0(0, 0, 0)$ ,  $d(T_0, \pi) = 1$

$$\pi \dots Ax + By + Cz + D = 0$$

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negativni predznak  
poštuje orijentaciju  
normale  $\vec{n}$

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negativni predznak  
poštuje orijentaciju  
normale  $\vec{n}$

pozitivni predznak ne  
poštuje orijentaciju  
normale  $\vec{n}$

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$$\pi \dots Ax + By + Cz + D = 0$$

$\pi \dots$

$$d(T_0, \pi) = \frac{|Ax_0 + By_0 + Cz_0 + D|}{\sqrt{A^2 + B^2 + C^2}}$$

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negativni predznak  
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2. način  $\vec{n} = (8, 9, 1)$ ,  $T_0(0, 0, 0)$ ,  $d(T_0, \pi) = 1$

$$\pi \dots Ax + By + Cz + D = 0$$

$$\pi \dots 8x + 9y + z - \sqrt{146} = 0$$

$$d(T_0, \pi) = \frac{|Ax_0 + By_0 + Cz_0 + D|}{\sqrt{A^2 + B^2 + C^2}}$$

$$1 = \frac{|8 \cdot 0 + 9 \cdot 0 + 1 \cdot 0 + D|}{\sqrt{8^2 + 9^2 + 1^2}}$$

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negativni predznak  
poštuje orijentaciju  
normale  $\vec{n}$

pozitivni predznak ne  
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negativni predznak  
poštuje orijentaciju  
normale  $\vec{n}$

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$$1 = \frac{|D|}{\sqrt{146}} \rightsquigarrow |D| = \sqrt{146} \rightsquigarrow D = \pm\sqrt{146}$$

pozitivni predznak ne  
poštuje orijentaciju  
normale  $\vec{n}$

2. način  $\vec{n} = \overset{A}{8}, \overset{B}{9}, \overset{C}{1}, T_0(\overset{x_0}{0}, \overset{y_0}{0}, \overset{z_0}{0}), d(T_0, \pi) = 1$

$$\pi \dots Ax + By + Cz + D = 0$$

$$\pi \dots 8x + 9y + z - \sqrt{146} = 0$$

negativni predznak  
poštuje orijentaciju  
normale  $\vec{n}$

$$d(T_0, \pi) = \frac{|Ax_0 + By_0 + Cz_0 + D|}{\sqrt{A^2 + B^2 + C^2}}$$

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pozitivni predznak ne  
poštuje orijentaciju  
normale  $\vec{n}$

$$\pi' \dots 8x + 9y + z + \sqrt{146} = 0$$

## **treći zadatak**

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### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Zadatak 3

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### Rješenje

$A(1, 2, 3)$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 =$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2$$



### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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### Rješenje

$$A(1, 2, 3) \overset{x \ y \ z}{\rightsquigarrow} 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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### Rješenje

$$A(1, 2, 3) \overset{x \ y \ z}{\rightsquigarrow} 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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### Rješenje

$$A(1, 2, 3) \overset{x \ y \ z}{\rightsquigarrow} 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$A(1, 2, 3) \xrightarrow{x \ y \ z} 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$A(1, 2, 3) \xrightarrow{x \ y \ z} 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$B(4, 0, -5)$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 =$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

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### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 - 5$$



### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 + 5 \cdot (-5)$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 + 5 \cdot (-5) - 1$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 + 5 \cdot (-5) - 1 = -18$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 + 5 \cdot (-5) - 1 = -18 < 0$$

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 + 5 \cdot (-5) - 1 = -18 < 0$$

Točke  $A$  i  $B$  se nalaze s različitih strana ravnine  $\Sigma$ .

### Zadatak 3

Ispitajte jesu li točke  $A(1, 2, 3)$  i  $B(4, 0, -5)$  s iste strane ravnine

$$\Sigma \dots 2x - y + 5z - 1 = 0.$$

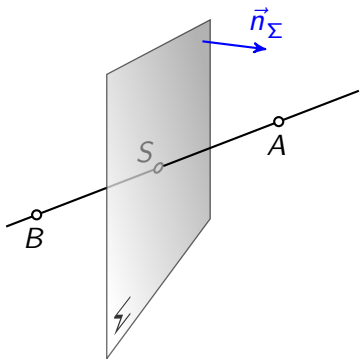
Odredite točku  $S$  u kojoj pravac  $AB$  siječe ravninu  $\Sigma$ . Pripada li točka  $S$  dužini  $\overline{AB}$ ? Obrazložite svoj odgovor.

### Rješenje

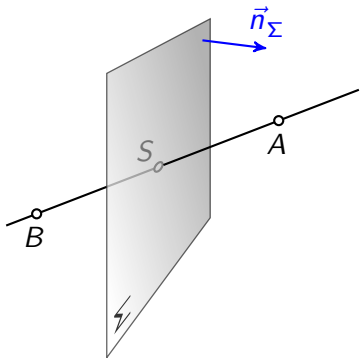
$$\begin{array}{c} x \quad y \quad z \\ A(1, 2, 3) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 1 - 2 + 5 \cdot 3 - 1 = 14 > 0$$

$$\begin{array}{c} x \quad y \quad z \\ B(4, 0, -5) \end{array} \rightsquigarrow 2x - y + 5z - 1 = 2 \cdot 4 - 0 + 5 \cdot (-5) - 1 = -18 < 0$$

Točke  $A$  i  $B$  se nalaze s različitih strana ravnine  $\Sigma$ . Točka  $A$  se nalazi na onoj strani na koju pokazuje normala  $\vec{n}_{\Sigma} = (2, -1, 5)$ .



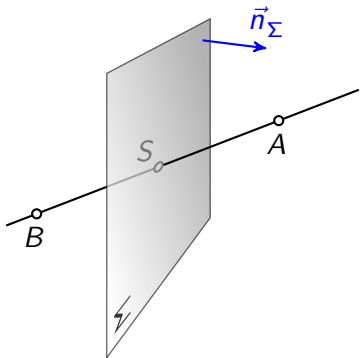
$A(1, 2, 3), B(4, 0, -5)$

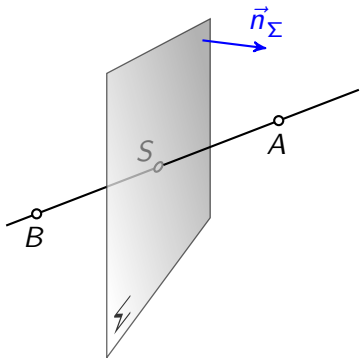




$A(1, 2, 3), B(4, 0, -5)$

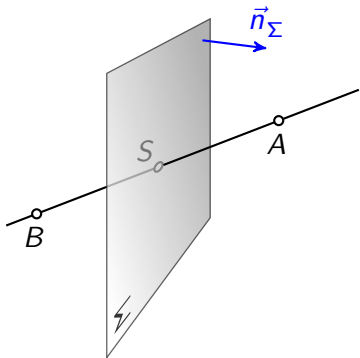
$AB \dots$





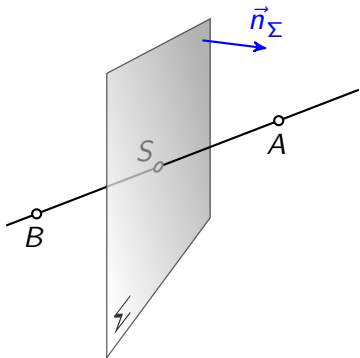
$$A(1, 2, 3), B(4, 0, -5)$$

$$AB \dots A, \vec{AB}$$



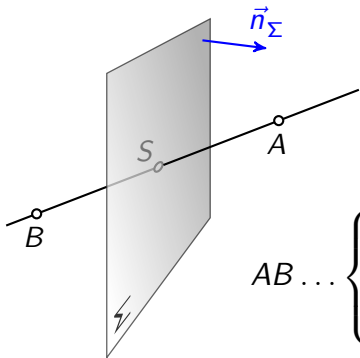
$$A(1, 2, 3), B(4, 0, -5)$$

$$AB \dots A, \vec{AB} \quad \vec{AB} =$$



$$A(1, 2, 3), B(4, 0, -5)$$

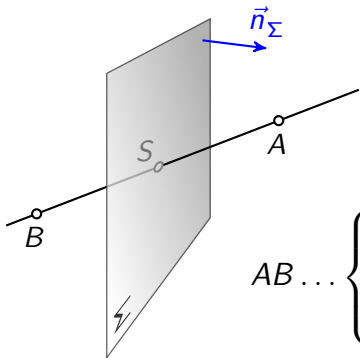
$$AB \dots A, \vec{AB} \quad \vec{AB} = (3, -2, -8)$$



$$A(1, 2, 3), B(4, 0, -5)$$

$$AB \dots A, \vec{AB} \quad \vec{AB} = (3, -2, -8)$$

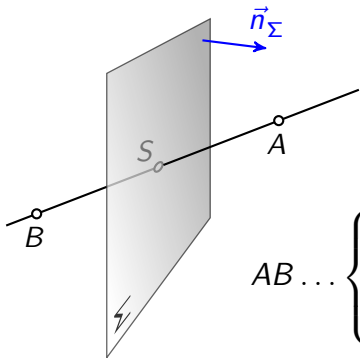
$AB \dots$  {



$$A(1, 2, 3), B(4, 0, -5)$$

$$AB \dots A, \vec{AB} \quad \vec{AB} = (3, -2, -8)$$

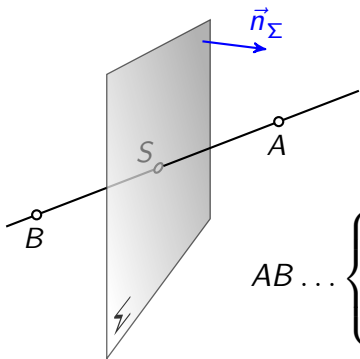
$$AB \dots \begin{cases} x = \\ y = \\ z = \end{cases}$$



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$$AB \dots \begin{cases} x = 1 \\ y = 2 \\ z = 3 \end{cases}$$

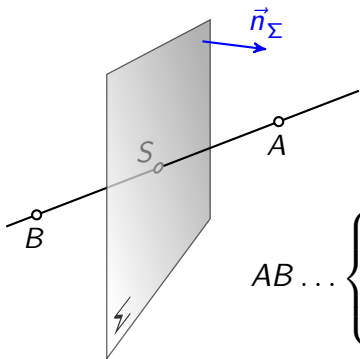


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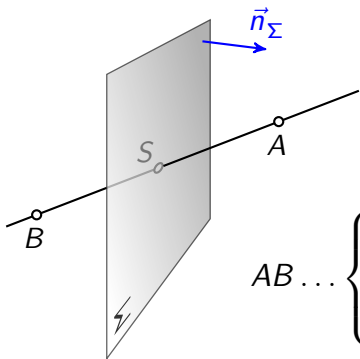




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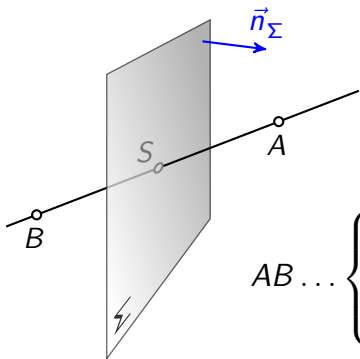
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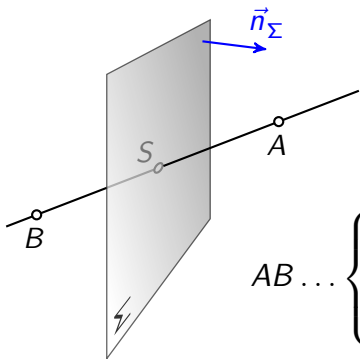
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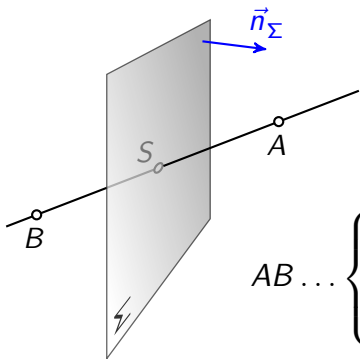
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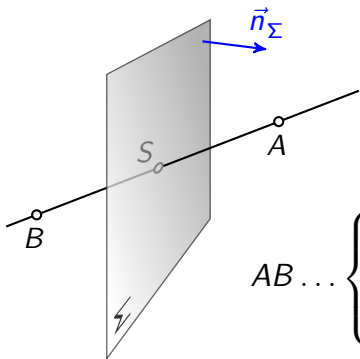
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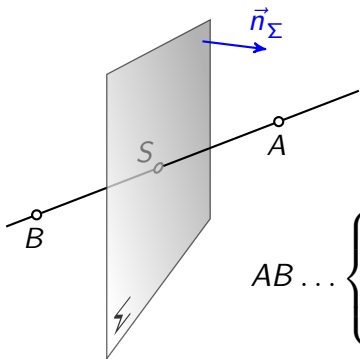
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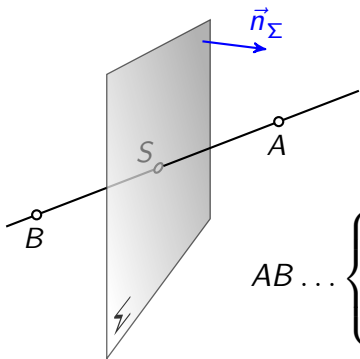


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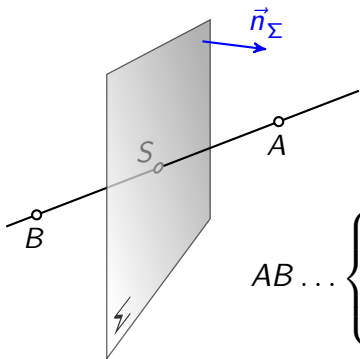
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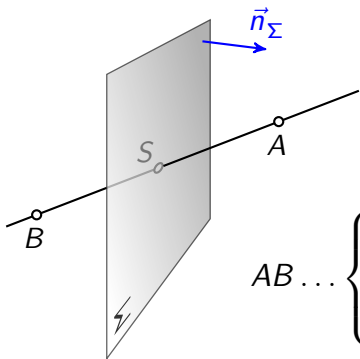
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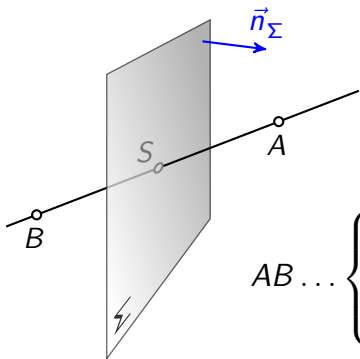
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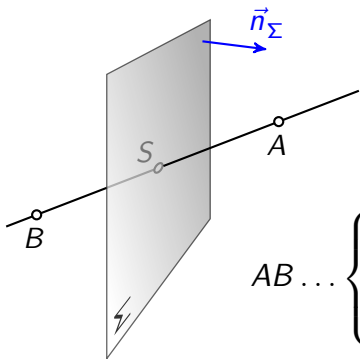
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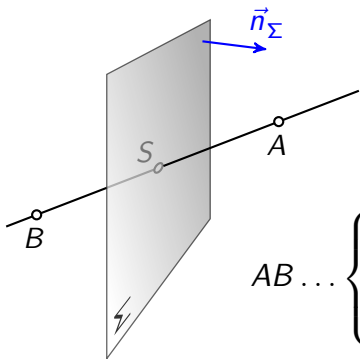
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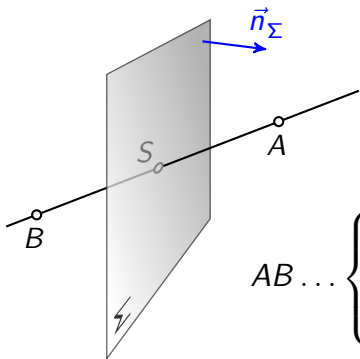
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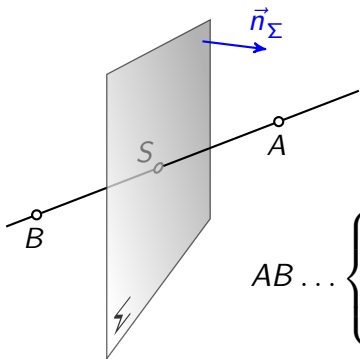
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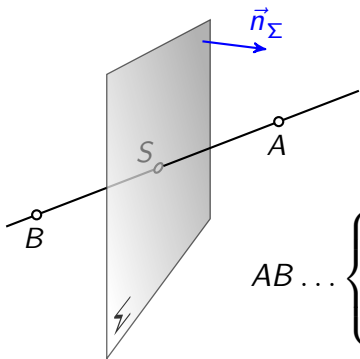
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$$2 + 6t$$



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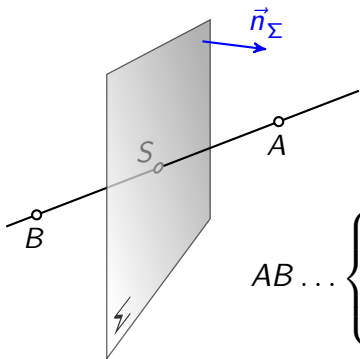
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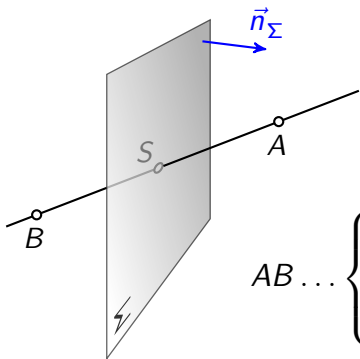
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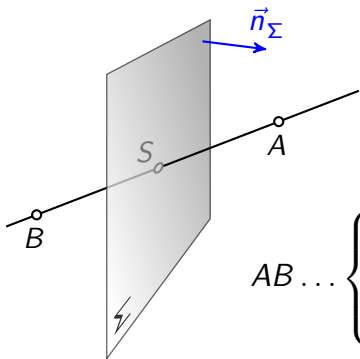
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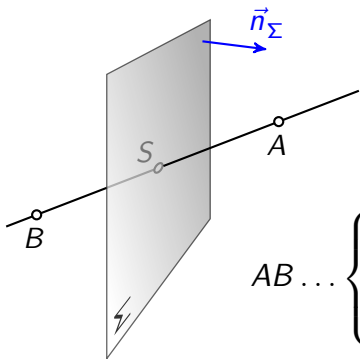
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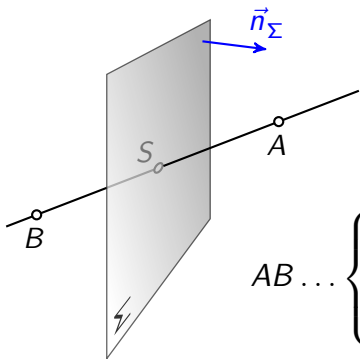
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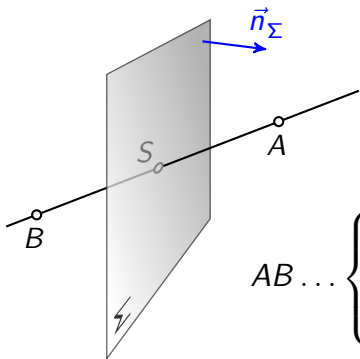
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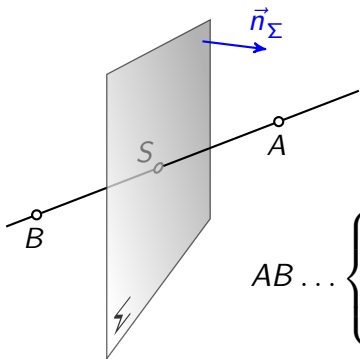
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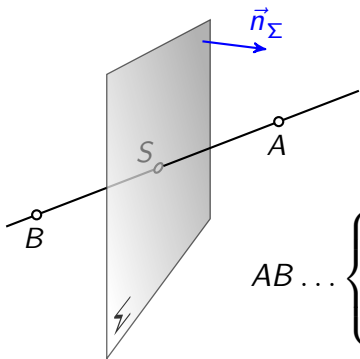
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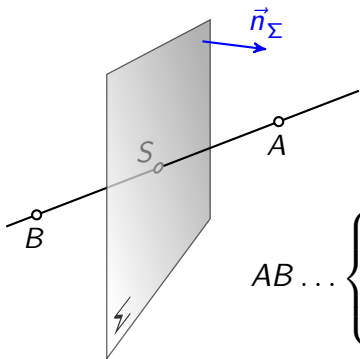
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$s($





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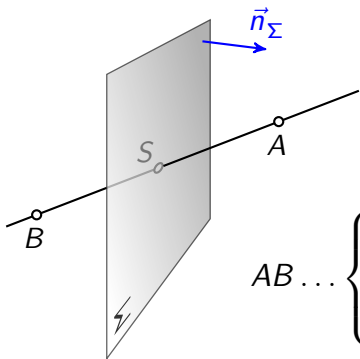
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$$S\left(\frac{37}{16}, \dots\right)$$



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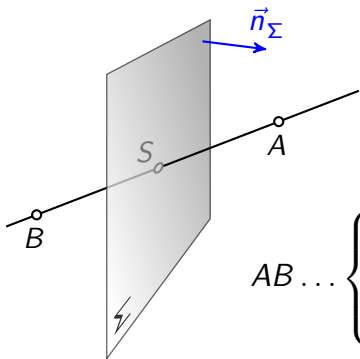
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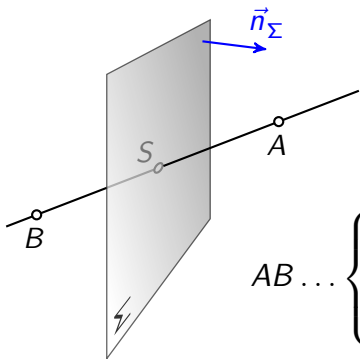
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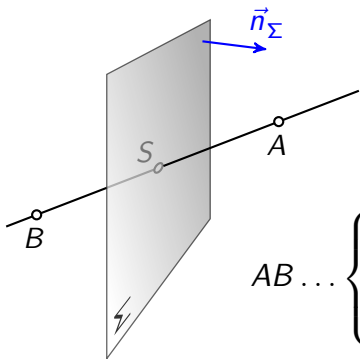
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$$t = \frac{7}{16}$$

$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$



$$A(1, 2, 3), B(4, 0, -5)$$

$$AB \dots A, \vec{AB} \quad \vec{AB} = (3, -2, -8)$$

$$\Sigma \dots 2x - y + 5z - 1 = 0$$

$$AB \dots \begin{cases} x = 1 + 3 \cdot t \\ y = 2 + (-2) \cdot t \\ z = 3 + (-8) \cdot t \end{cases}$$

$$AB \dots \begin{cases} x = 1 + 3t \\ y = 2 - 2t \\ z = 3 - 8t \end{cases}$$

$$2x - y + 5z - 1 = 0$$

$$2 \cdot (1 + 3t) - (2 - 2t) + 5 \cdot (3 - 8t) - 1 = 0$$

$$2 + 6t - 2 + 2t + 15 - 40t - 1 = 0$$

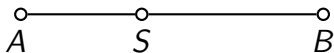
$$-32t + 14 = 0$$

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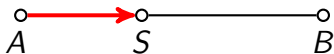
$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

Točka  $S$  pripada dužini  $\overline{AB}$  jer se  
točke  $A$  i  $B$  nalaze s različitih  
strana ravnine  $\Sigma$ .

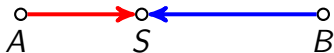
2. način pomoću djelišnog omjera



2. način pomoću djelišnog omjera



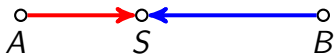
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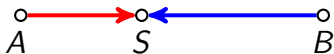


2. način pomoću djelišnog omjera

$A(1, 2, 3)$ ,  $B(4, 0, -5)$



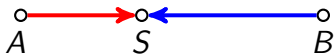
2. način pomoću djelišnog omjera



$$A(1, 2, 3), B(4, 0, -5)$$

$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

2. način pomoću djelišnog omjera

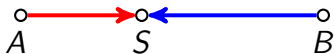


$$A(1, 2, 3), B(4, 0, -5)$$

$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

$$\vec{AS} = \lambda \vec{BS}$$

2. način pomoću djelišnog omjera



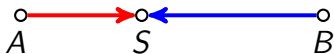
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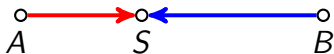
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2. način pomoću djelišnog omjera



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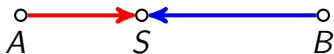
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2. način pomoću djelišnog omjera

$$A(1, 2, 3), B(4, 0, -5)$$



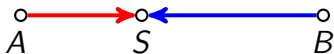
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2. način pomoću djelišnog omjera

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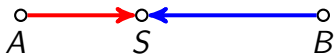
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2. način pomoću djelišnog omjera

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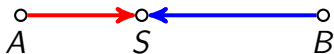
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$$\frac{21}{16}$$

2. način pomoću djelišnog omjera

$$A(1, 2, 3), B(4, 0, -5)$$



$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

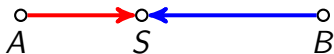
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$$\frac{\frac{21}{16}}{-\frac{27}{16}}$$

2. način pomoću djelišnog omjera

$$A(1, 2, 3), B(4, 0, -5)$$



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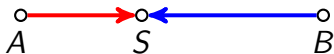
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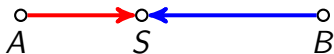
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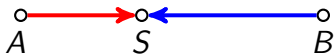
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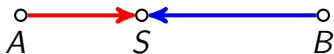
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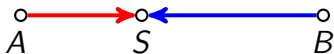
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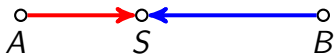
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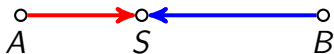
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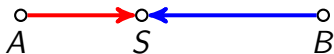
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2. način pomoću djelišnog omjera

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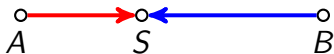
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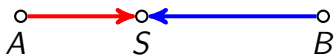
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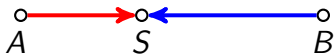
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2. način pomoću djelišnog omjera

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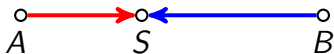
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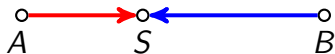
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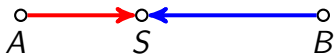
Kako je  $\lambda < 0$ , točka  $S$  pripada dužini  $\overline{AB}$ .

$$\lambda = -\frac{7}{9}$$



2. način pomoću djelišnog omjera

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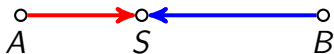
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3. način još jedna ideja

2. način pomoću djelišnog omjera

$$A(1, 2, 3), B(4, 0, -5)$$



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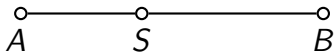
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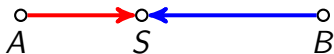
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3. način još jedna ideja



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$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

$$\vec{AS} = \left(\frac{21}{16}, -\frac{7}{8}, -\frac{7}{2}\right) \quad \vec{BS} = \left(-\frac{27}{16}, \frac{9}{8}, \frac{9}{2}\right)$$

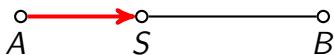
$$\vec{AS} = \lambda \vec{BS}$$

$$\frac{\frac{21}{16}}{-\frac{27}{16}} = \frac{-\frac{7}{8}}{\frac{9}{8}} = \frac{-\frac{7}{2}}{\frac{9}{2}} \rightsquigarrow -\frac{7}{9} = -\frac{7}{9} = -\frac{7}{9} \rightsquigarrow \text{točke } A, B \text{ i } S \text{ su kolinearne}$$

Kako je  $\lambda < 0$ , točka  $S$  pripada dužini  $\overline{AB}$ .

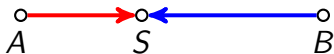
$$\lambda = -\frac{7}{9}$$

3. način još jedna ideja



2. način pomoću djelišnog omjera

$$A(1, 2, 3), B(4, 0, -5)$$



$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

$$\vec{AS} = \left(\frac{21}{16}, -\frac{7}{8}, -\frac{7}{2}\right) \quad \vec{BS} = \left(-\frac{27}{16}, \frac{9}{8}, \frac{9}{2}\right)$$

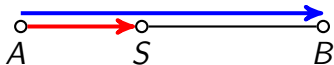
$$\vec{AS} = \lambda \vec{BS}$$

$$\frac{\frac{21}{16}}{-\frac{27}{16}} = \frac{-\frac{7}{8}}{\frac{9}{8}} = \frac{-\frac{7}{2}}{\frac{9}{2}} \rightsquigarrow -\frac{7}{9} = -\frac{7}{9} = -\frac{7}{9} \rightsquigarrow \text{točke } A, B \text{ i } S \text{ su kolinearne}$$

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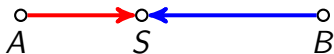
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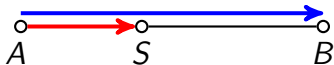
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Kako je  $\lambda < 0$ , točka  $S$  pripada dužini  $\overline{AB}$ .

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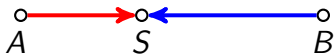
3. način još jedna ideja

$$\vec{AS} = \mu \vec{AB}$$



2. način pomoću djelišnog omjera

$$A(1, 2, 3), B(4, 0, -5)$$



$$S\left(\frac{37}{16}, \frac{9}{8}, -\frac{1}{2}\right)$$

$$\vec{AS} = \left(\frac{21}{16}, -\frac{7}{8}, -\frac{7}{2}\right) \quad \vec{BS} = \left(-\frac{27}{16}, \frac{9}{8}, \frac{9}{2}\right)$$

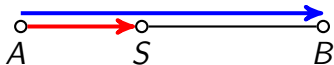
$$\vec{AS} = \lambda \vec{BS}$$

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Kako je  $\lambda < 0$ , točka  $S$  pripada dužini  $\overline{AB}$ .

$$\lambda = -\frac{7}{9}$$

3. način još jedna ideja



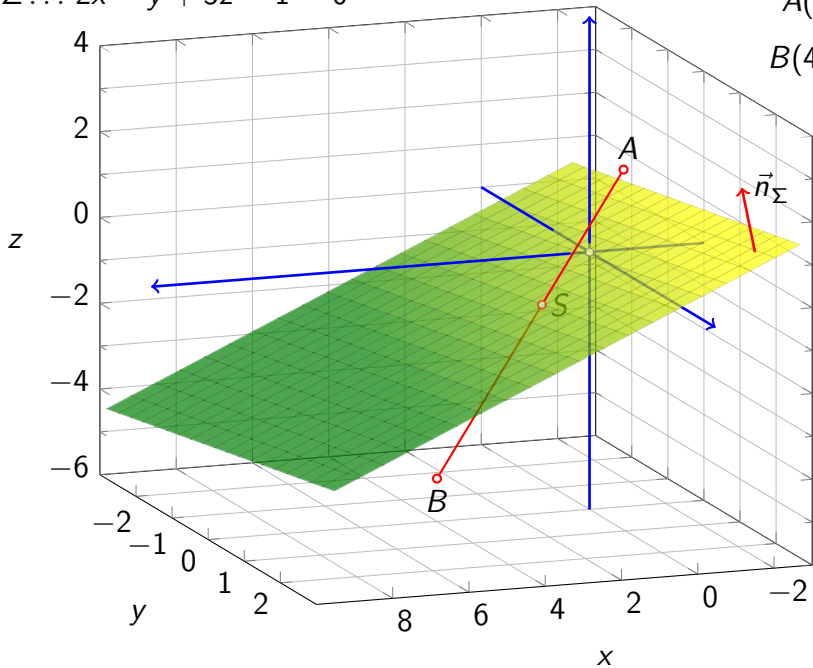
$$\vec{AS} = \mu \vec{AB}$$

$$S \in \overline{AB} \Leftrightarrow \mu \in [0, 1]$$

$$\Sigma \dots 2x - y + 5z - 1 = 0$$

$A(1, 2, 3)$

$B(4, 0, -5)$



## čtvrti zadatak

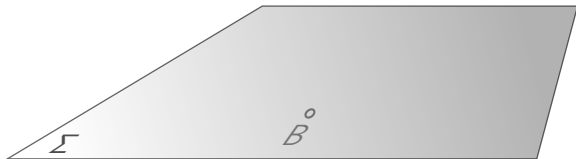
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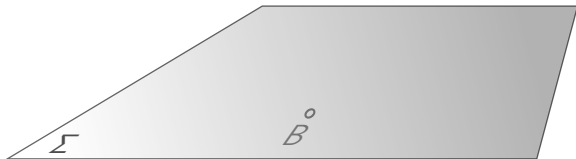
#### Zadatak 4

Napišite jednadžbu ravnine koja prolazi točkom  $B(-1, 2, -4)$ , a okomita je na ravnine  $x + 3y - 2z + 5 = 0$  i  $-4x + 5y - z + 3 = 0$ .

## Rješenje



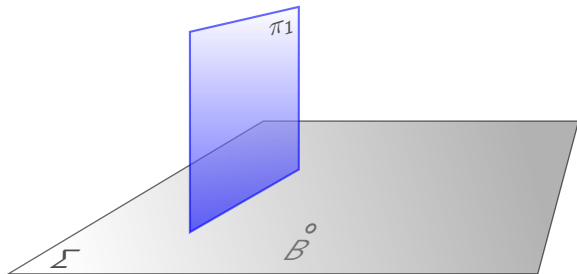
## Rješenje



$$B(-1, 2, -4)$$

## Rješenje

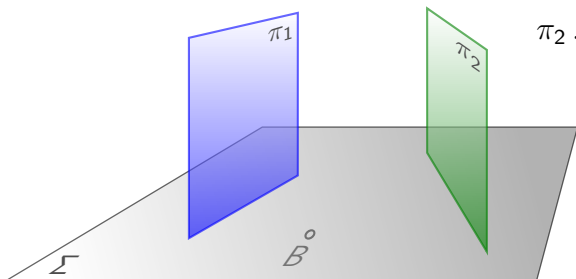
$$\pi_1 \dots x + 3y - 2z + 5 = 0$$



$$B(-1, 2, -4)$$

$$\Sigma \perp \pi_1$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

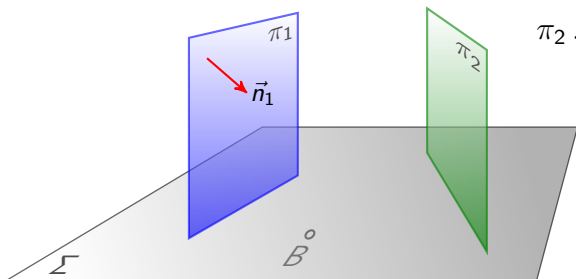
$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(-1, 2, -4)$$

$$\Sigma \perp \pi_1$$

$$\Sigma \perp \pi_2$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

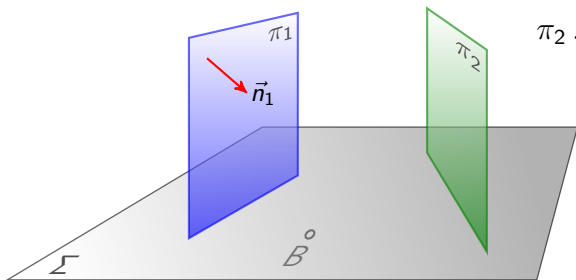
$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(-1, 2, -4)$$

$$\Sigma \perp \pi_1$$

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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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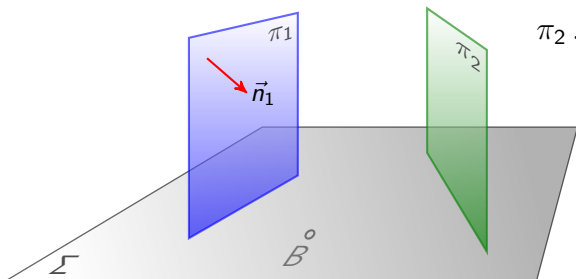
$$B(-1, 2, -4)$$

$$\vec{n}_1 =$$

$$\Sigma \perp \pi_1$$

$$\Sigma \perp \pi_2$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(-1, 2, -4)$$

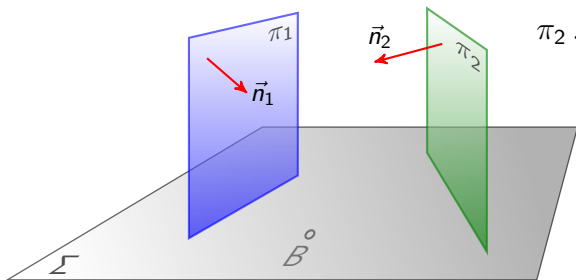
$$\vec{n}_1 = (1, 3, -2)$$

$$\Sigma \perp \pi_1$$

$$\Sigma \perp \pi_2$$



## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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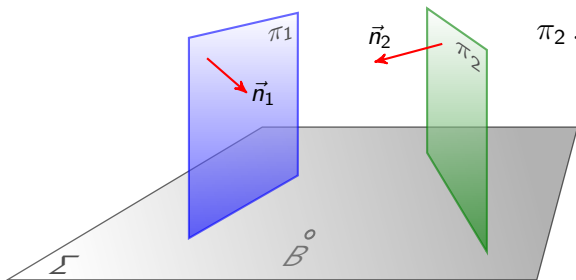
$$B(-1, 2, -4)$$

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$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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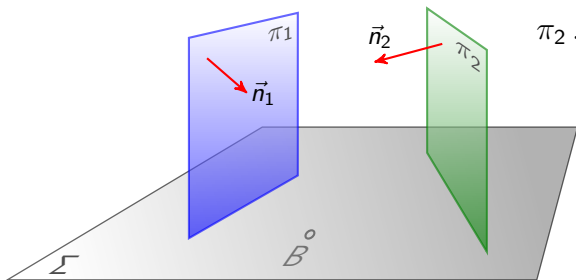
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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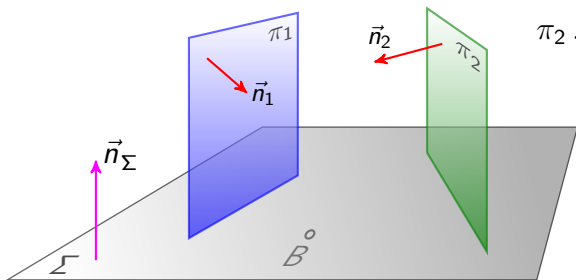
$$\vec{n}_1 = (1, 3, -2)$$

$$\vec{n}_2 = (-4, 5, -1)$$

$$\Sigma \perp \pi_1$$

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## Rješenje



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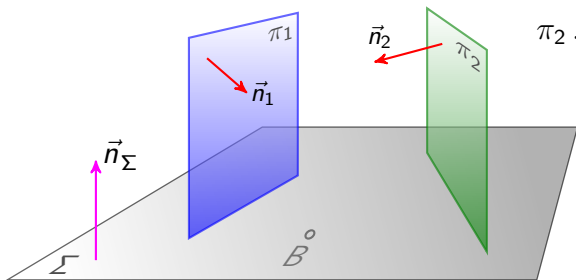
$$\vec{n}_1 = (1, 3, -2)$$

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## Rješenje



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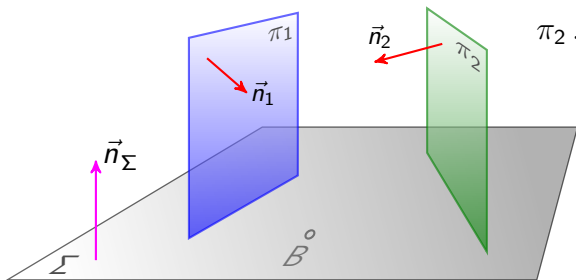
$$\vec{n}_1 = (1, 3, -2)$$

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$$\Sigma \perp \pi_1 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_1$$

$$\Sigma \perp \pi_2$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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$$B(-1, 2, -4)$$

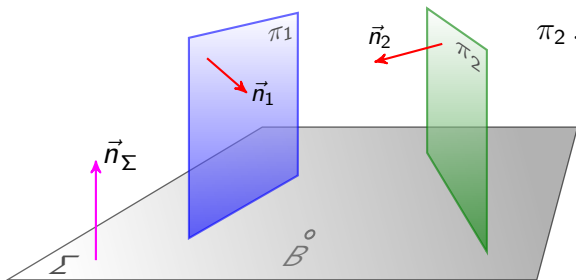
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

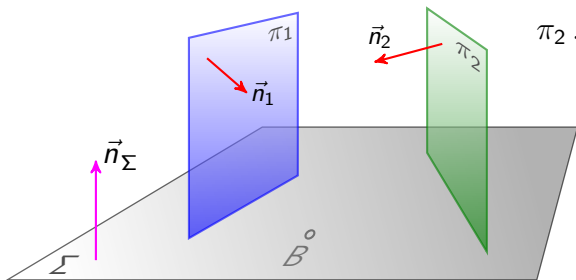
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(-1, 2, -4)$$

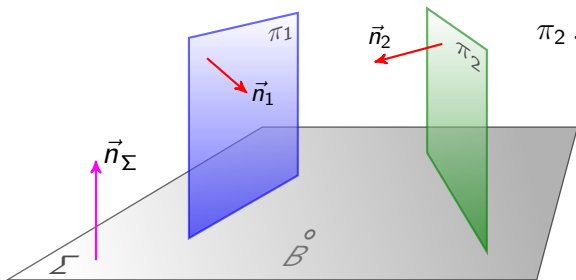
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

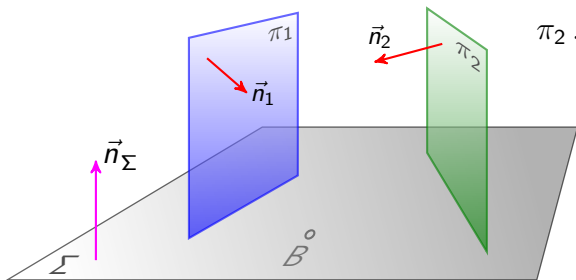
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$$\vec{n}_1 = (1, 3, -2)$$

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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

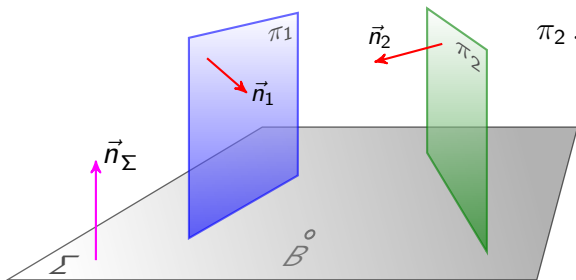
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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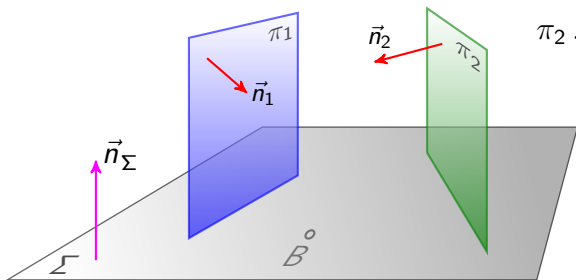
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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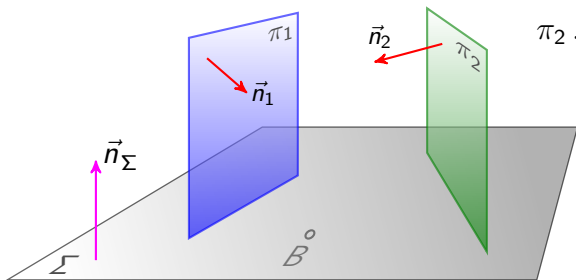
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

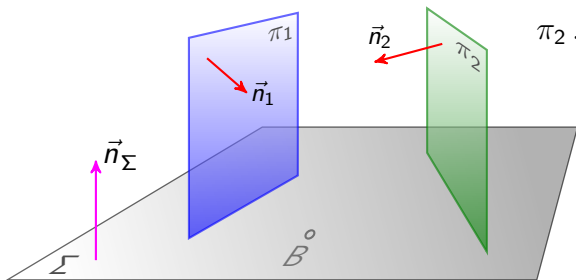
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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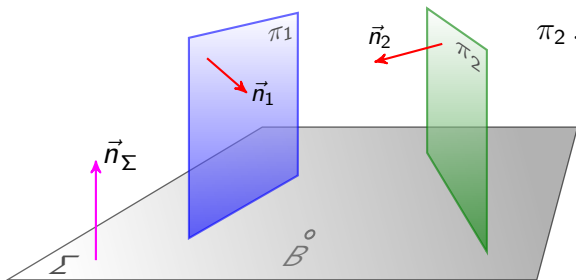
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$$\vec{n}_1 = (1, 3, -2)$$

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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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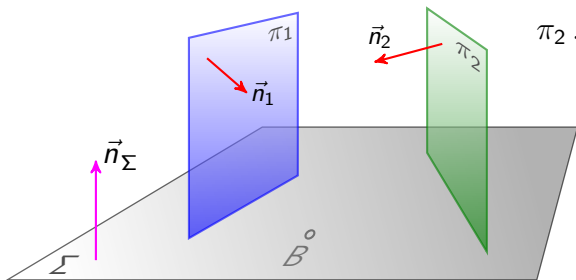
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## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

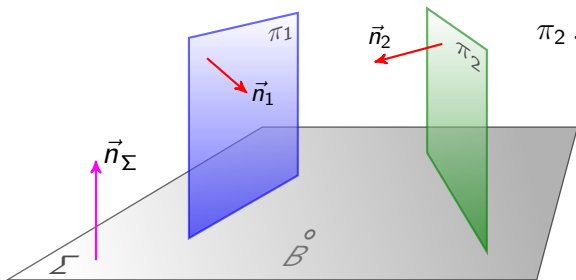
$$\vec{n}_2 = (-4, 5, -1)$$

$$\left. \begin{array}{l} \Sigma \perp \pi_1 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_1 \\ \Sigma \perp \pi_2 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_2 \end{array} \right\} \Rightarrow \vec{n}_\Sigma = \vec{n}_1 \times \vec{n}_2 = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 3 & -2 \\ -4 & 5 & -1 \end{vmatrix} = (7, 9, 17)$$

$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$



## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(-1, 2, -4)$$

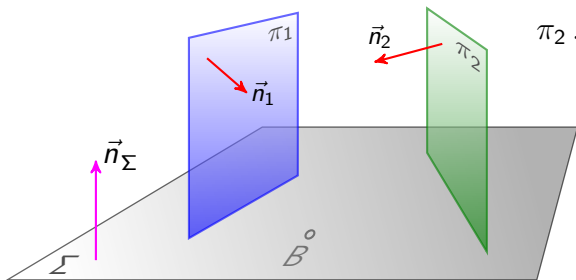
$$\vec{n}_1 = (1, 3, -2)$$

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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

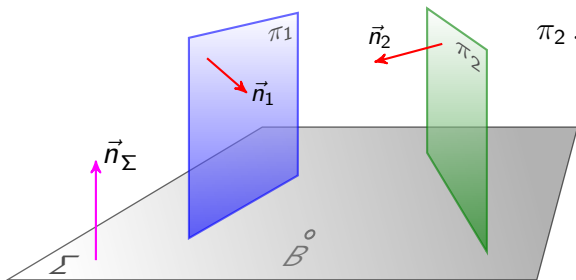
$$\vec{n}_1 = (1, 3, -2)$$

$$\vec{n}_2 = (-4, 5, -1)$$

$$\left. \begin{array}{l} \Sigma \perp \pi_1 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_1 \\ \Sigma \perp \pi_2 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_2 \end{array} \right\} \Rightarrow \vec{n}_\Sigma = \vec{n}_1 \times \vec{n}_2 = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 3 & -2 \\ -4 & 5 & -1 \end{vmatrix} = (7, 9, 17)$$

$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

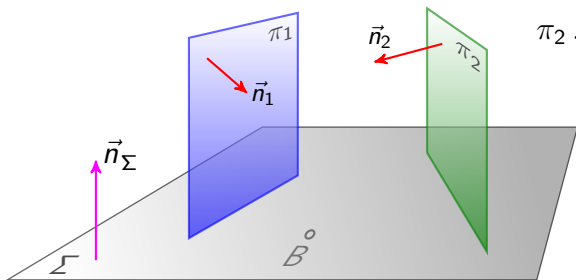
$$\vec{n}_2 = (-4, 5, -1)$$

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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

7.

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

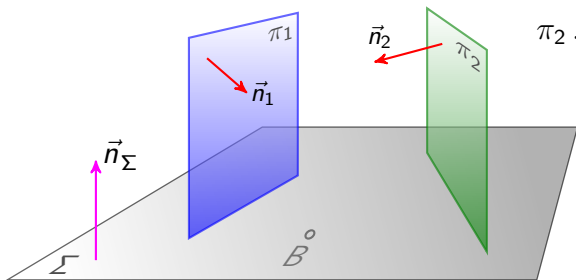
$$\vec{n}_2 = (-4, 5, -1)$$

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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1))$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

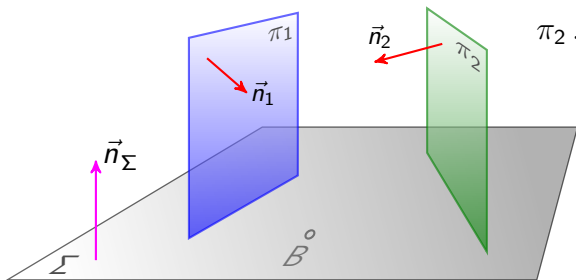
$$\vec{n}_2 = (-4, 5, -1)$$

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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

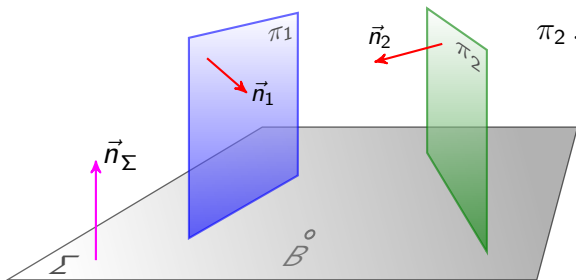
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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2)$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

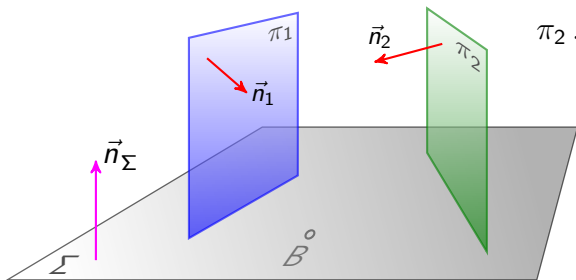
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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2) + 17 \cdot$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

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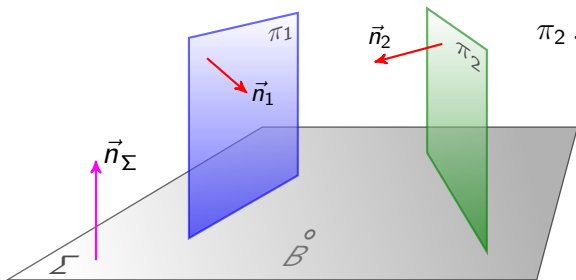
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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2) + 17 \cdot (z - (-4))$$



## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

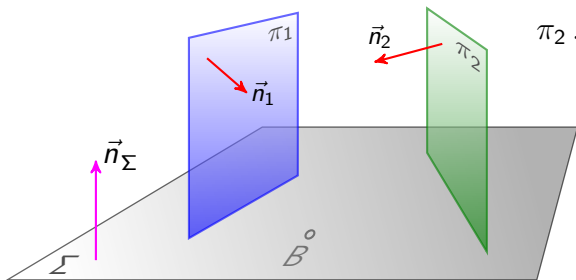
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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2) + 17 \cdot (z - (-4)) = 0$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

$$\vec{n}_2 = (-4, 5, -1)$$

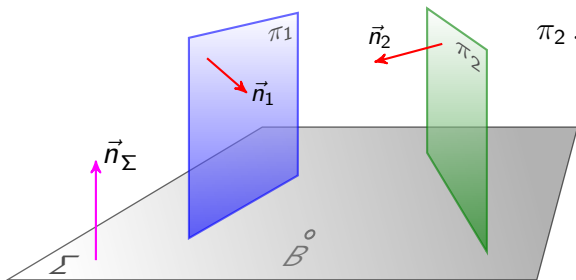
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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2) + 17 \cdot (z - (-4)) = 0$$

$$\Sigma \dots$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

$$\vec{n}_2 = (-4, 5, -1)$$

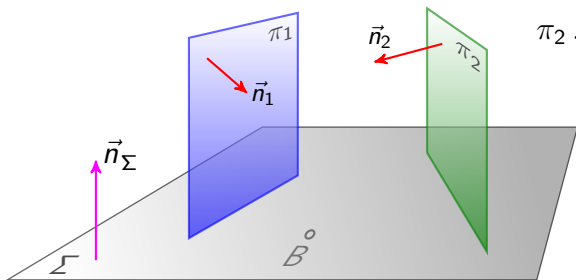
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$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2) + 17 \cdot (z - (-4)) = 0$$

$$\Sigma \dots 7x + 9y + 17z + 57 = 0$$

## Rješenje



$$\pi_1 \dots x + 3y - 2z + 5 = 0$$

$$\pi_2 \dots -4x + 5y - z + 3 = 0$$

$$B(x_0, y_0, z_0) \\ B(-1, 2, -4)$$

$$\vec{n}_1 = (1, 3, -2)$$

$$\vec{n}_2 = (-4, 5, -1)$$

$$\left. \begin{array}{l} \Sigma \perp \pi_1 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_1 \\ \Sigma \perp \pi_2 \Rightarrow \vec{n}_\Sigma \perp \vec{n}_2 \end{array} \right\} \Rightarrow \vec{n}_\Sigma = \vec{n}_1 \times \vec{n}_2 = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 3 & -2 \\ -4 & 5 & -1 \end{vmatrix} = (7, 9, 17)$$

$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

$$7 \cdot (x - (-1)) + 9 \cdot (y - 2) + 17 \cdot (z - (-4)) = 0$$

$$\Sigma \dots 7x + 9y + 17z + 57 = 0$$

**peti zadatak**

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## Zadatak 5

Zadani su pravac  $p$  i ravnina  $\Sigma$  svojim vektorskim jednadžbama

$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0),$$

$$\Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2).$$


- Napišite parametarske jednadžbe i opći oblik jednadžbe ravnine  $\Sigma$ .
- Odredite pravac  $q$  koji prolazi točkom  $T(1, 0, 4)$  i siječe zadani pravac  $p$  te je paralelan s ravninom  $\Sigma$ .

## Rješenje

a)  $\Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$

## Rješenje

$$\text{a) } \quad \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$




## Rješenje

$$\text{a) } \quad \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$

$$\vec{a} = (1, 0, 0)$$

## Rješenje

$$\text{a) } \quad \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$

$$\vec{a} = (1, 0, 0)$$

$$\vec{b} = (-1, 1, 2)$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$

$$\vec{a} = (1, 0, 0)$$

$$\vec{b} = (-1, 1, 2)$$

Parametarske jednačbe

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$

$$\vec{a} = (1, 0, 0)$$

$$\vec{b} = (-1, 1, 2)$$

Parametarske jednačbe

$$\Sigma \dots \left\{ \right.$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$

$$\vec{a} = (1, 0, 0)$$

$$\vec{b} = (-1, 1, 2)$$

Parametarske jednačbe

$$\Sigma \dots \left\{ \right.$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

*(Note: Red arrows in the original image point from the vector components in the equation to their respective labels below.)*

Parametarske jednačbe

$$\Sigma \dots \left\{ \begin{array}{l} x = 2 + u - v \\ \dots \end{array} \right.$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

*(Note: Red arrows in the original image point from the coordinates in the vector equation to the labels below: from (2,1,3) to T0, from (1,0,0) to a, and from (-1,1,2) to b. A red arrow also points from the label (x,y,z) to the vector r.)*

Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$



## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

$$\vec{n}_\Sigma = \vec{a} \times \vec{b}$$

Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$$T_0(2, 1, 3)$$

$$\vec{a} = (1, 0, 0)$$

$$\vec{b} = (-1, 1, 2)$$

$$\vec{n}_\Sigma = \vec{a} \times \vec{b} = \left| \begin{array}{c} \phantom{\vec{a}} \\ \phantom{\vec{b}} \end{array} \right|$$

Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

$$\vec{n}_\Sigma = \vec{a} \times \vec{b} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 0 & 0 \\ -1 & 1 & 2 \end{vmatrix}$$

Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$



## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3) \quad \vec{a} = (1, 0, 0) \quad \vec{b} = (-1, 1, 2)$

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$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

## Rješenje

$$\text{a) } \Sigma \dots \vec{r} = (2, 1, 3) + u \cdot (1, 0, 0) + v \cdot (-1, 1, 2)$$

$T_0(2, 1, 3)$        $\vec{a} = (1, 0, 0)$        $\vec{b} = (-1, 1, 2)$

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Parametarske jednačbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

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$$0 \cdot (x - 2)$$

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$$\Sigma \dots$$

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Parametarske jednadžbe

$$\Sigma \dots \begin{cases} x = 2 + u - v \\ y = 1 + v \\ z = 3 + 2v \end{cases}$$

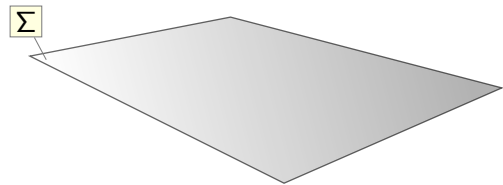
$$\Sigma \dots A(x - x_0) + B(y - y_0) + C(z - z_0) = 0$$

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$$\Sigma \dots -2y + z - 1 = 0$$

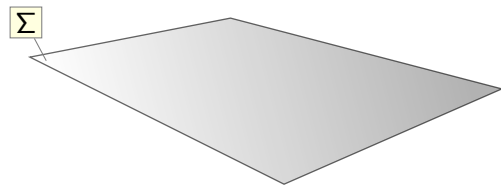
opći oblik

b)



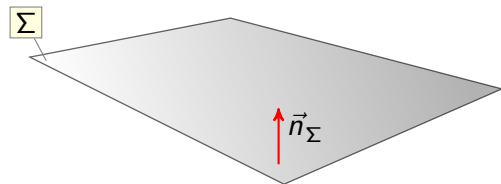


b)



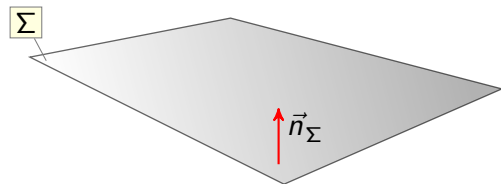
$$\Sigma \dots -2y + z - 1 = 0$$

b)



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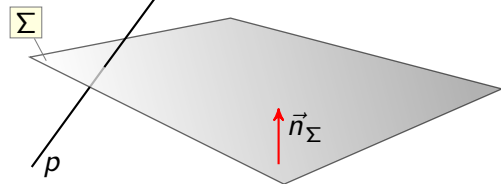
b)



$$\vec{n}_\Sigma = (0, -2, 1)$$

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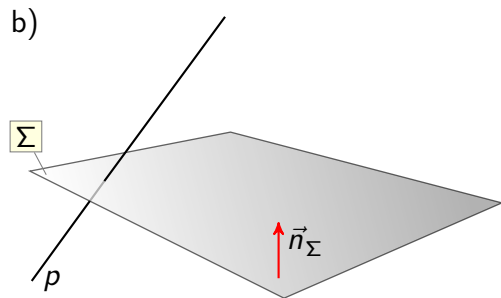
b)



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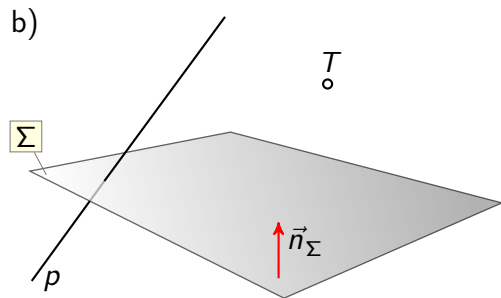
$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$



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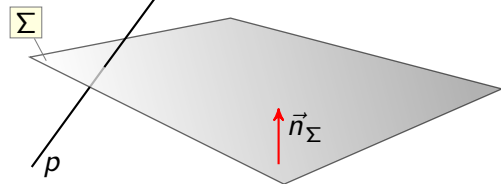
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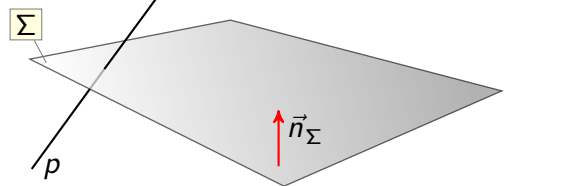
$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4)$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

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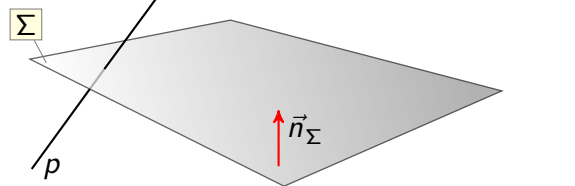


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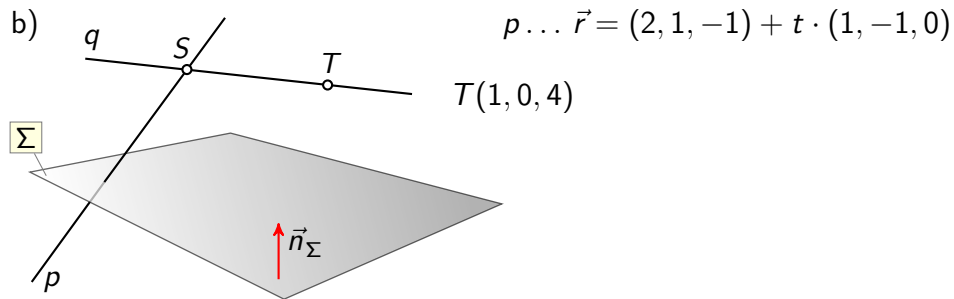


b)  $p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$



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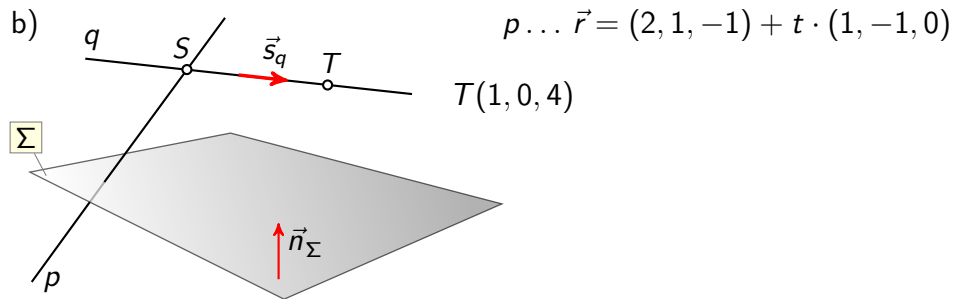
$$\Sigma \dots -2y + z - 1 = 0$$



$$\vec{n}_\Sigma = (0, -2, 1)$$

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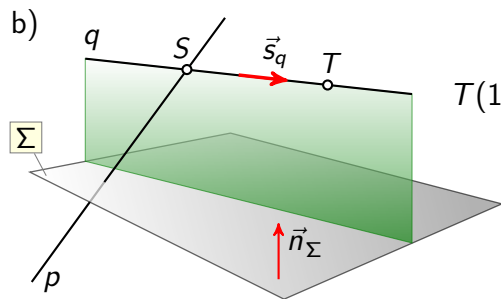
$$q \parallel \Sigma$$



$$\vec{n}_\Sigma = (0, -2, 1)$$

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$$q \parallel \Sigma$$



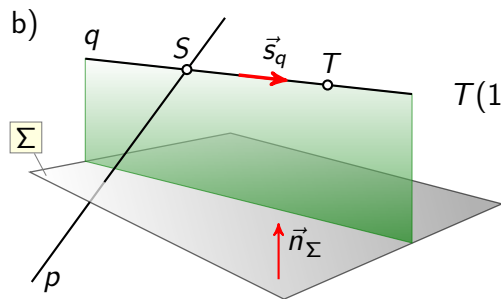
$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4)$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

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$$q \parallel \Sigma$$



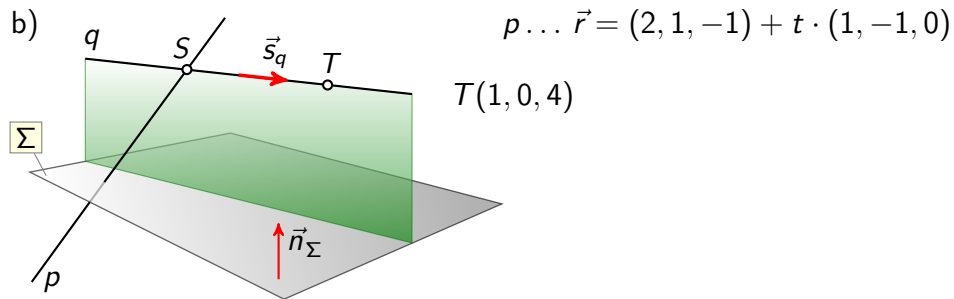
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$$q \parallel \Sigma \Rightarrow \overrightarrow{ST} \perp \vec{n}_\Sigma$$



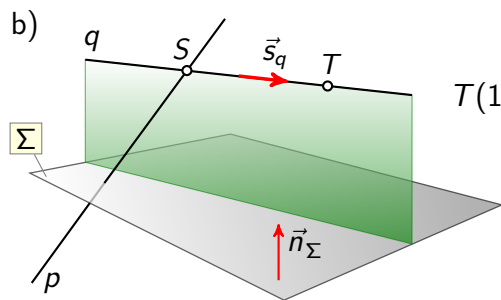
$$\vec{n}_\Sigma = (0, -2, 1)$$

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$$q \parallel \Sigma \Rightarrow \overrightarrow{ST} \perp \vec{n}_\Sigma \Rightarrow \overrightarrow{ST} \cdot \vec{n}_\Sigma = 0$$

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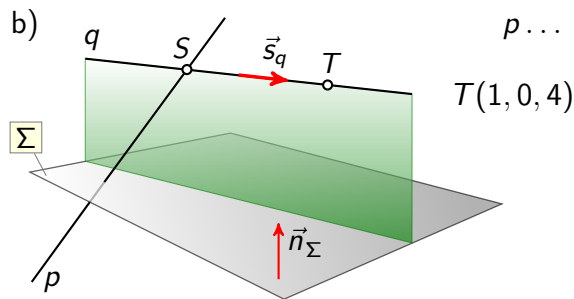
$$T(1, 0, 4)$$



$$\vec{n}_\Sigma = (0, -2, 1)$$

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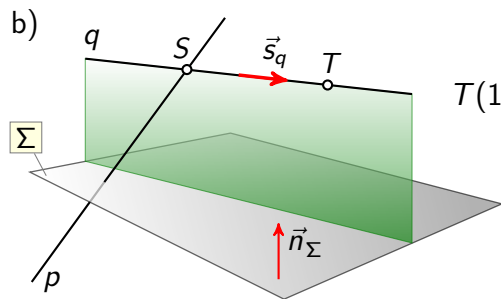
$$p \dots \left\{ \right.$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

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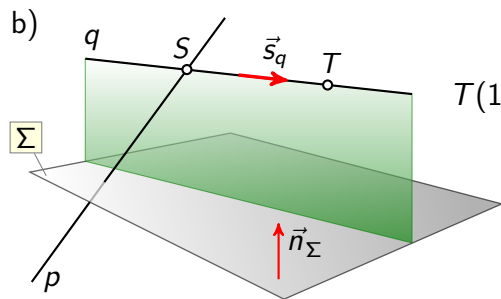
$(x, y, z)$

$p \dots \left\{ \right.$

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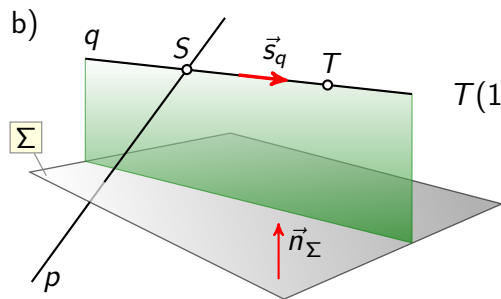
$$T(1, 0, 4) \quad (x, y, z)$$

$$p \dots \left\{ \begin{array}{l} x = 2 + t \end{array} \right.$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

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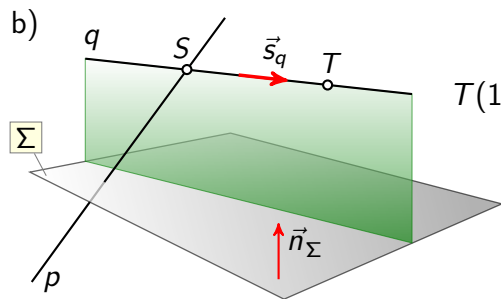
$$T(1, 0, 4) \quad (x, y, z)$$

$$p \dots \begin{cases} x = 2 + t \\ y = 1 - t \end{cases}$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

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$(x, y, z)$

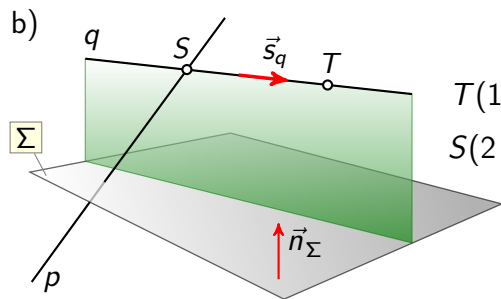
$$T(1, 0, 4)$$

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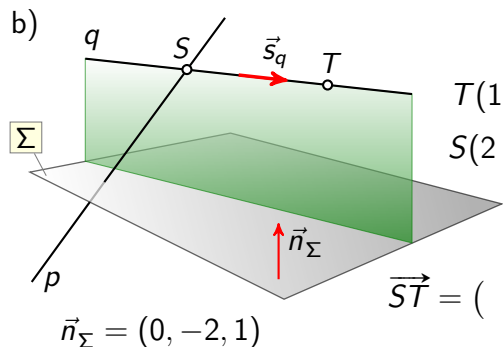
$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

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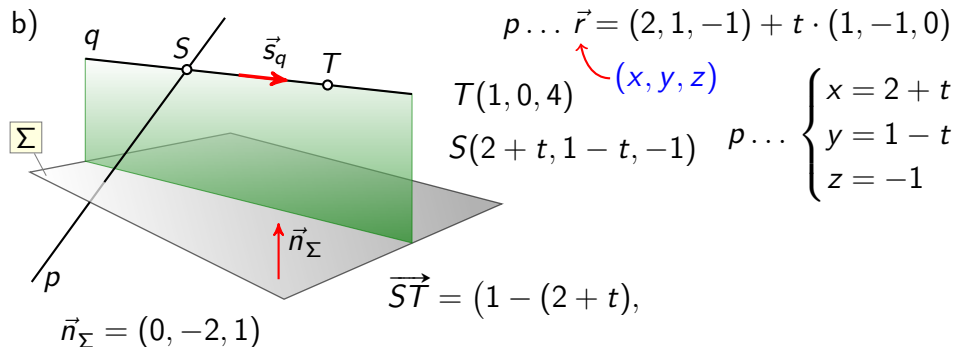
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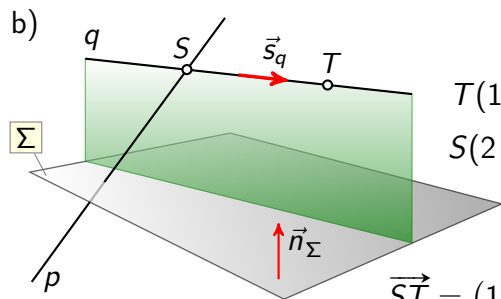
$$\Sigma \dots -2y + z - 1 = 0$$

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$$\Sigma \dots -2y + z - 1 = 0$$

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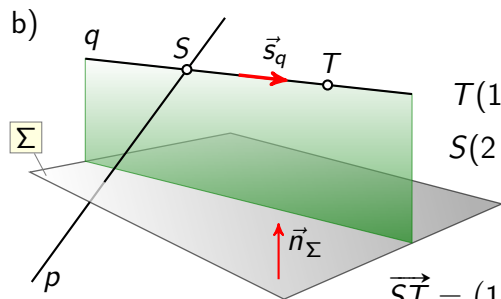
$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), -1 - (-1)) = (-1 - t, -1 + t, 0)$$

$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$





$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

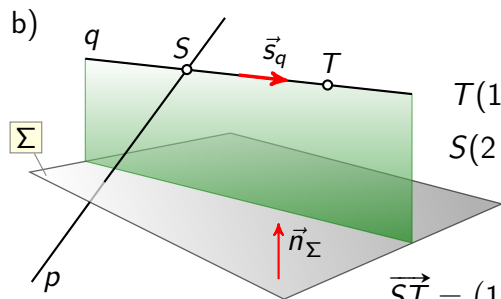
$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

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$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

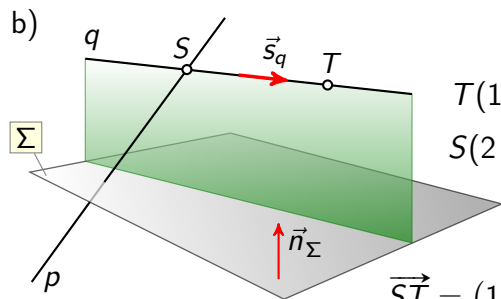
$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} =$$

$$\Sigma \dots -2y + z - 1 = 0$$

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$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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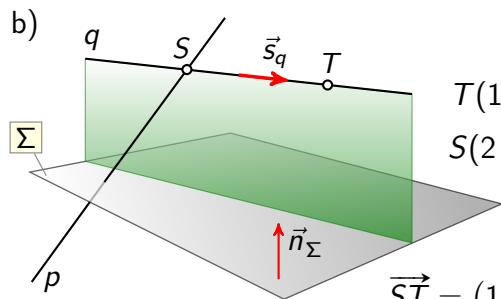
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$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t,$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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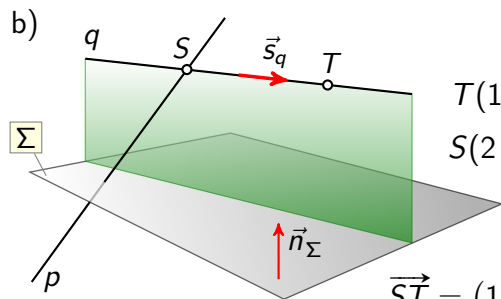
$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\Sigma \dots -2y + z - 1 = 0$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1,$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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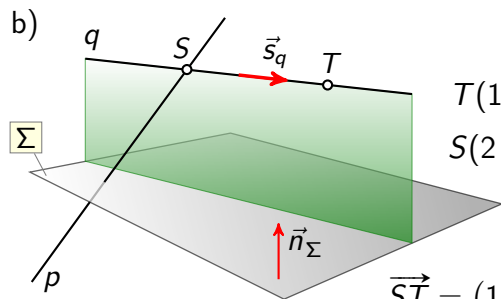
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$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_\Sigma \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_\Sigma = 0}$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$\vec{n}_{\Sigma} = (0, -2, 1)$$

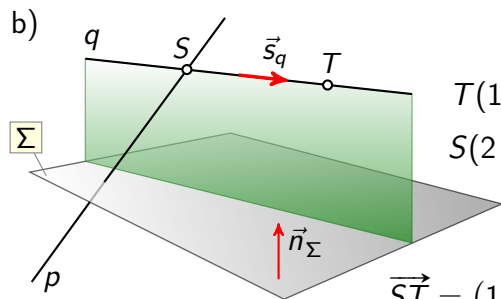
$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

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$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1 - t, t - 1, 5) \cdot$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

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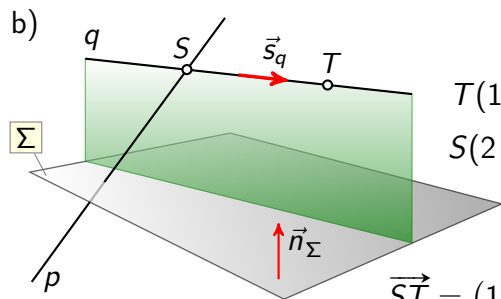
$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1)$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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$$\vec{n}_{\Sigma} = (0, -2, 1)$$

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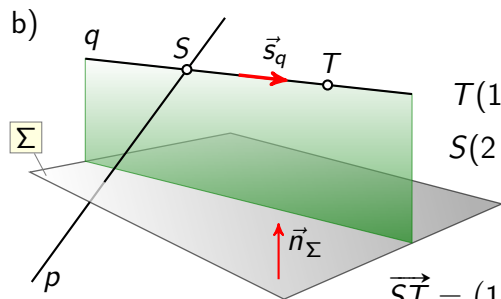
$$\vec{ST} = (-1 - t, t - 1, 5)$$

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$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$





$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

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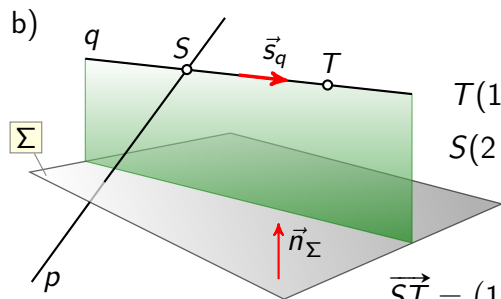
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$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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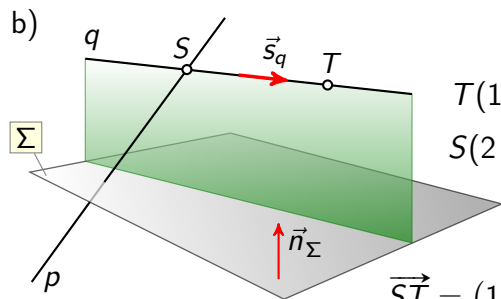
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$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2)$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

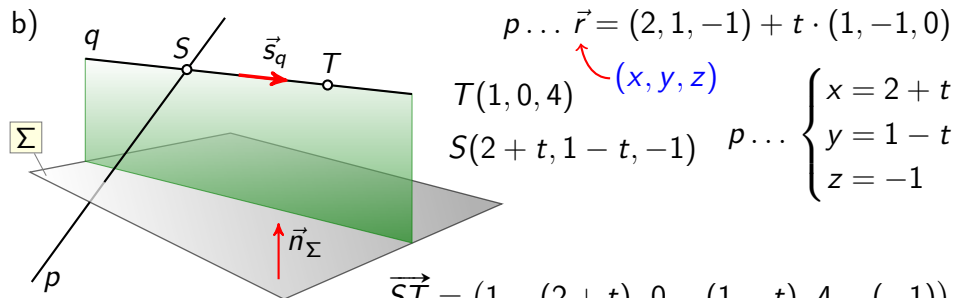
$$\vec{ST} = (-1 - t, t - 1, 5)$$

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$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_\Sigma \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_\Sigma = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1$$



$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

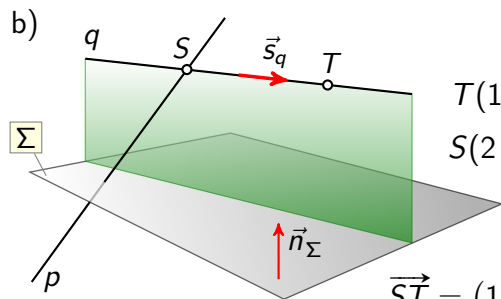
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$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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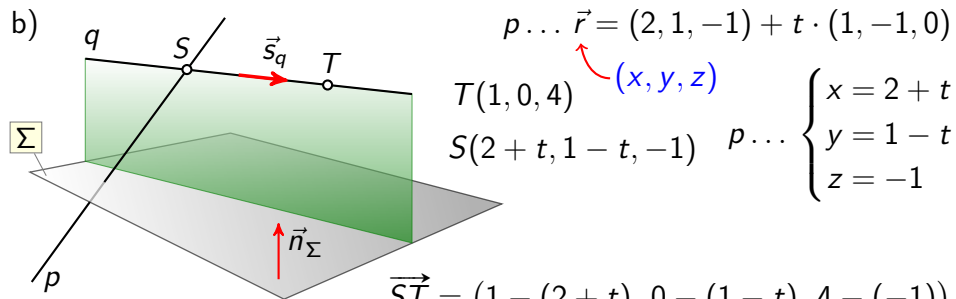
$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0$$



$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

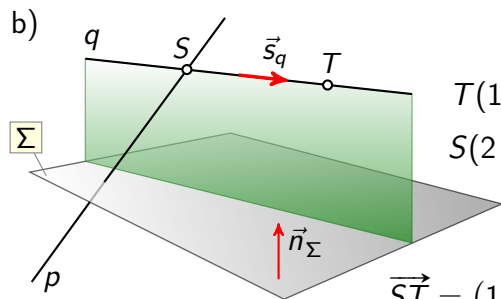
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$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow t = \frac{7}{2}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

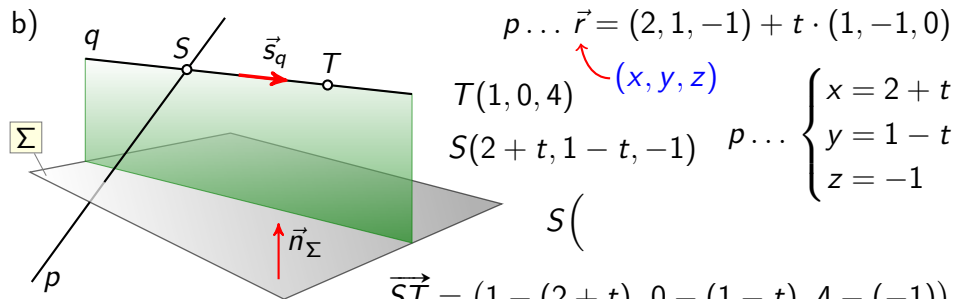
$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\Sigma \dots -2y + z - 1 = 0$$

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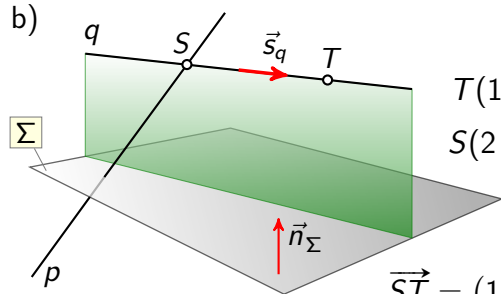
$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



b)



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

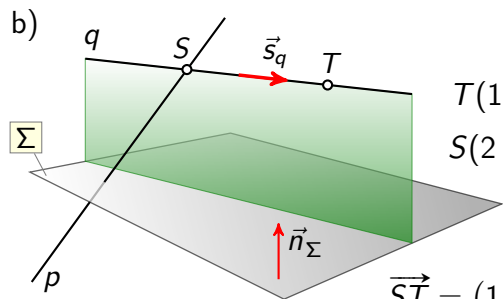
$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_\Sigma \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_\Sigma = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

$$\vec{ST} =$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

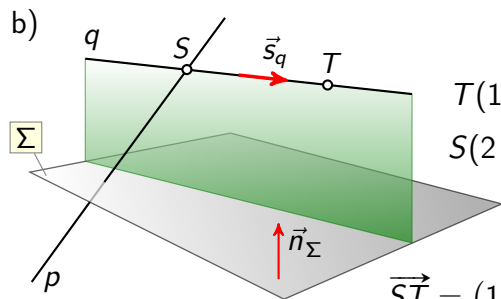
$$\Sigma \dots -2y + z - 1 = 0$$

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$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

$$\vec{ST} = \left(-\frac{9}{2}, \frac{5}{2}, 5\right)$$

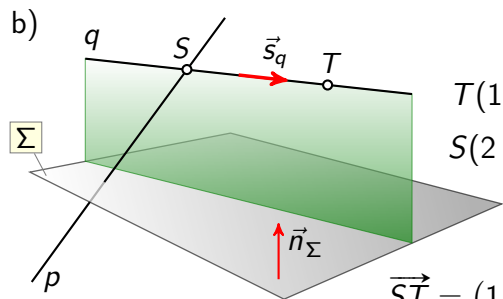
$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_\Sigma \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_\Sigma = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

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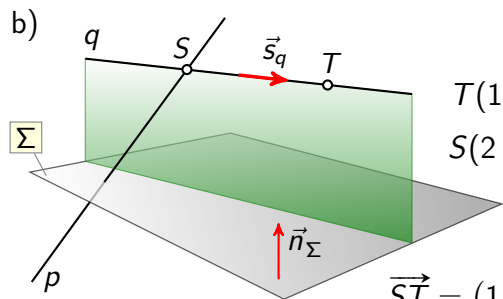
$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$\vec{s}_q = 2 \cdot \vec{ST}$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2 + t, 1 - t, -1) \quad p \dots \begin{cases} x = 2 + t \\ y = 1 - t \\ z = -1 \end{cases}$$

$$S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

$$\vec{ST} = \left(-\frac{9}{2}, \frac{5}{2}, 5\right)$$

$$\vec{s}_q = 2 \cdot \vec{ST} = (-9, 5, 10)$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

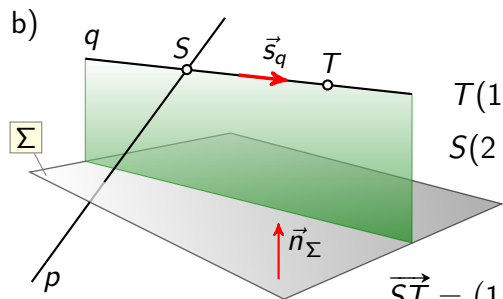
$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_\Sigma \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_\Sigma = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

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$$S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

$$\vec{ST} = \left(-\frac{9}{2}, \frac{5}{2}, 5\right)$$

$$\vec{s}_q = 2 \cdot \vec{ST} = (-9, 5, 10)$$

$$\vec{n}_\Sigma = (0, -2, 1)$$

$$\Sigma \dots -2y + z - 1 = 0$$

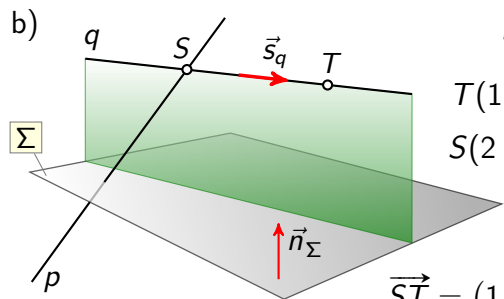
$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_\Sigma \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_\Sigma = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$

$$q \dots T, \vec{s}_q$$



$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z)$$

$$S(2+t, 1-t, -1) \quad p \dots \begin{cases} x = 2+t \\ y = 1-t \\ z = -1 \end{cases}$$

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$$\vec{ST} = (1 - (2+t), 0 - (1-t), 4 - (-1))$$

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$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1-t, t-1, 5) \cdot (0, -2, 1) = 0$$

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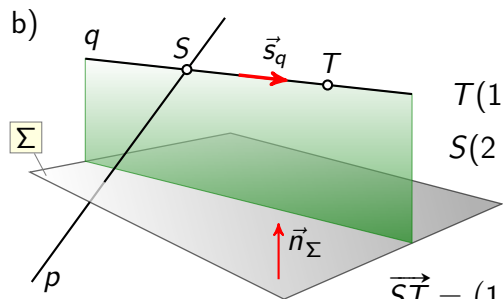
$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$

$$\vec{ST} = \left(-\frac{9}{2}, \frac{5}{2}, 5\right)$$

$$\vec{s}_q = 2 \cdot \vec{ST} = (-9, 5, 10)$$

$$q \dots \text{---} = \text{---} = \text{---}$$

$$q \dots T, \vec{s}_q$$



$$\vec{n}_{\Sigma} = (0, -2, 1)$$

$$\Sigma \dots -2y + z - 1 = 0$$

$$q \parallel \Sigma \Rightarrow \vec{ST} \perp \vec{n}_{\Sigma} \Rightarrow \boxed{\vec{ST} \cdot \vec{n}_{\Sigma} = 0}$$

$$(-1 - t, t - 1, 5) \cdot (0, -2, 1) = 0$$

$$(-1 - t) \cdot 0 + (t - 1) \cdot (-2) + 5 \cdot 1 = 0$$

$$-2t + 7 = 0 \rightsquigarrow \boxed{t = \frac{7}{2}}$$

$$p \dots \vec{r} = (2, 1, -1) + t \cdot (1, -1, 0)$$

$$T(1, 0, 4) \quad (x, y, z) \quad \left\{ \begin{array}{l} x = 2 + t \\ y = 1 - t \\ z = -1 \end{array} \right.$$

$$S(2 + t, 1 - t, -1) \quad p \dots S\left(\frac{11}{2}, -\frac{5}{2}, -1\right)$$

$$\vec{ST} = (1 - (2 + t), 0 - (1 - t), 4 - (-1))$$

$$\vec{ST} = (-1 - t, t - 1, 5)$$

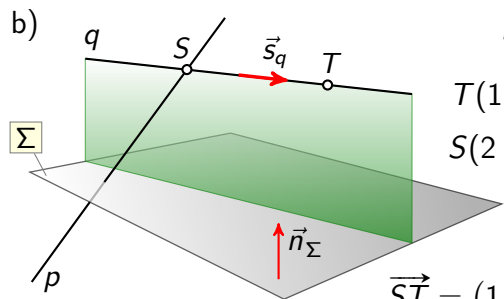
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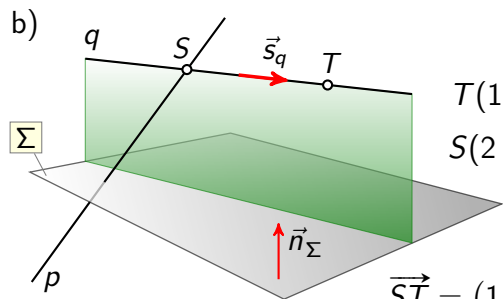
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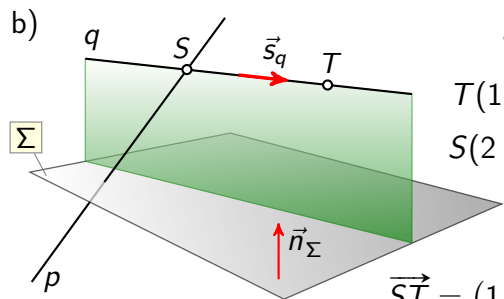
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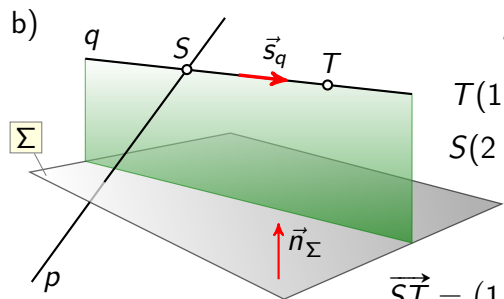
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